

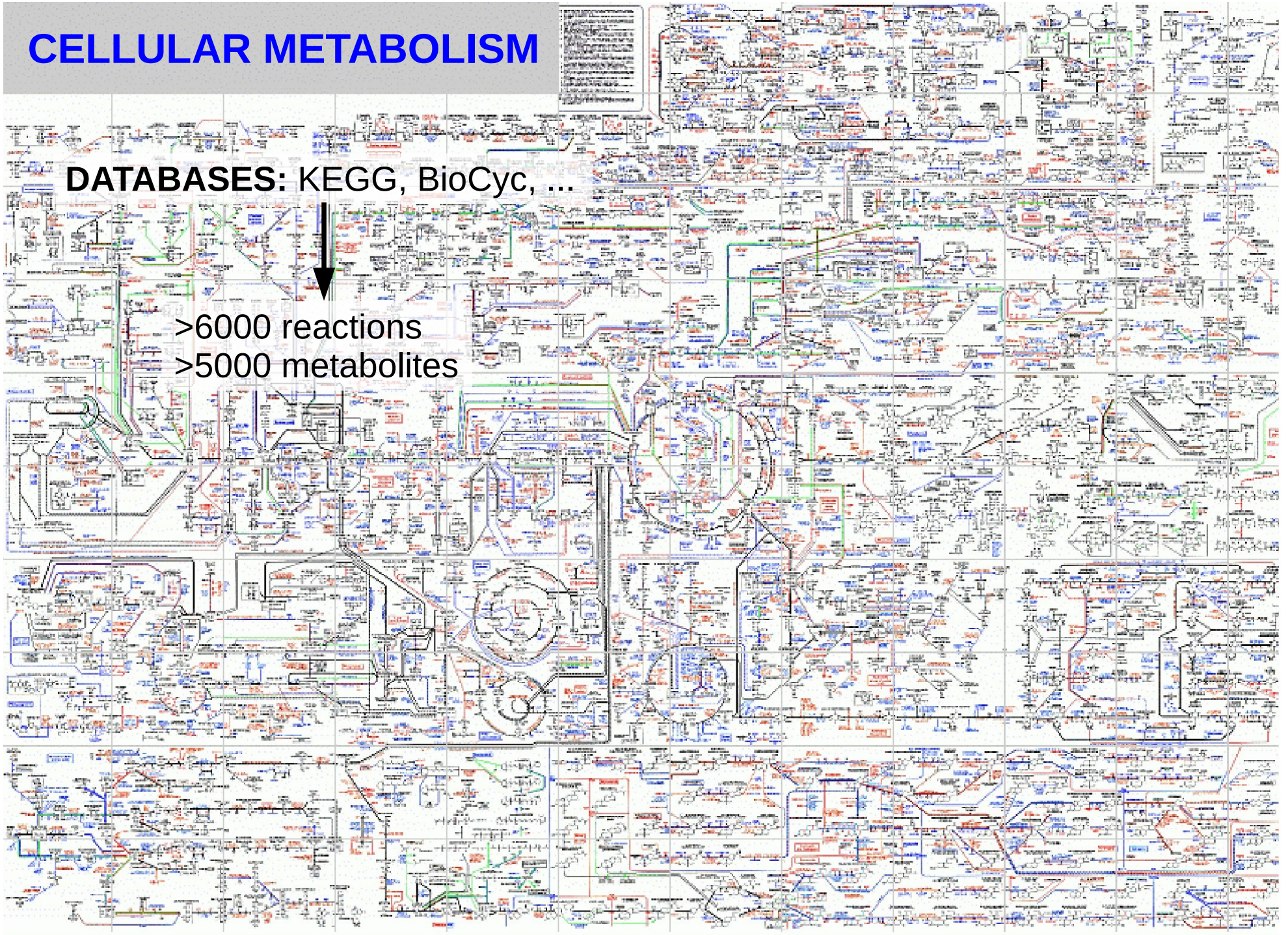
Network Expansion and Scopes

Oliver Ebenhöh

CELLULAR METABOLISM

DATABASES: KEGG, BioCyc, ...

↓
>6000 reactions
>5000 metabolites



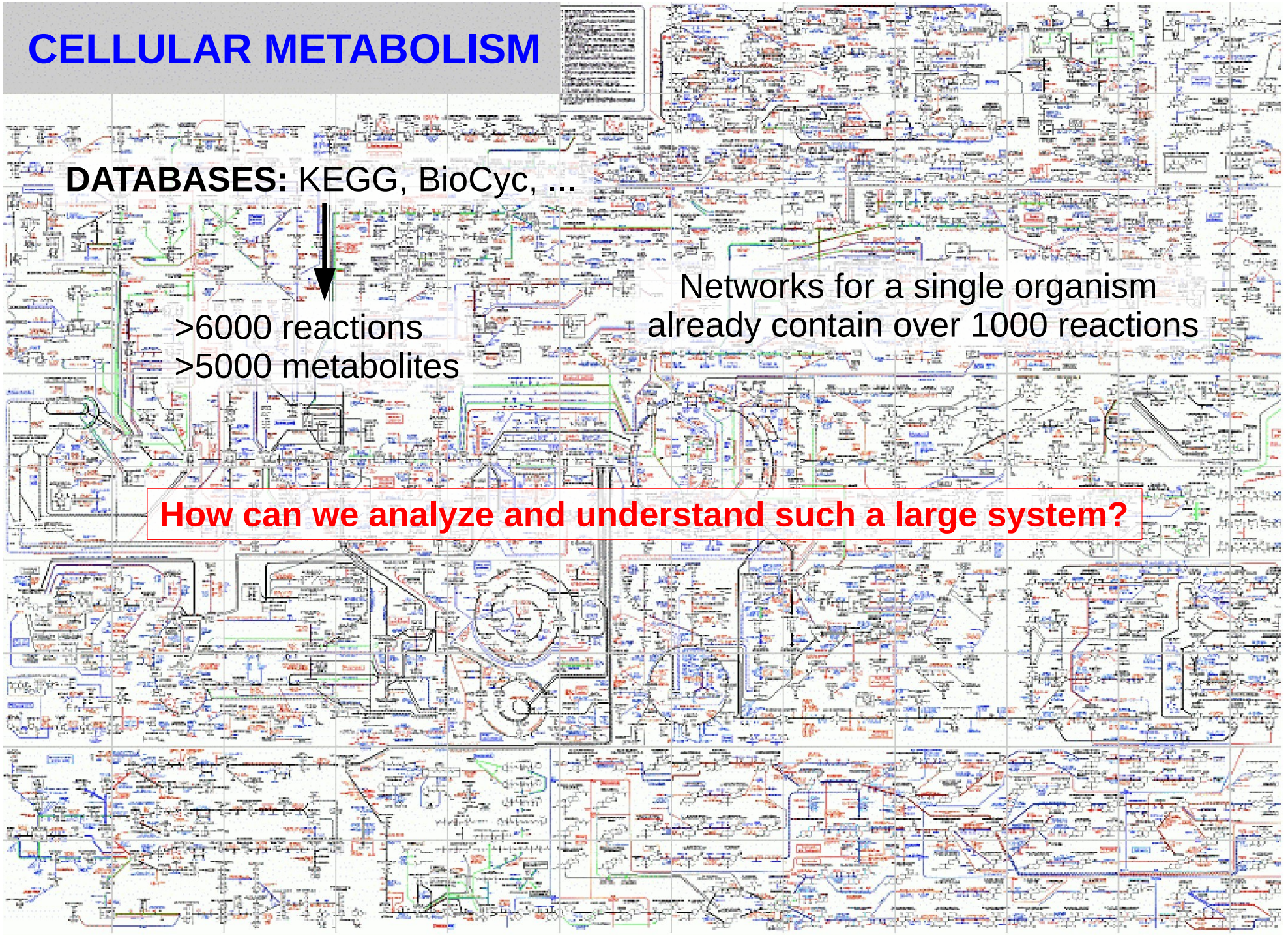
CELLULAR METABOLISM

DATABASES: KEGG, BioCyc, ...

>6000 reactions
>5000 metabolites

Networks for a single organism
already contain over 1000 reactions

How can we analyze and understand such a large system?



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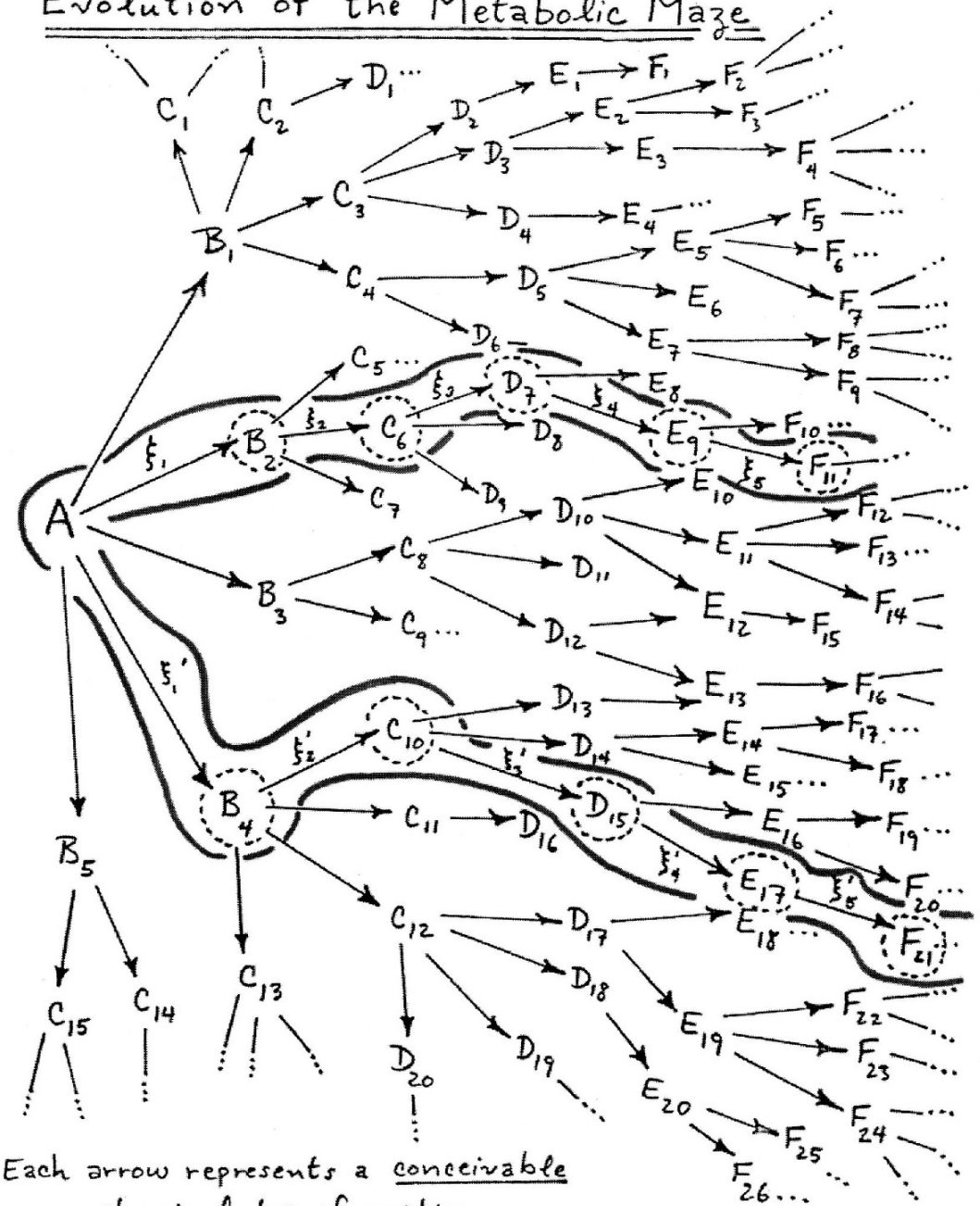
Networks for a single organism
already contain over 1000 reactions

How can we analyze and understand such a large system?

- Graph theory
- Elementary modes analysis
- Flux Balance Analysis
- Network expansion

Evolution of the Metabolic Maze

SCOTT C. MOHR
mohr@bu.edu



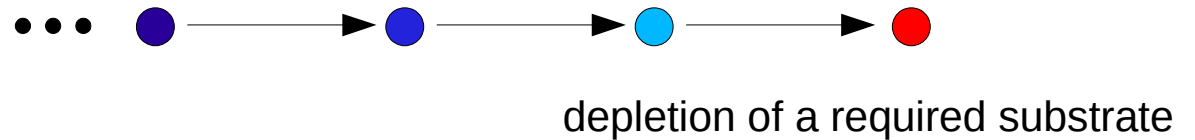
Each arrow represents a conceivable chemical transformation...

Pathway Evolution

- No *fossil record* of metabolism available
- The evolutionary history must have left imprints in the present structure

Existing hypotheses on metabolic evolution

retrograde evolution

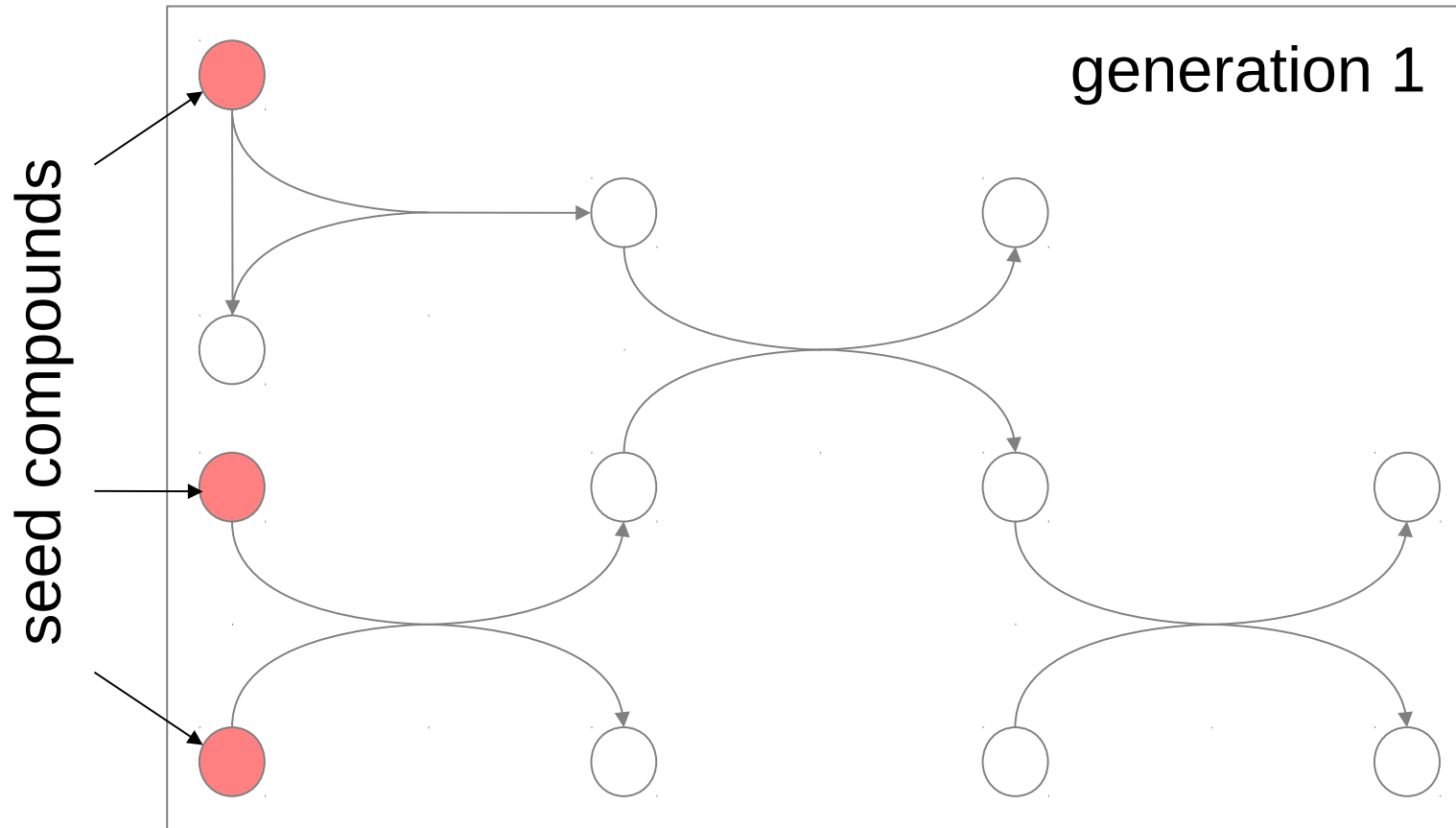


forward evolution

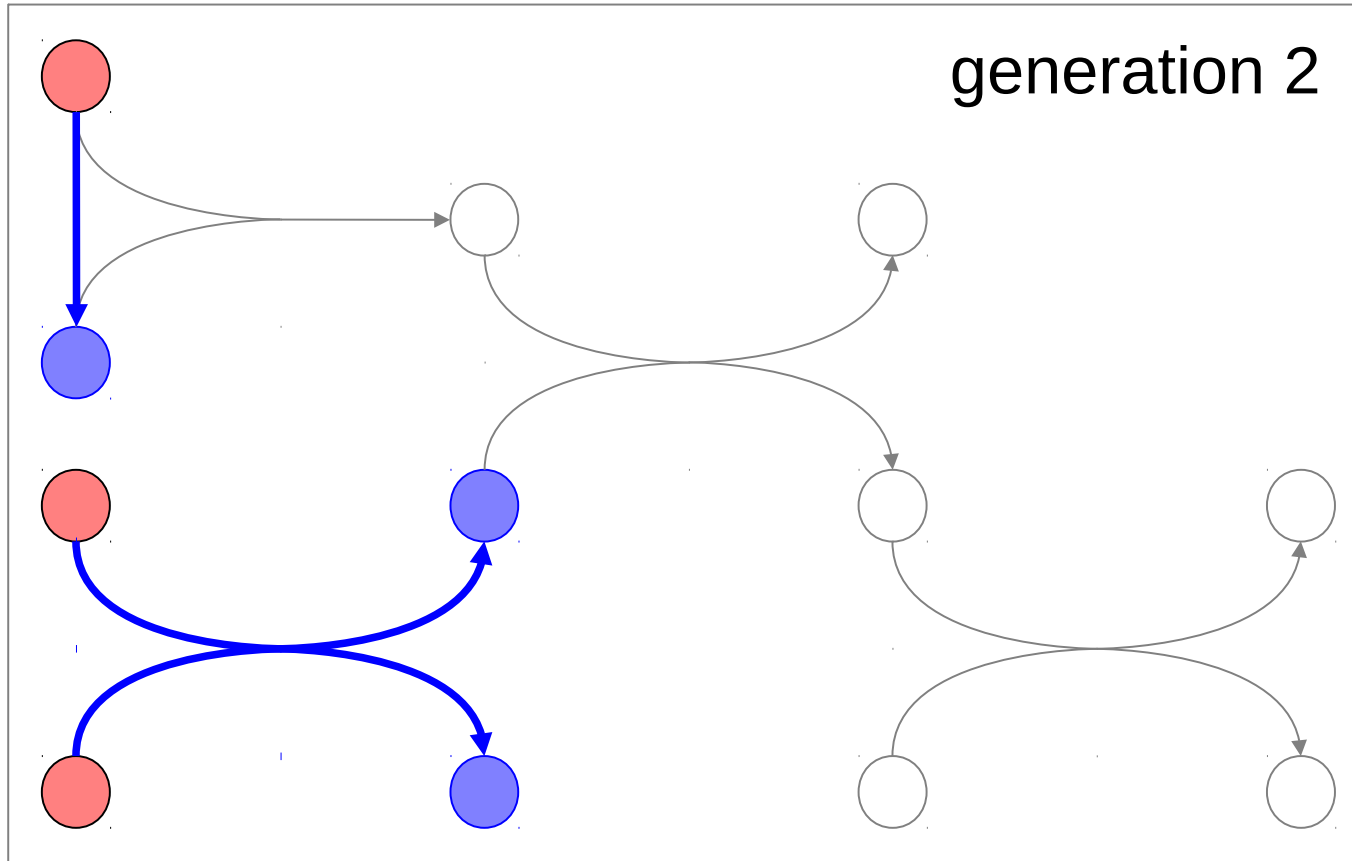


substrates in the environment trigger 'invention' of new metabolites

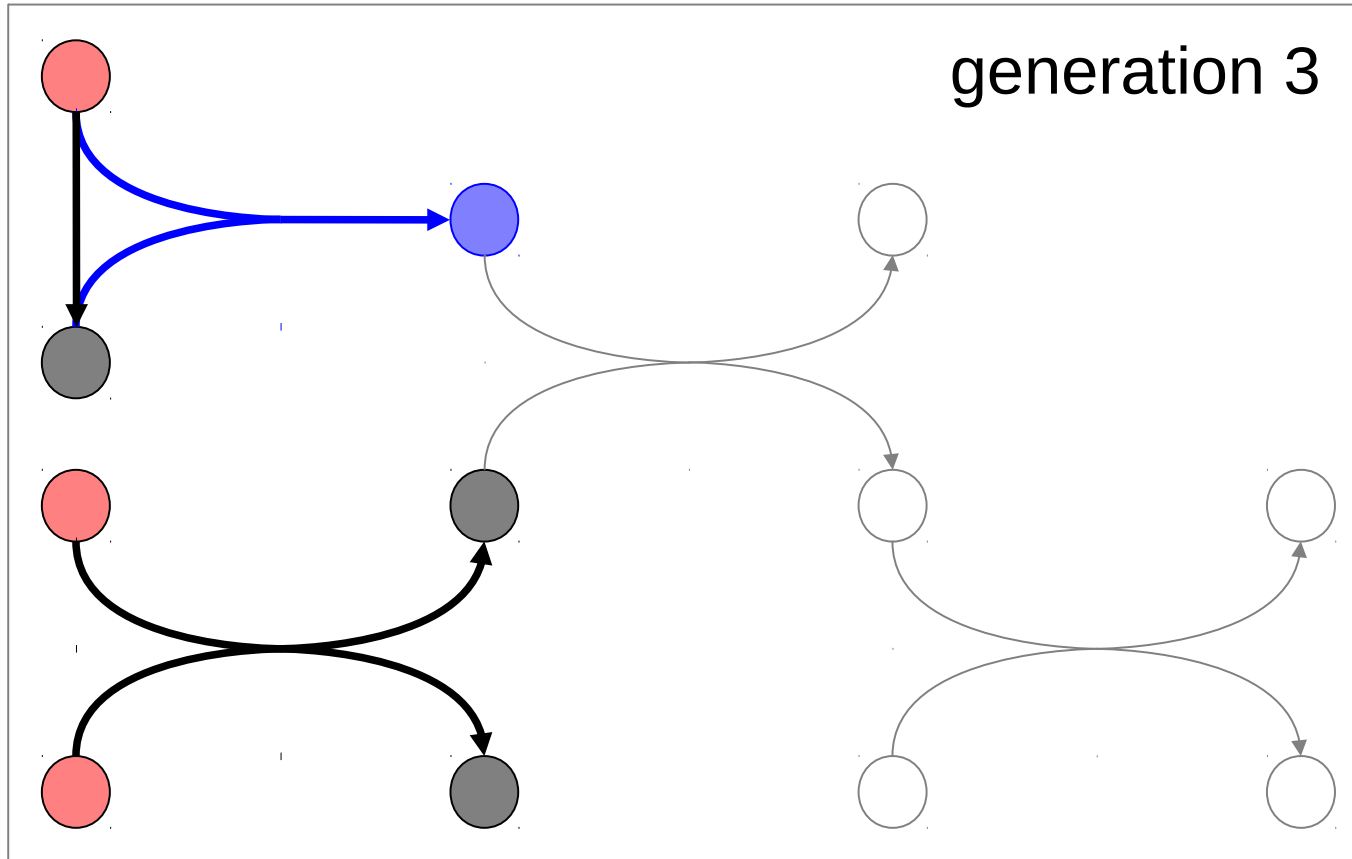
Concept of Network Expansion



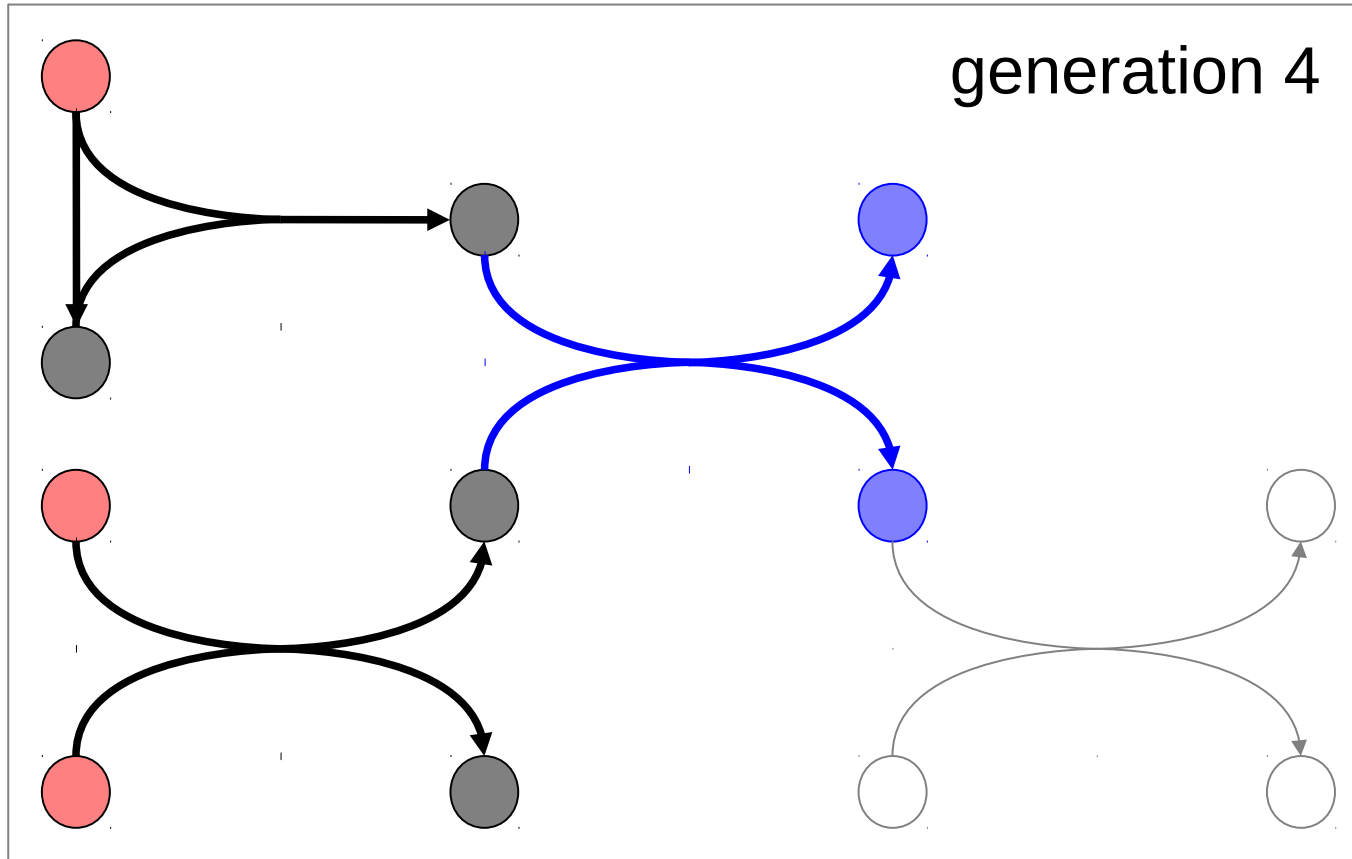
Concept of Network Expansion



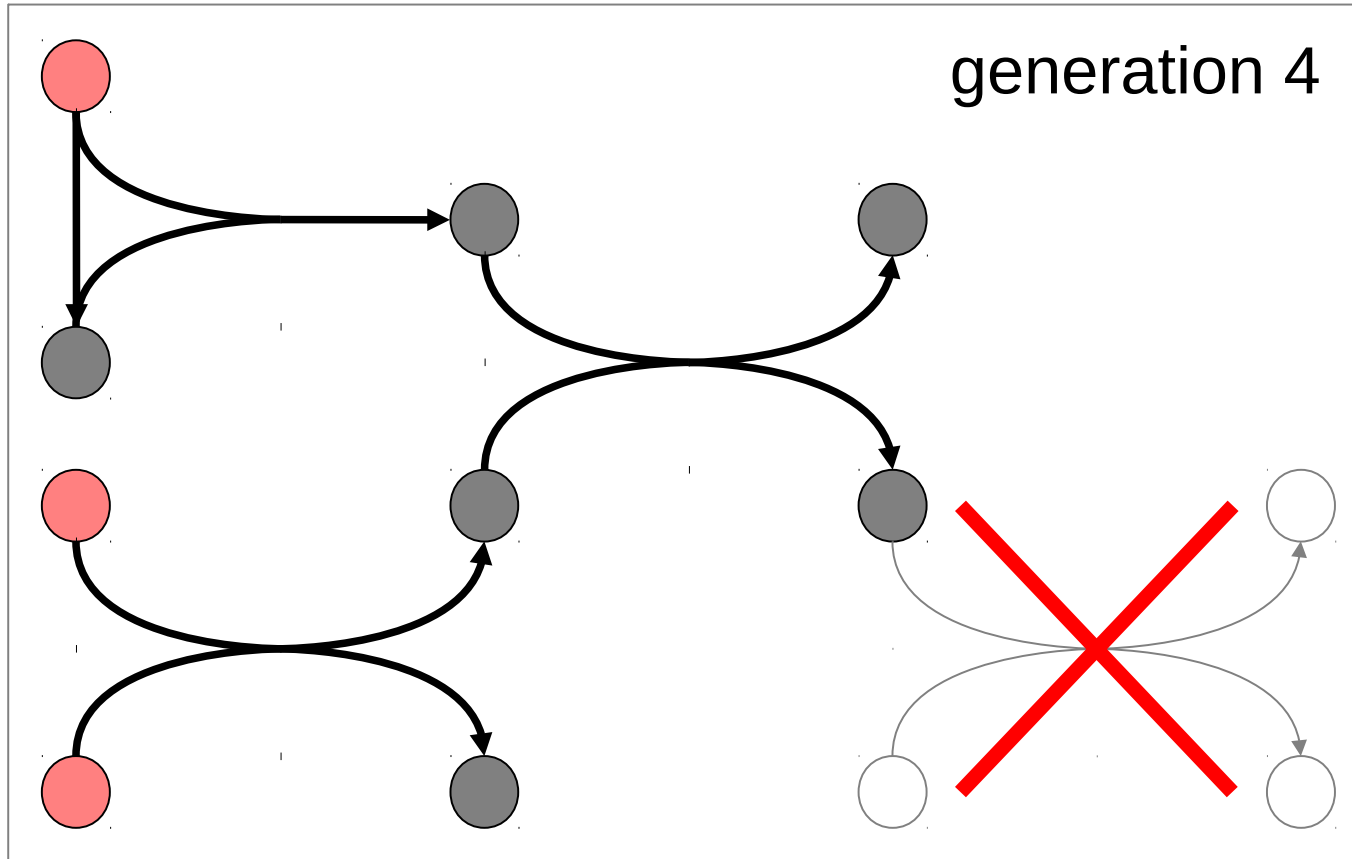
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Concept of Network Expansion

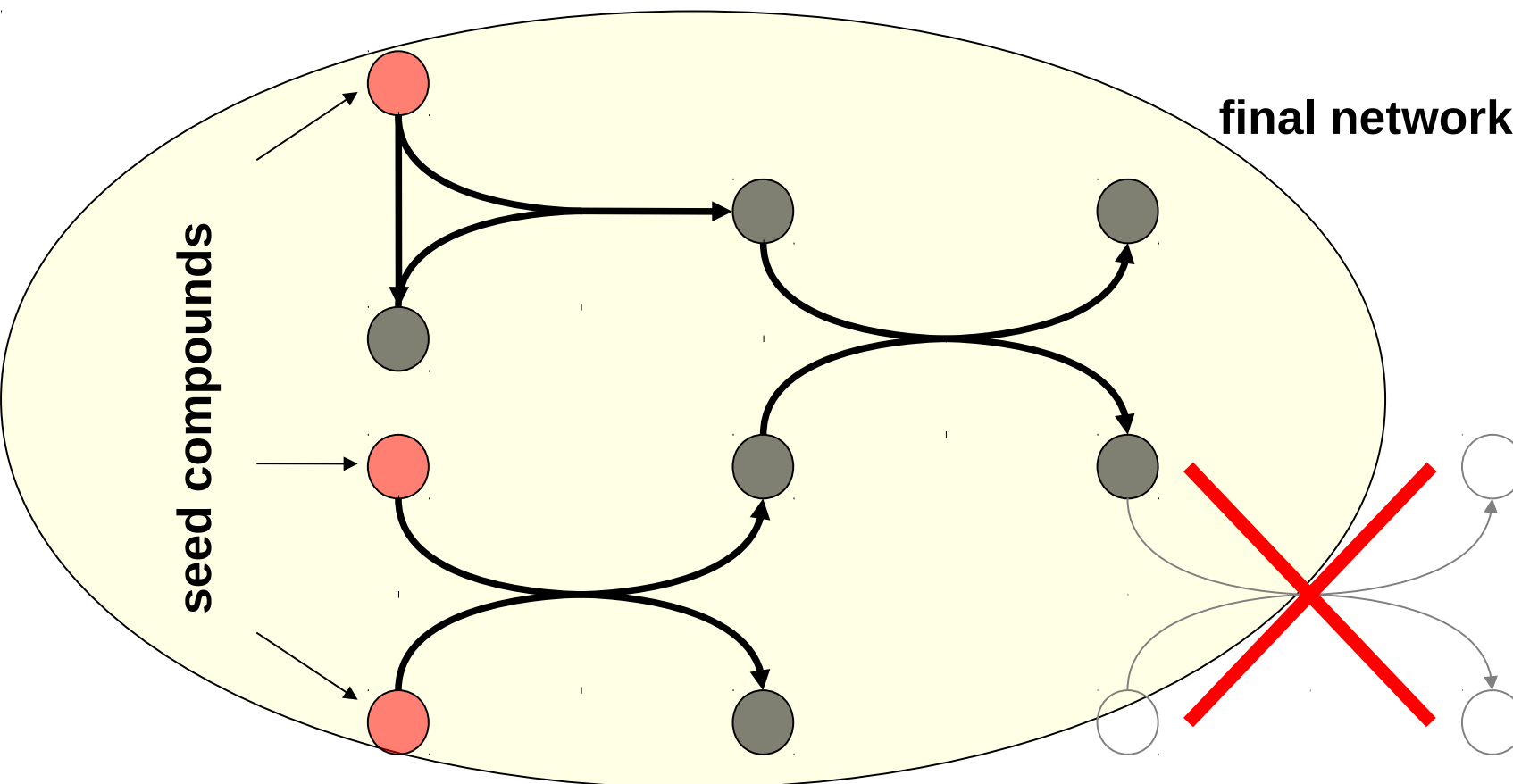


Concept of Network Expansion



Concept of Scopes

Scope: set of compounds that is reached by a network expansion



The Scope describes the synthesizing capacity of the metabolic network, if it is provided with the seed compounds

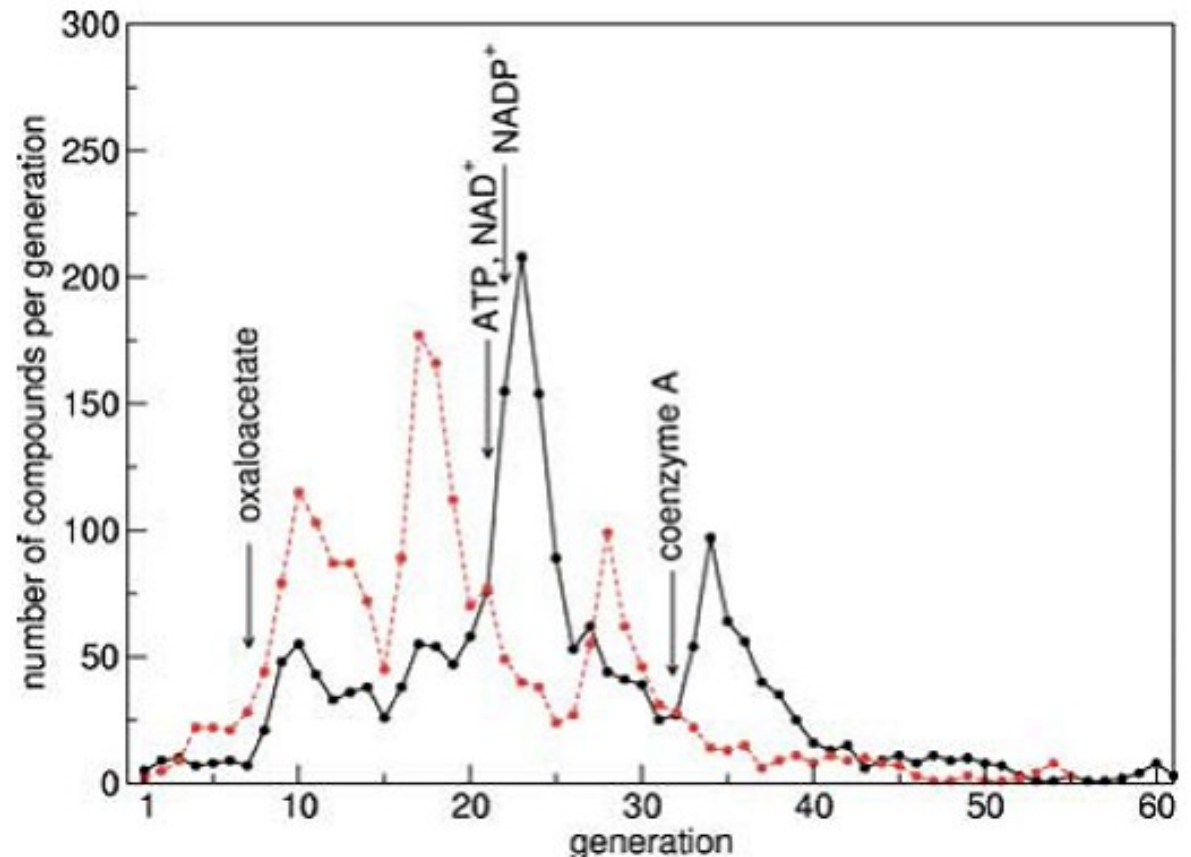
The expansion process

Initial conditions: availability of inorganic, 'prebiotic' compounds

(Martin and Russell, 2003)

carbonic acid:	H_2CO	(carbon)
methanethiol:	CH_3SH	(carbon, sulfur)
ammonia:	NH_3	(nitrogen)
pyrophosphate:	$\text{P}_2\text{O}_7^{4-}$	(phosphate)

Expansion on the
complete KEGG network



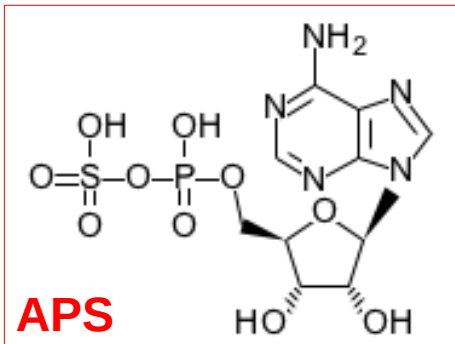
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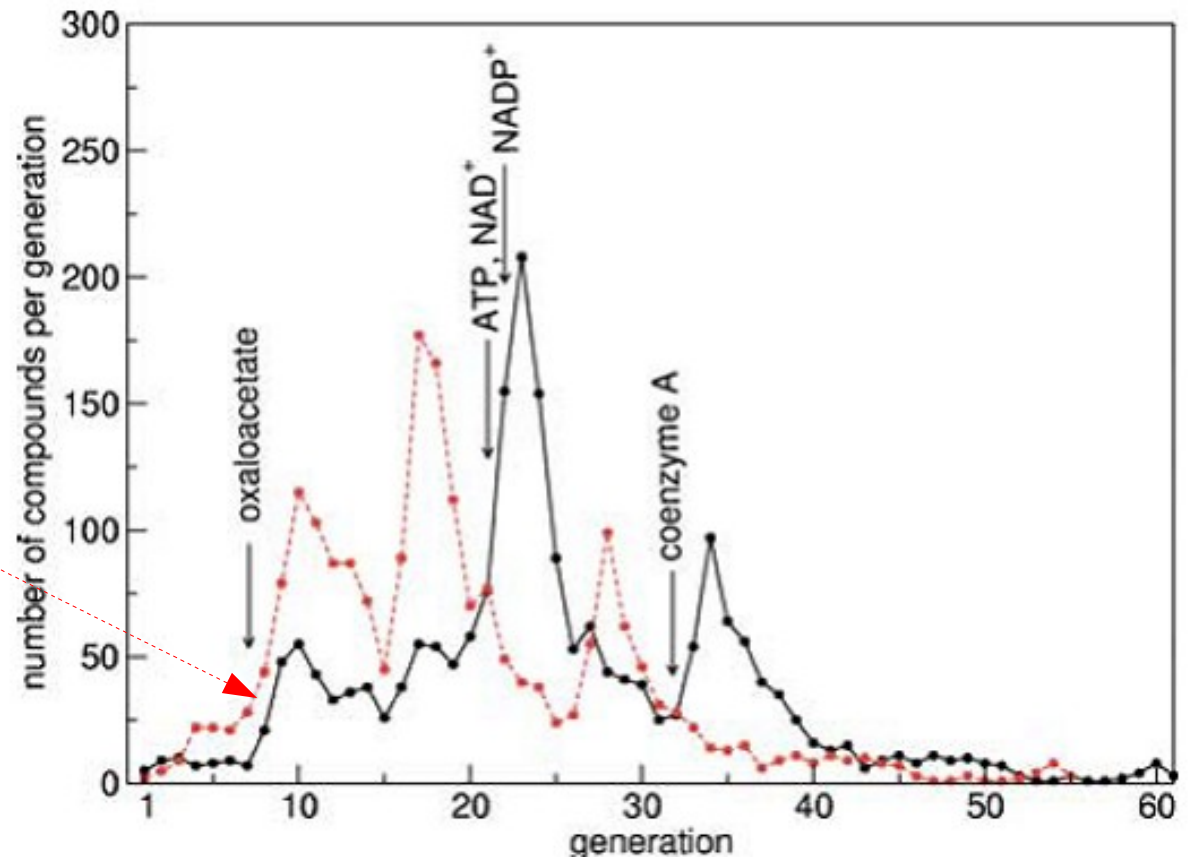
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Expansion on the complete KEGG network



APS

C00224



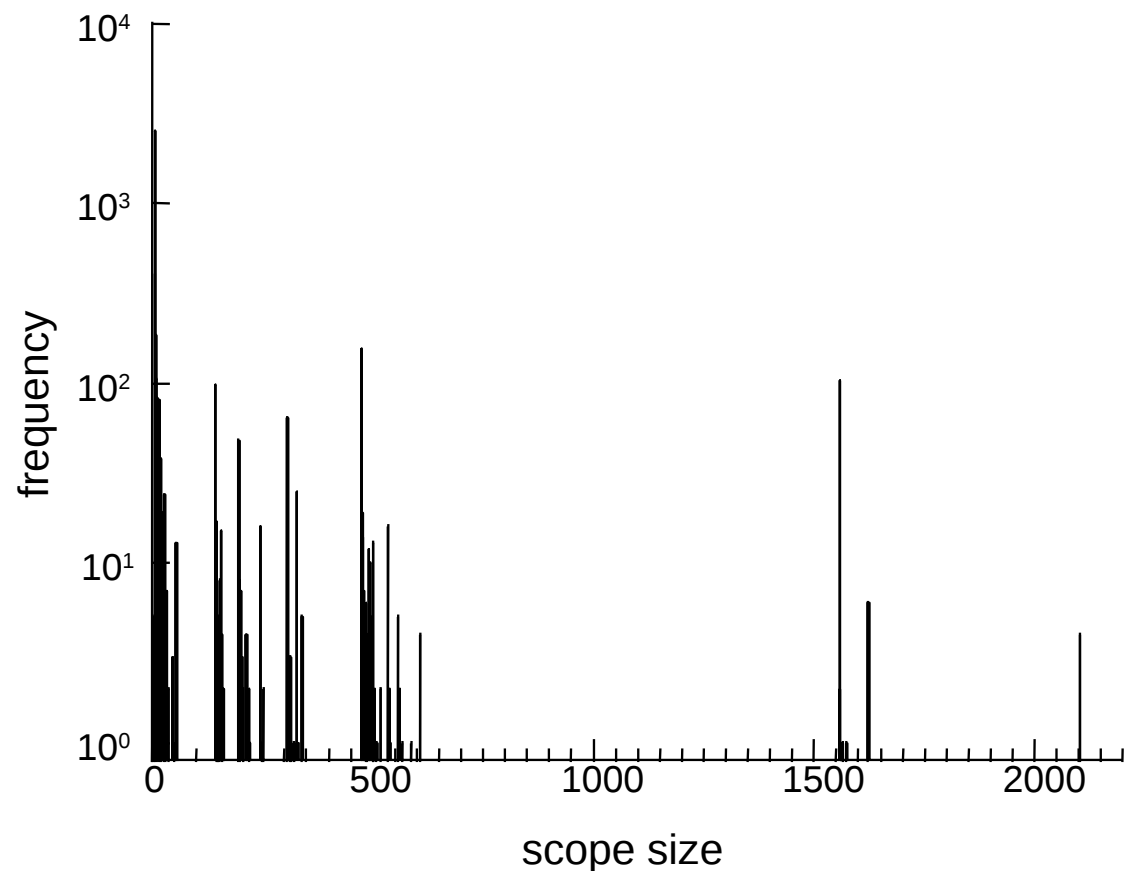
Analysis of the “global” network

A scope characterizes the
biosynthetic potential
of a chemical substance

Analysis of the “global” network

A scope characterizes the ***biosynthetic potential*** of a chemical substance

Characterize all metabolites!



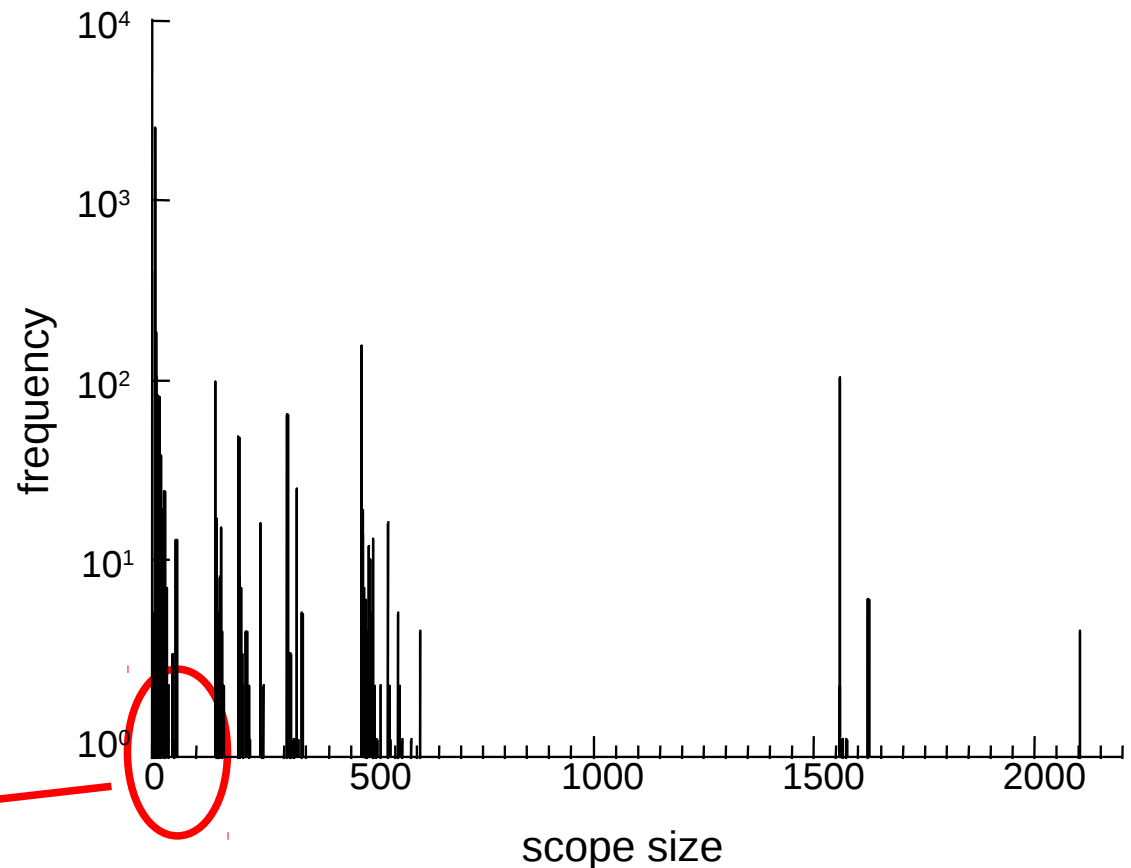
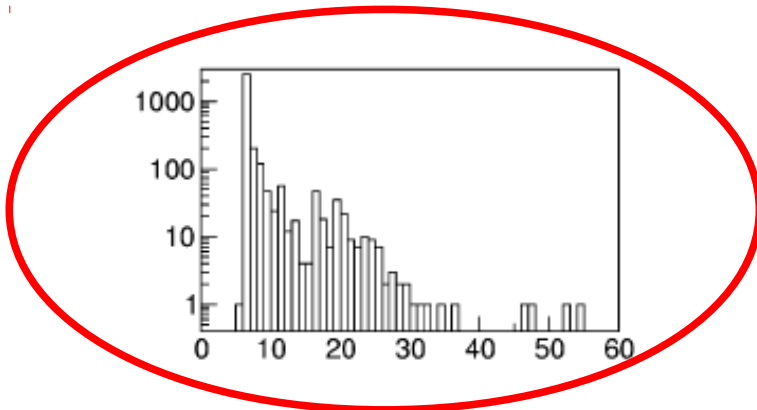
(Handorf, Ebenhöf and Heinrich, *J. Mol. Evol.*, 2005)

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Characterise all metabolites!

**MOST METABOLITES
CARRY A LOW POTENTIAL**



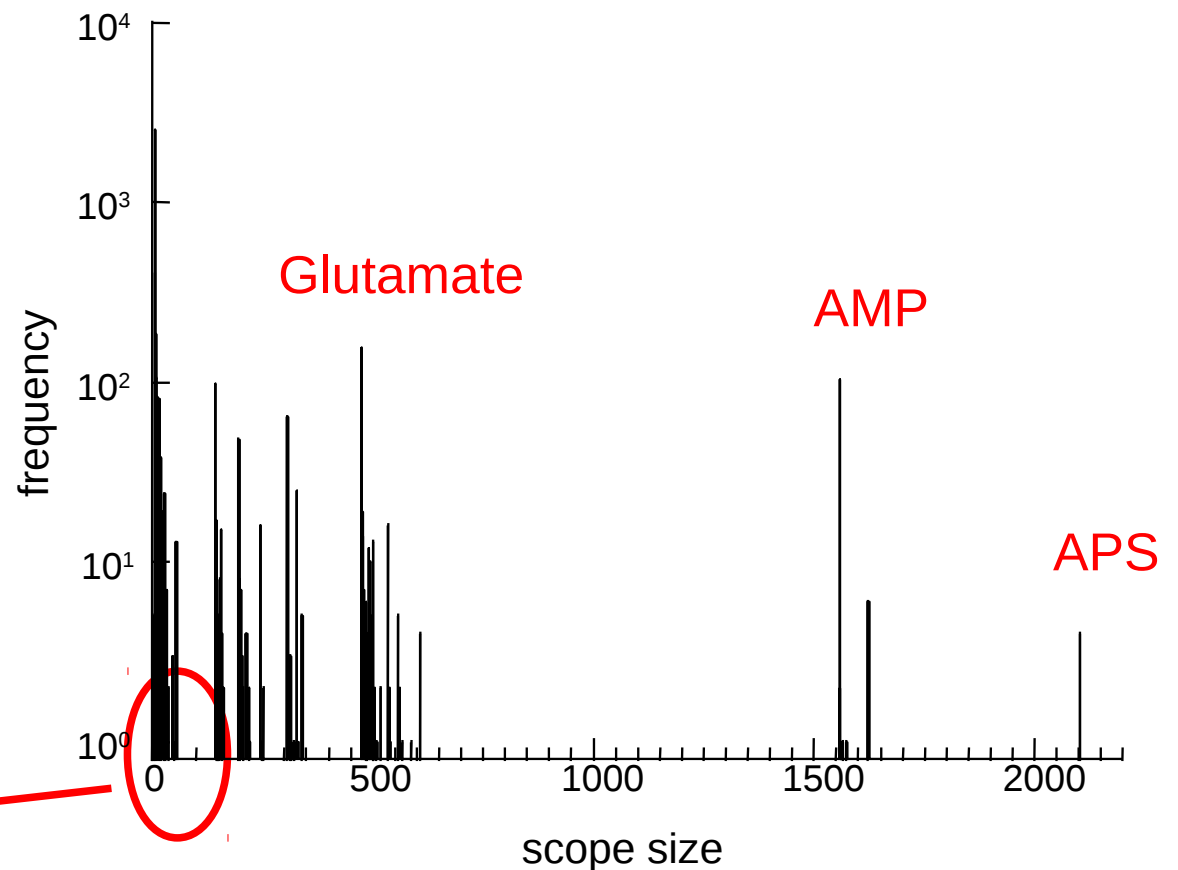
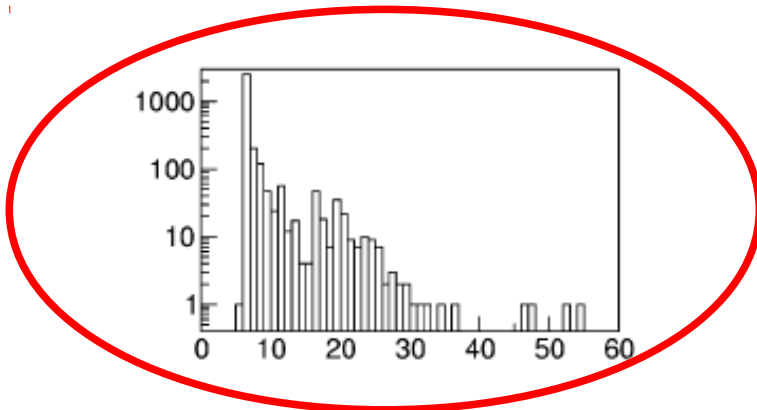
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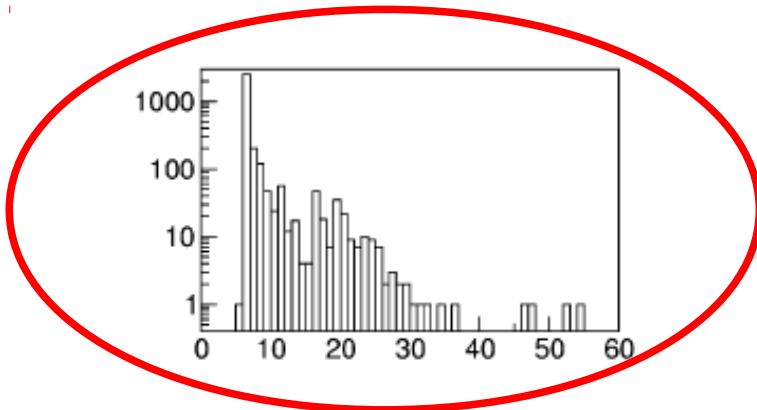
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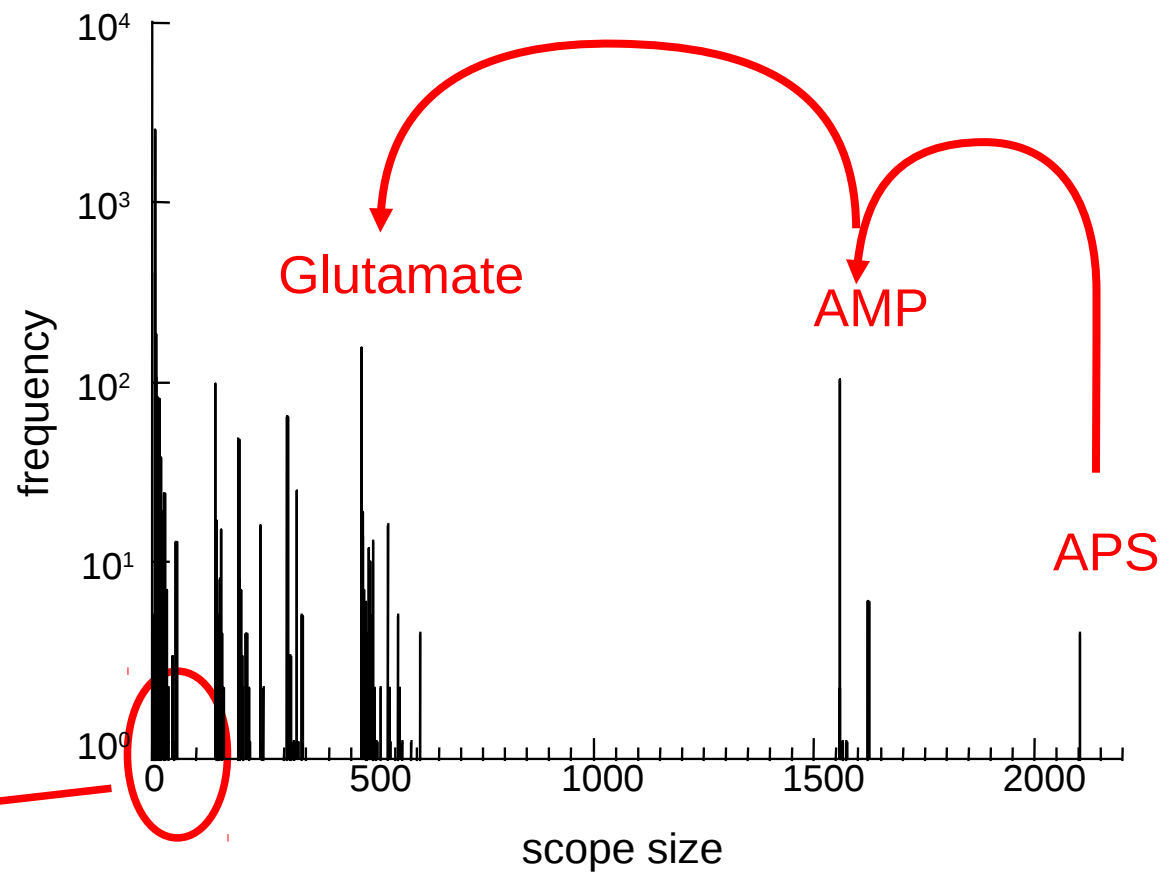
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Characterise all metabolites!

MOST METABOLITES CARRY A LOW POTENTIAL



SOME SCOPES ARE INCLUDED IN OTHERS



(Handorf, Ebenhöh and Heinrich, *J. Mol. Evol.*, 2005)

Global organisation of metabolism

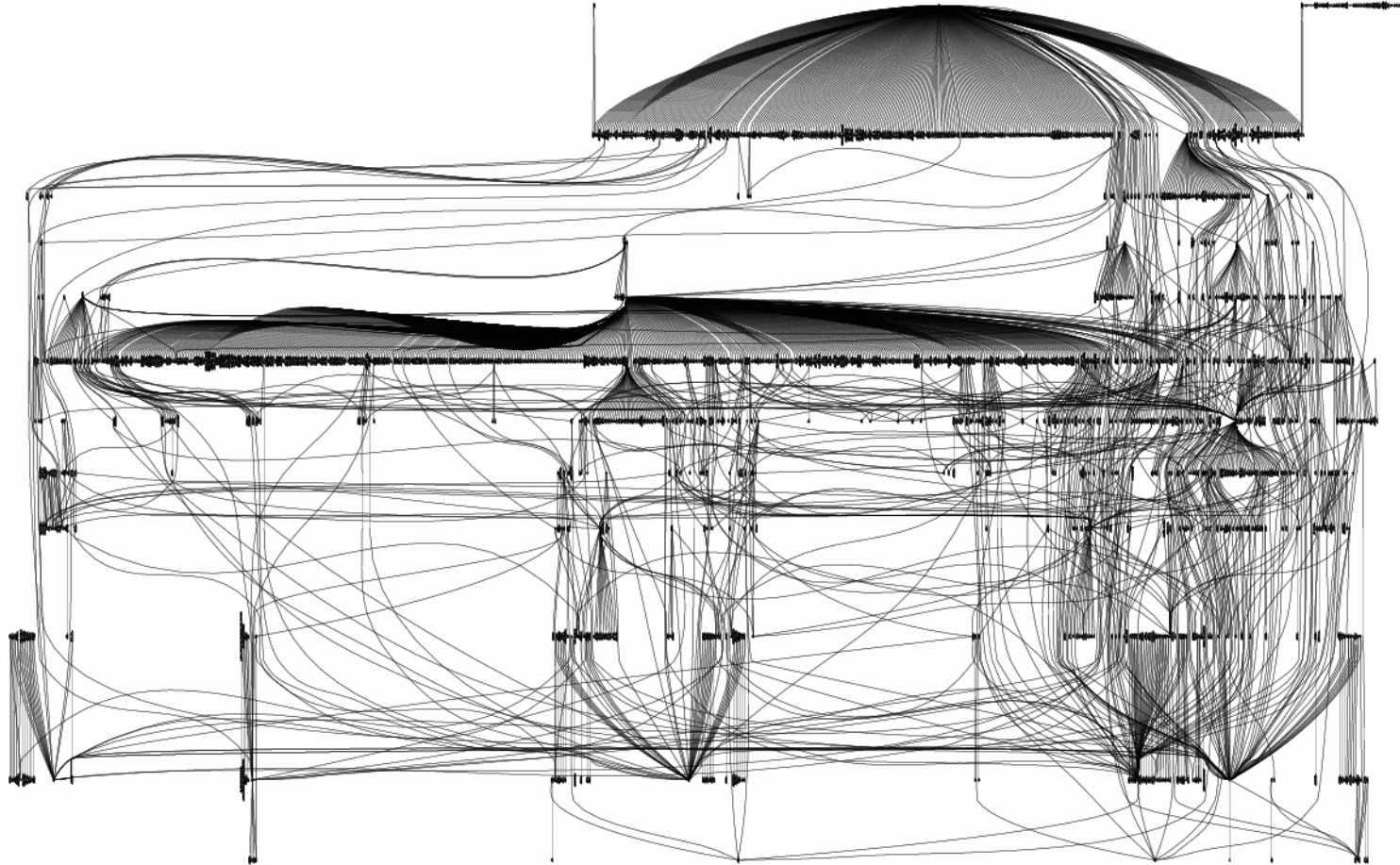
Reference network
from KEGG



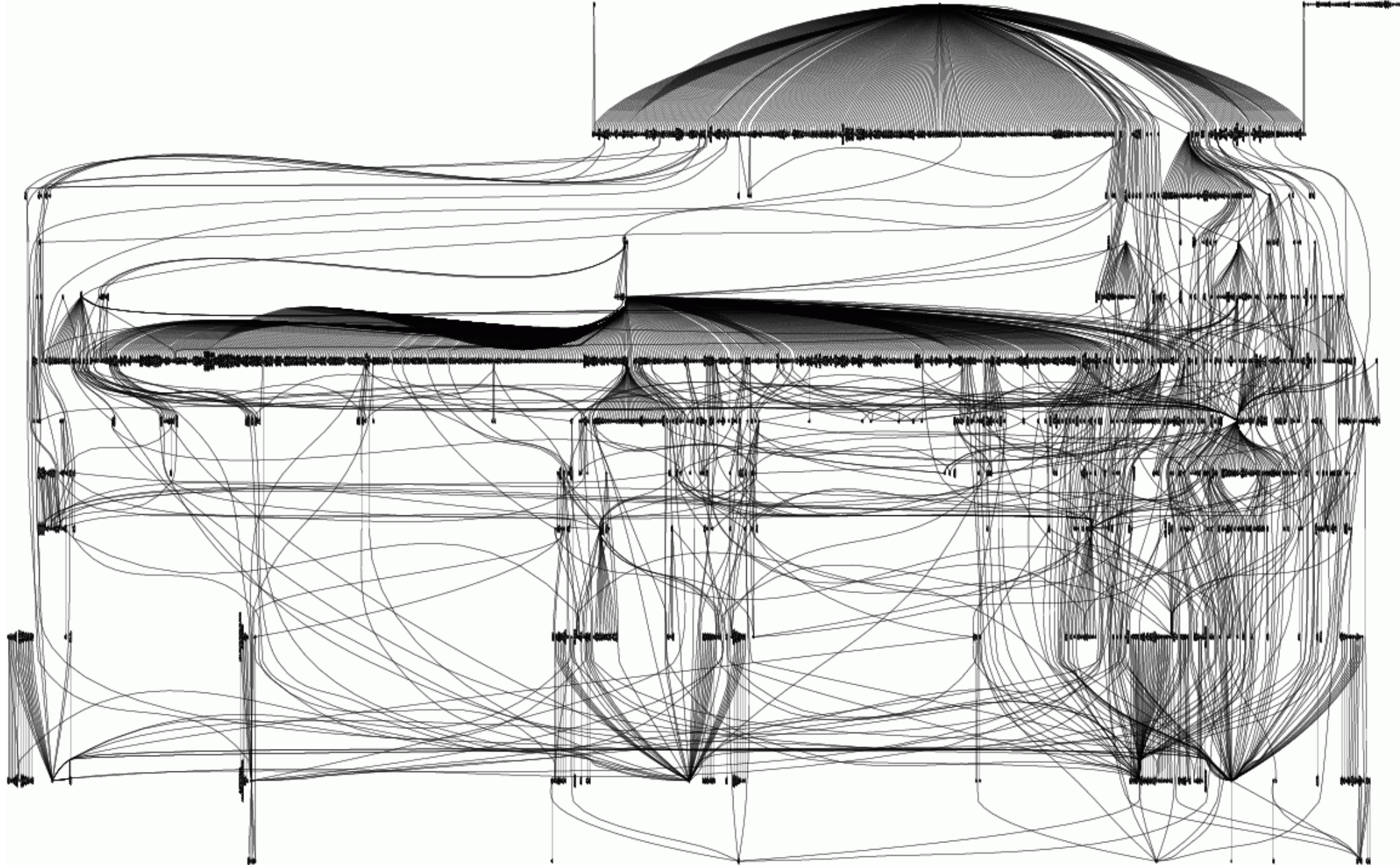
calculate all single
scopes



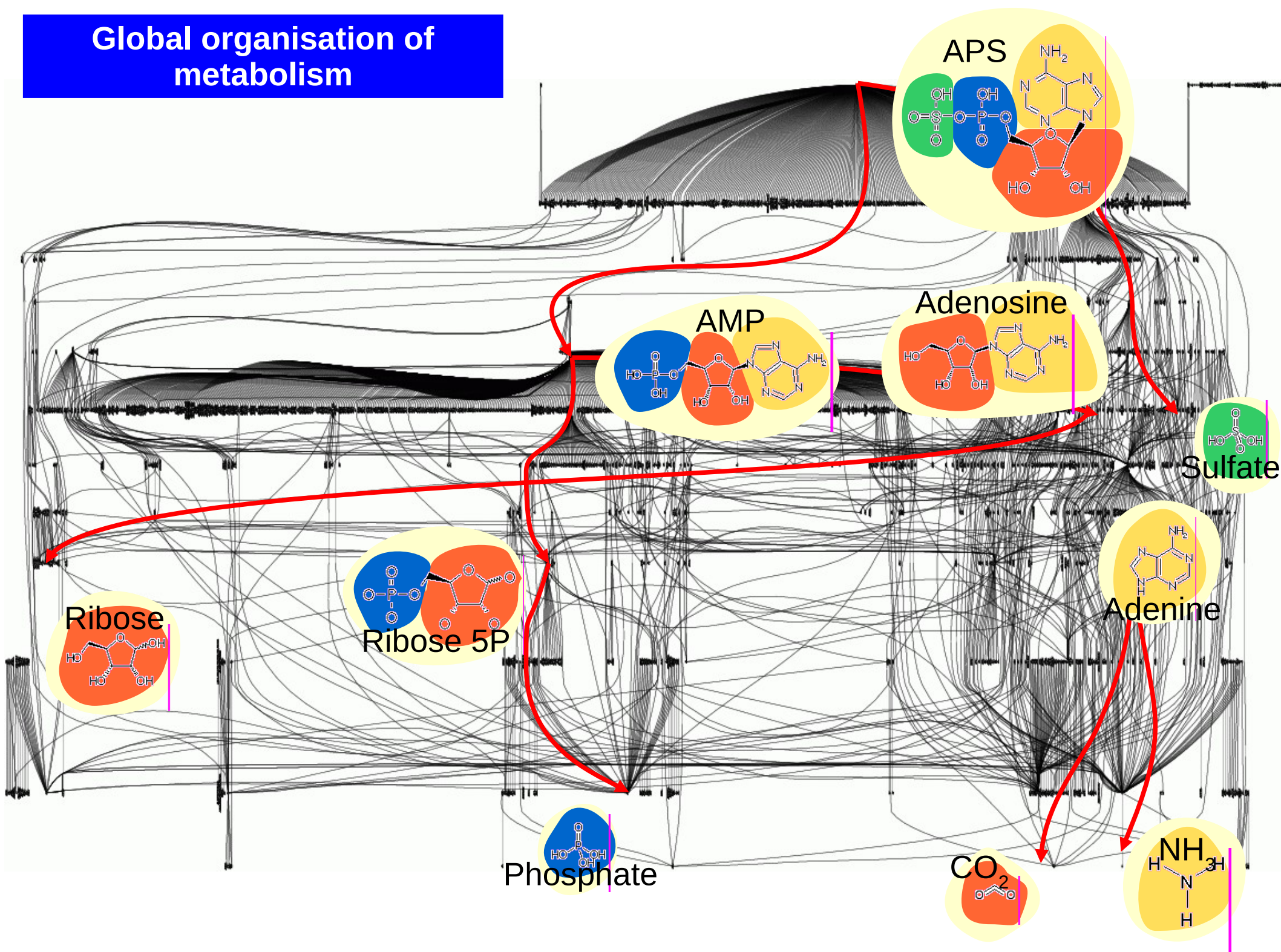
determine all
inclusion relations



Global organisation of metabolism



Global organisation of metabolism



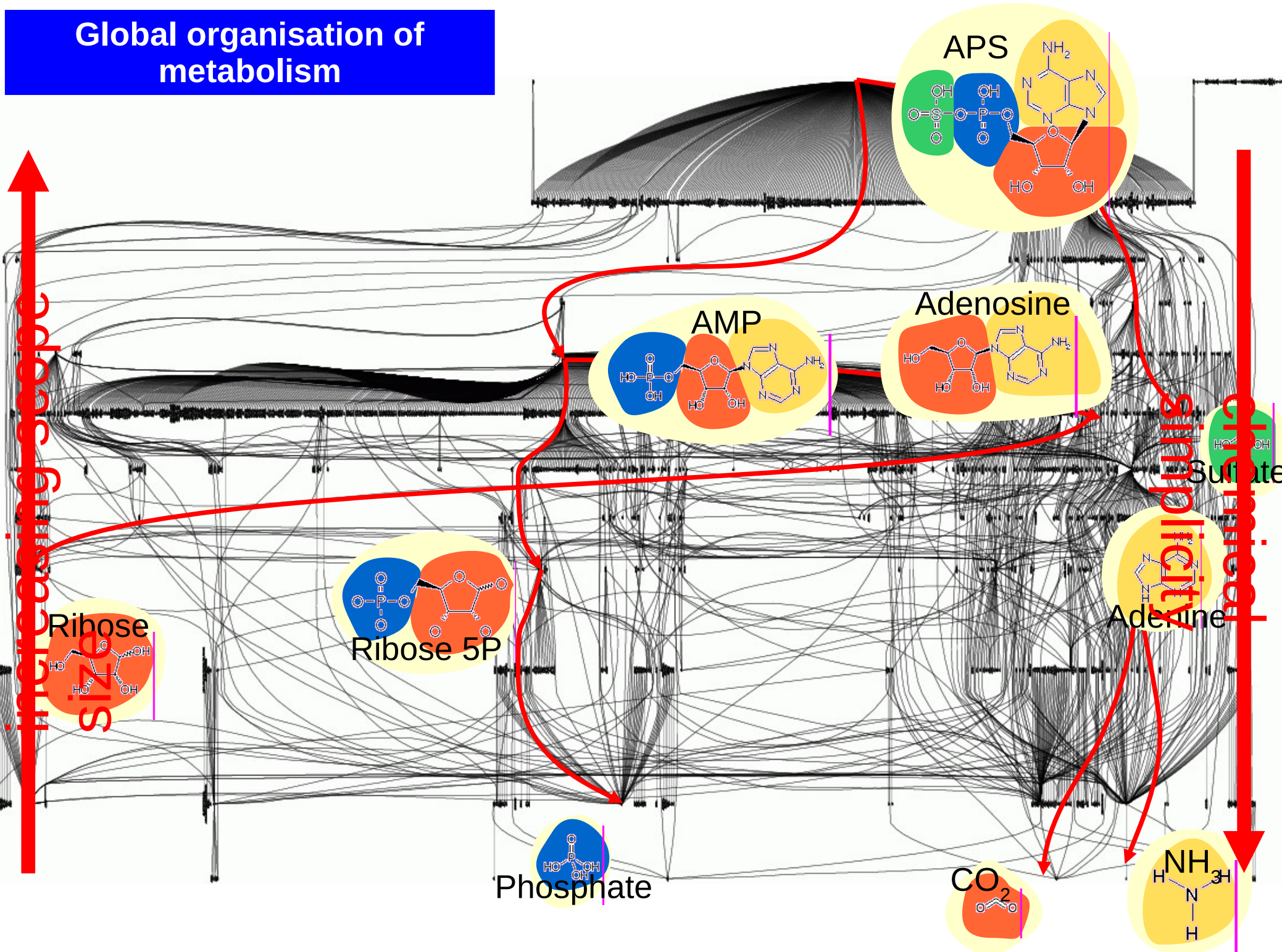
Global organisation of metabolism

↑ increasing scope

↑ size

↓ simplicity

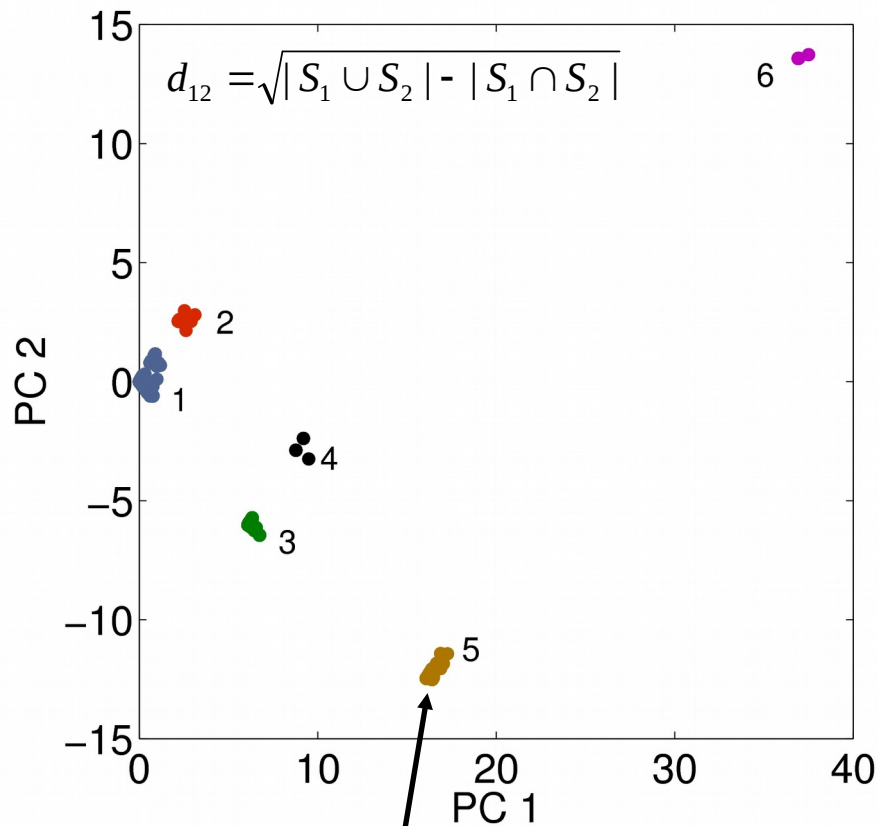
↓ molecular



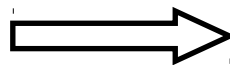
Similarity of biosynthetic potentials

Many metabolites carry *similar* biosynthetic potentials

Groups with similar potentials can be identified by *clustering analysis*



metabolites with similar
biosynthetic potentials

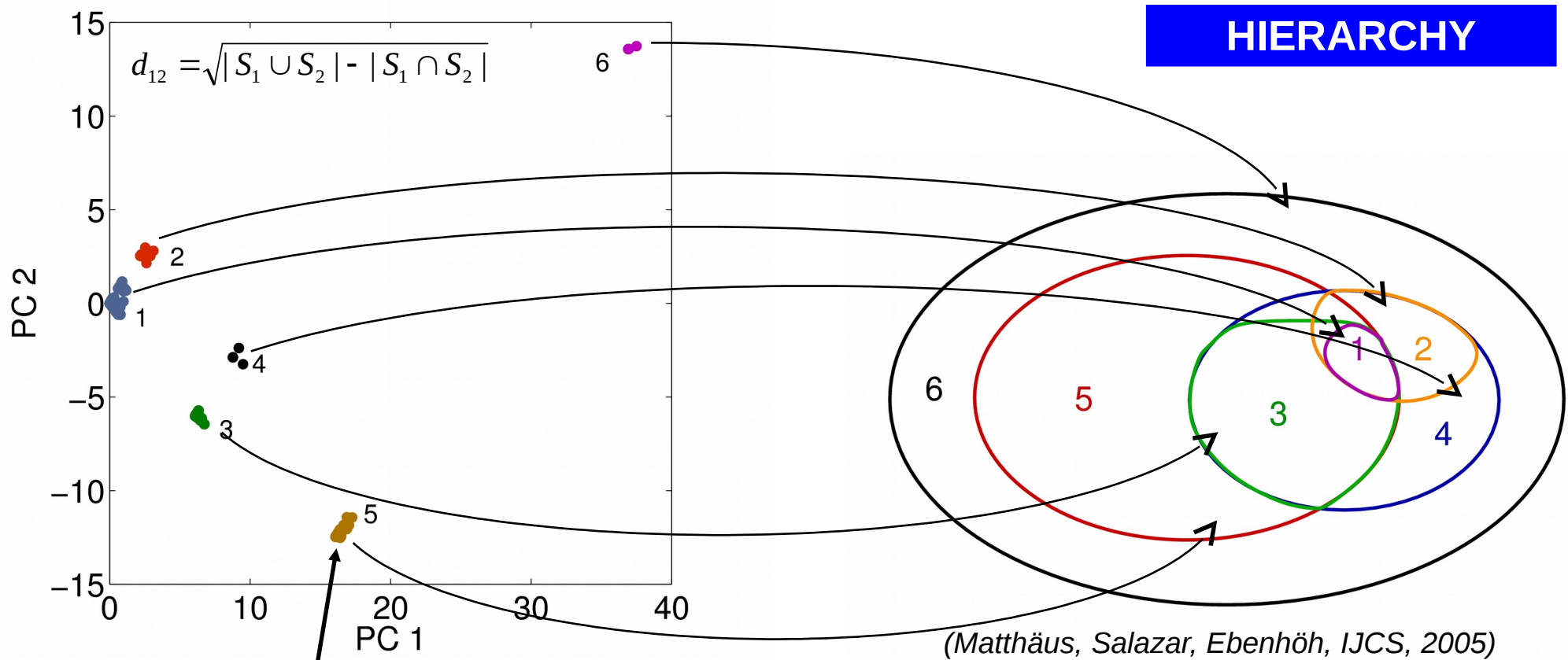


“consensus scope”
(typical biosynthetic potential)

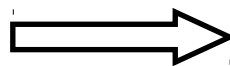
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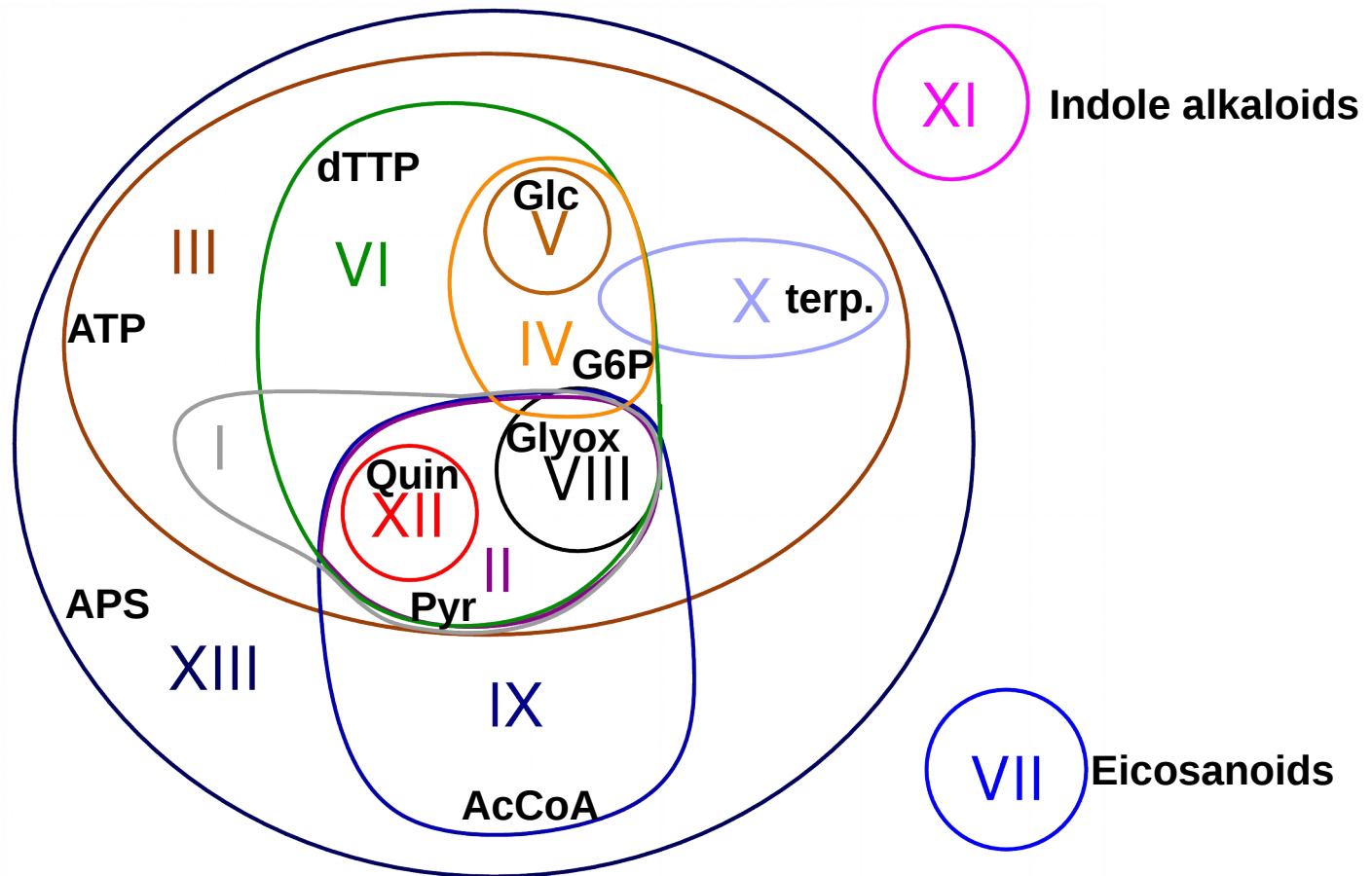
“*consensus scope*”
(typical biosynthetic potential)

Similarity of biosynthetic potentials

higher resolution with

$$d_{12} = 1 - \frac{|S_1 \cap S_2|}{|S_1 \cup S_2|}$$

HIERARCHY

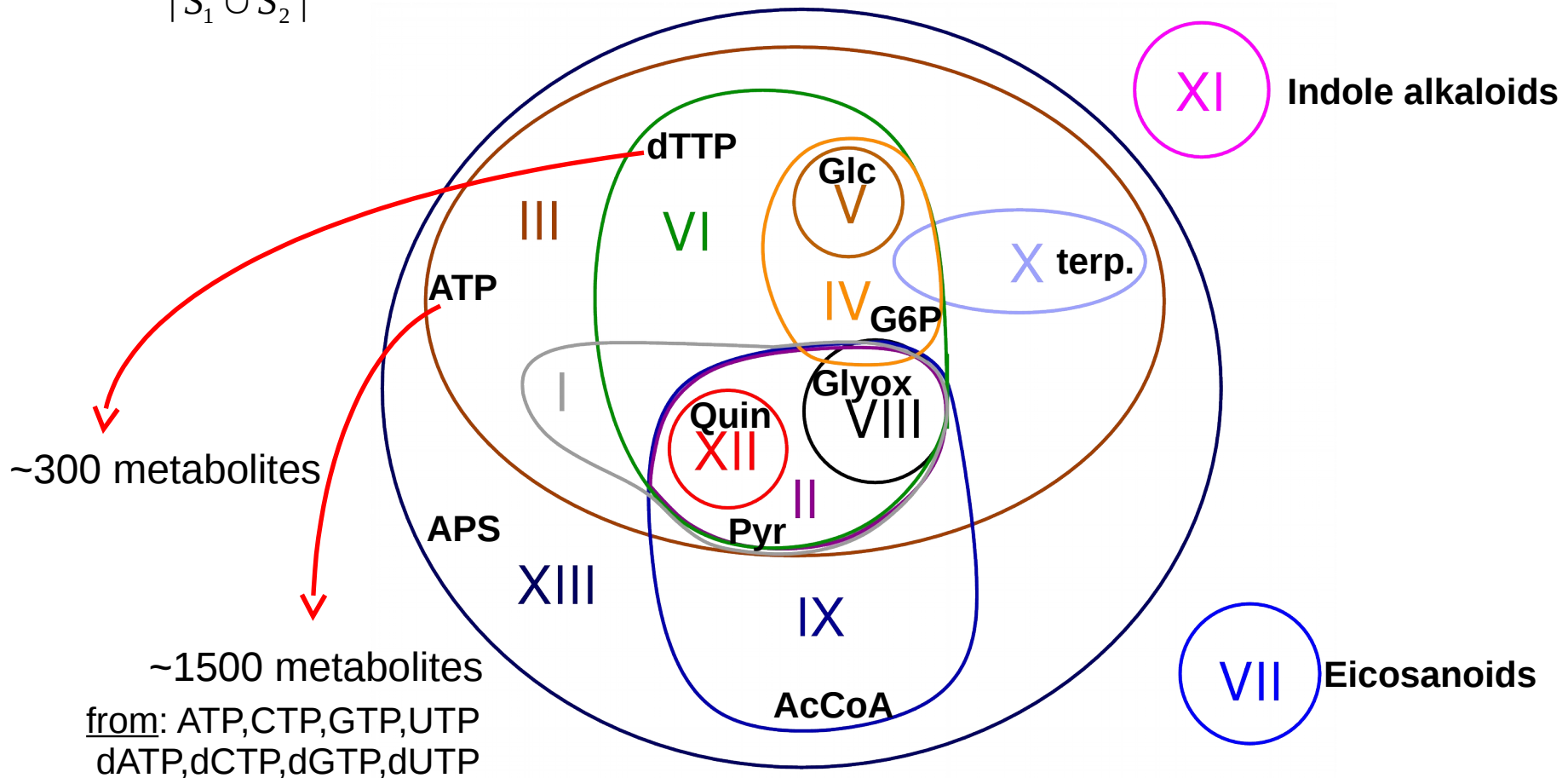


Similarity of biosynthetic potentials

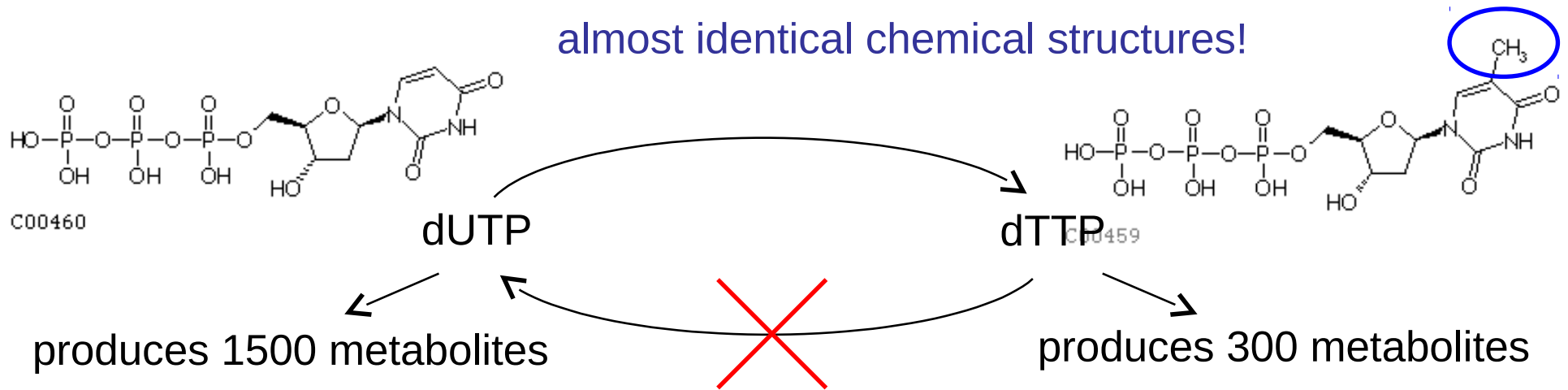
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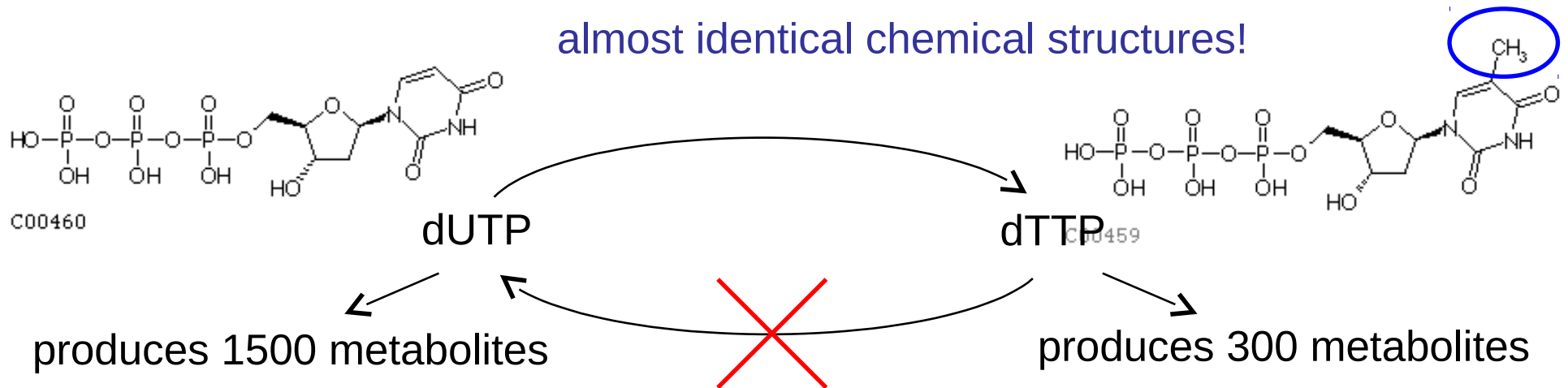
HIERARCHY



Separation of biosynthetic potentials



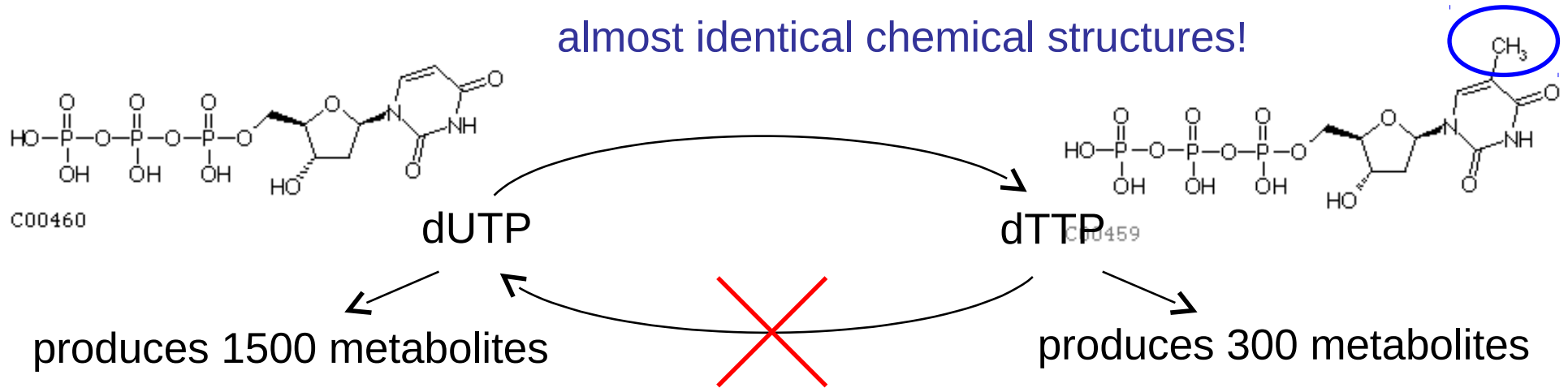
Separation of biosynthetic potentials



in agreement with experiments (growth of *Physarum Polycephalum* with ^{14}C nucleosides)

Fink & Nygaard (1978), *Eur. J. Biochem*

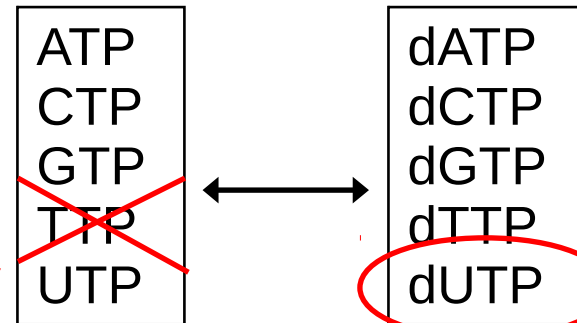
Separation of biosynthetic potentials



in agreement with experiments (growth of *Physarum Polycephalum* with ^{14}C nucleosides)

Fink & Nygaard (1978), Eur. J. Biochem

Explanation



does not exist!

should be low!

The chemical complexity alone does not determine the biosynthetic potential!

RNA

DNA

Single Organisms

Producibility in the flux language

What are the *biosynthetic capabilities* of a network?

Let U denote the set of available nutrient metabolites.

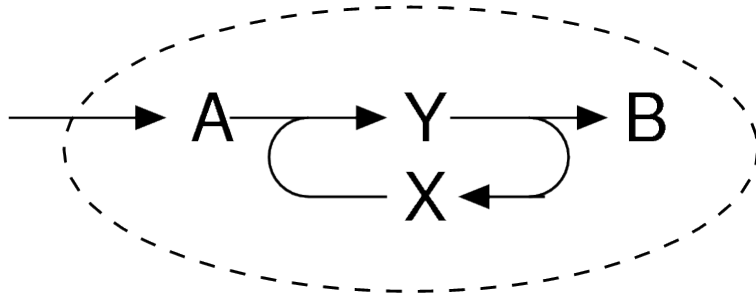
A metabolite is *producible* from the nutrients U if there exists a flux solution such that

- its own concentration increases
- only nutrients are consumed
- all others are at least balanced

Metabolite k is producible if $\exists v: [Sv]_k > 0 \wedge [Sv]_i \geq 0 \quad \forall i \notin U$

Let $P(U)$ denote the set of all metabolites producible from nutrients U

Growth and Dilution: Toy models



$$U = \{A\}$$

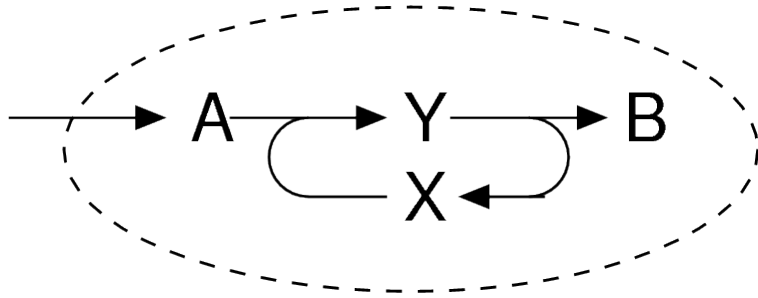
$$P = \{B\}$$

X and Y not producible from A !

What if the cell is growing? \Rightarrow Dilution! $\Rightarrow X, Y \rightarrow 0$

B is not producible under growth!

Growth and Dilution: Toy models



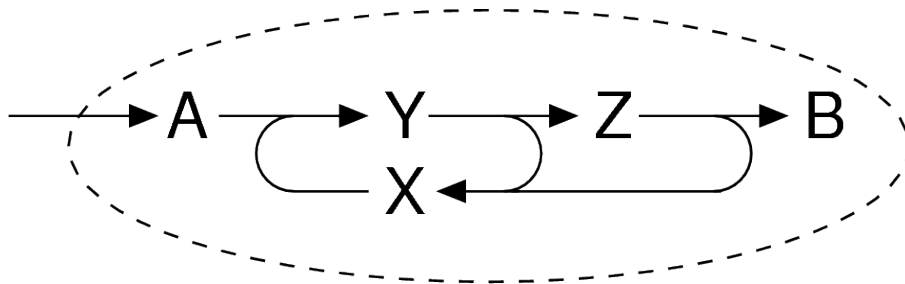
$$U = \{A\}$$

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What if the cell is growing? \Rightarrow Dilution! $\Rightarrow X, Y \rightarrow 0$

B is not producible under growth!



$$U = \{A\}$$

$$P = \{X, Y, Z, B\}$$

B is producible under growth!

Sustainability

A metabolite is **sustainable** from nutrients U if there exists a flux solution such that

- its own concentration increases
- only nutrients are consumed
- **all other required intermediates are sustainable**

Let U denote the set of available nutrient metabolites.

Let $P(U)$ denote the set of all metabolites producible from nutrients U

Recursive definition of sustainable metabolites:

Let $P_0 = P(U)$

Define forbidden set of reactions: $F_n = \{j \mid \exists i \notin P_n : S_{ij} < 0\}$

$P_{n+1} = \{k \mid \exists v : v_j = 0 \ \forall j \in F_n \wedge [Sv]_k > 0 \wedge [Sv]_i \geq 0 \ \forall i \notin U\}$

Let $S(U)$ denote the set of all metabolites sustainable from U , defined by

$$S(U) = \lim_{n \rightarrow \infty} P_n$$

Takes a long time to compute!

Relating scopes to flux models

Let $\Sigma(U)$ denote the scope of U

It can simply be shown that $\Sigma(U) \subseteq S(U) \subseteq P(U)$

Numerical experiment for the network of *E.coli* (Reed et al., 2003)

determine $\Sigma(U)$ and $S(U)$

for all sets $U = \{k, H_2O\}$

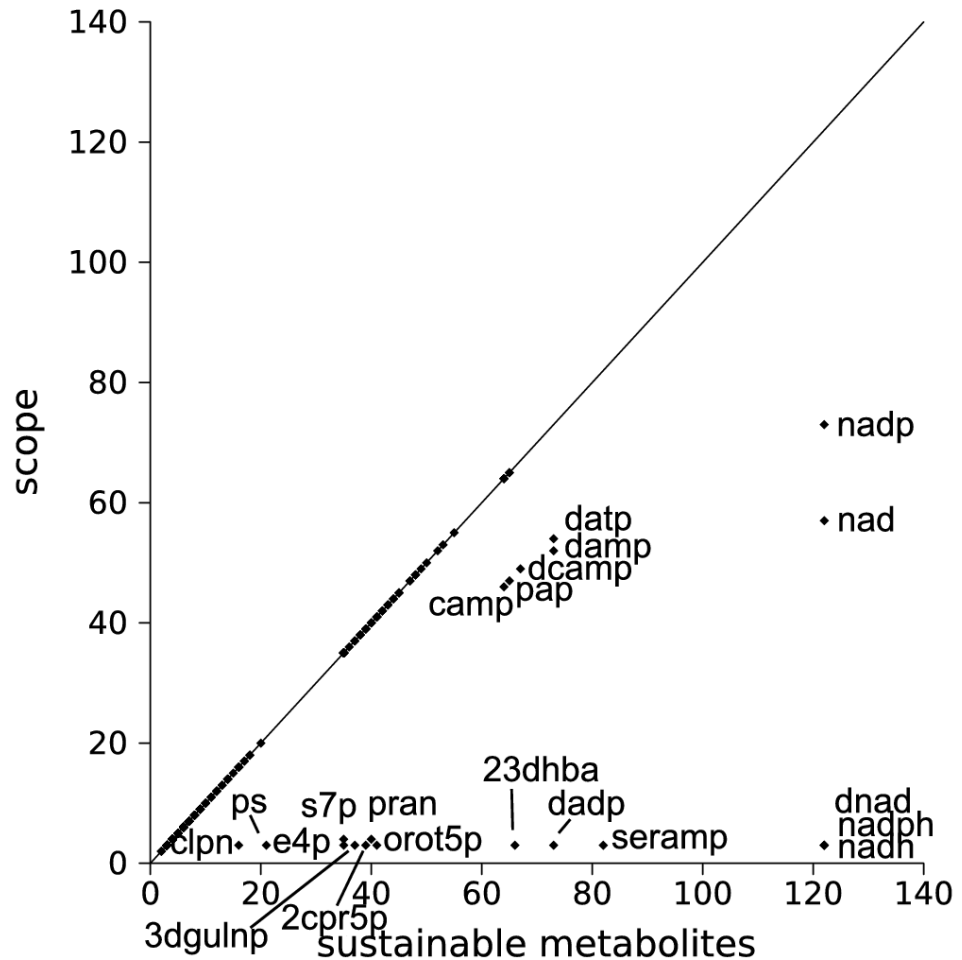
Observation:

for most metabolites:

$$\Sigma(U) = S(U)$$

→ Agreement even better for more complex sets U

(Kruse and Ebenhöf, GI 2008)



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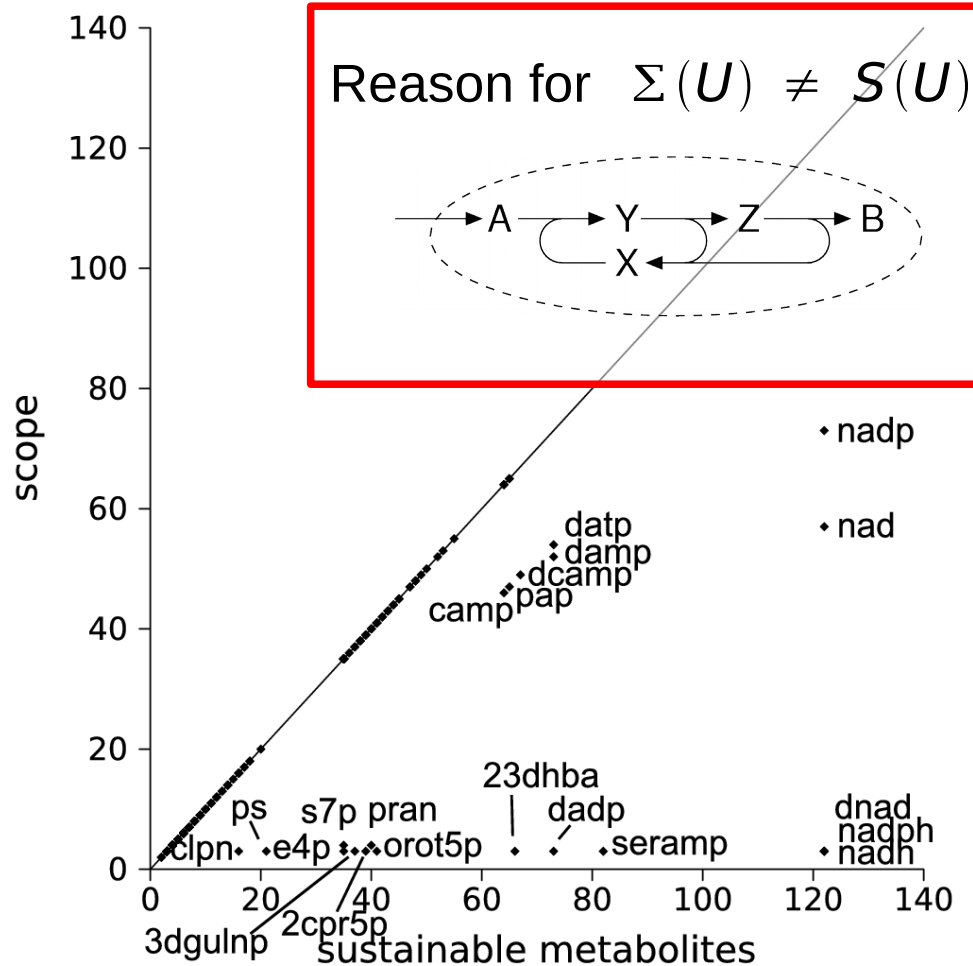
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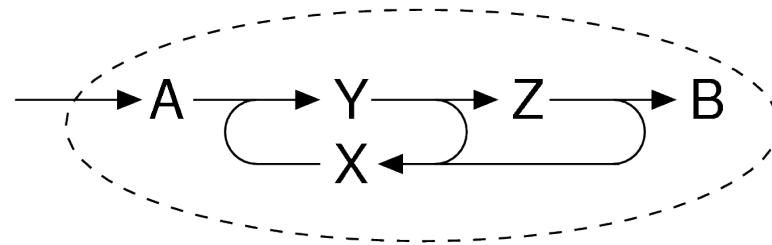
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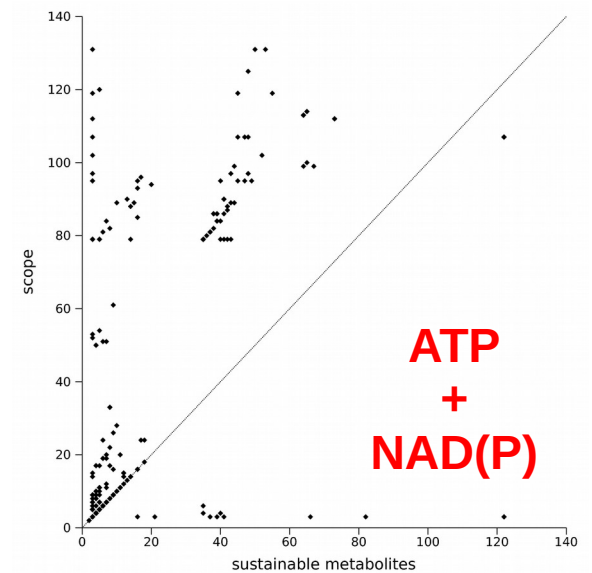
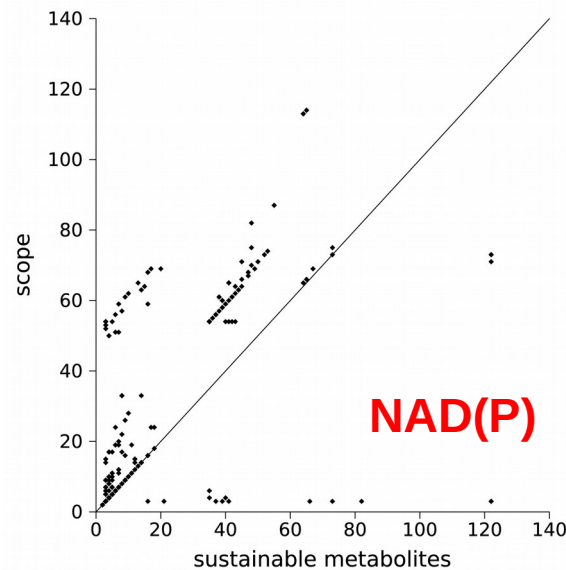
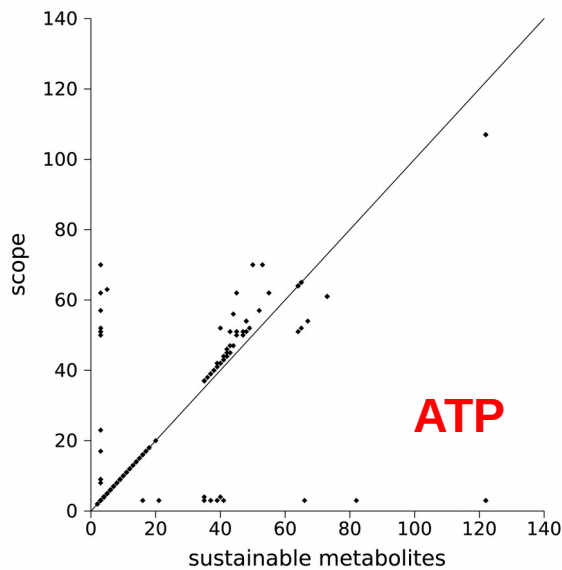


The role of cofactors

Common cofactors (ATP/NADH) are of the type



We add cofactors to the seed
(ATP does not have to be produced to be used as a cofactor)



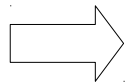
We tend to overestimate the 'true' biosynthetic capacity (under constant growth)

But that's OK to give a meaning to “The scope of glucose”

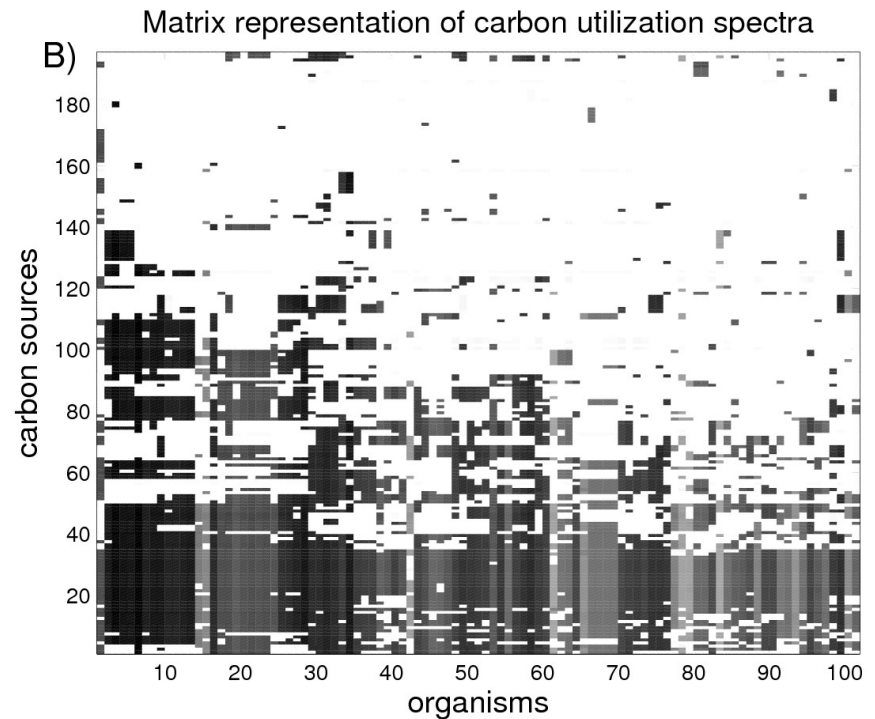
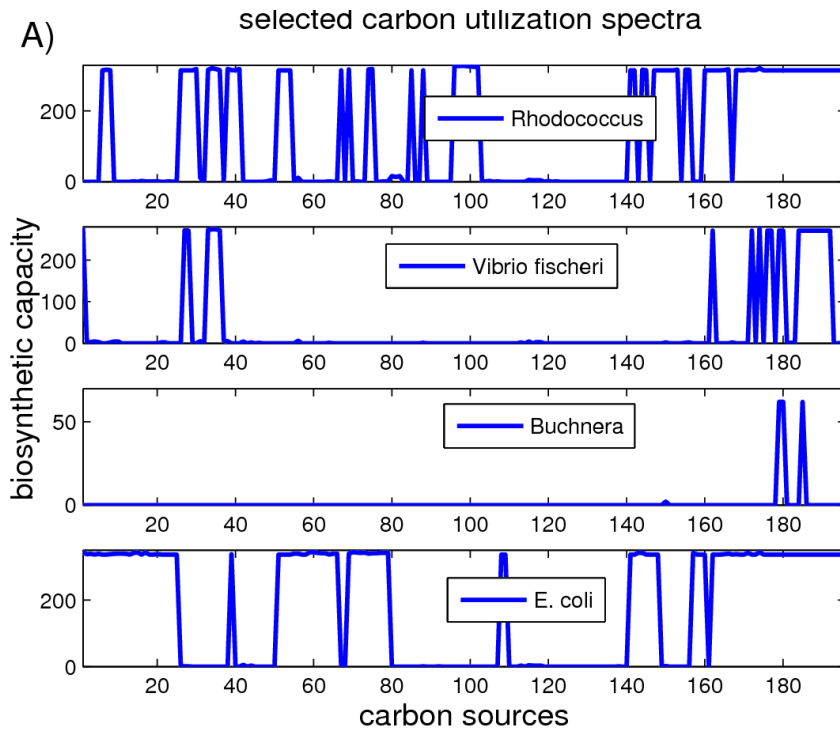
Single organisms

Investigate biosynthetic capacities of organisms on various carbon sources:

- 447 organism specific networks (KEGG)
- 200 carbon sources



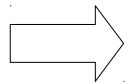
CARBON UTILIZATION SPECTRA



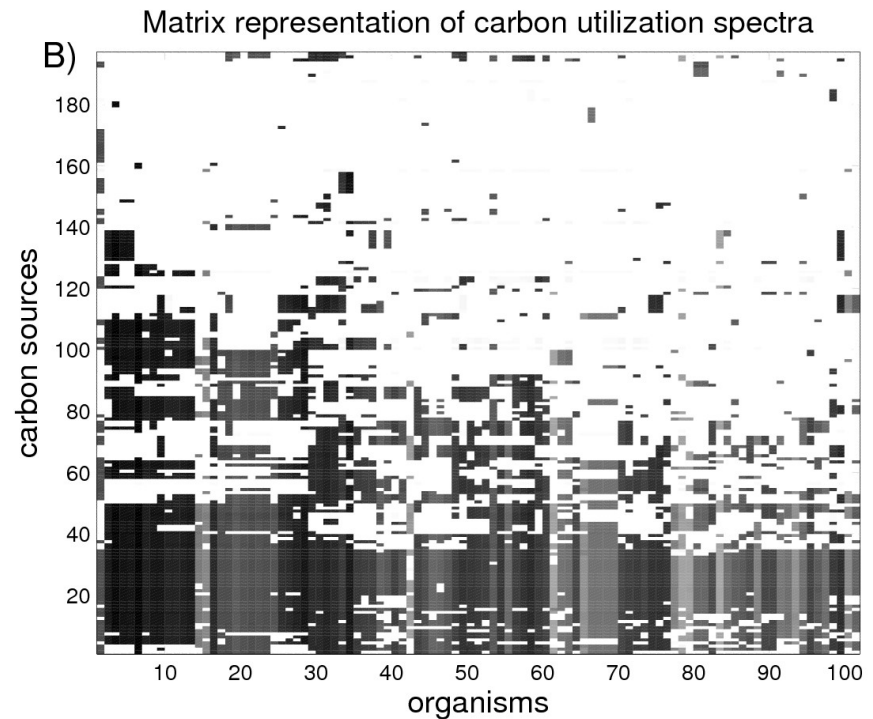
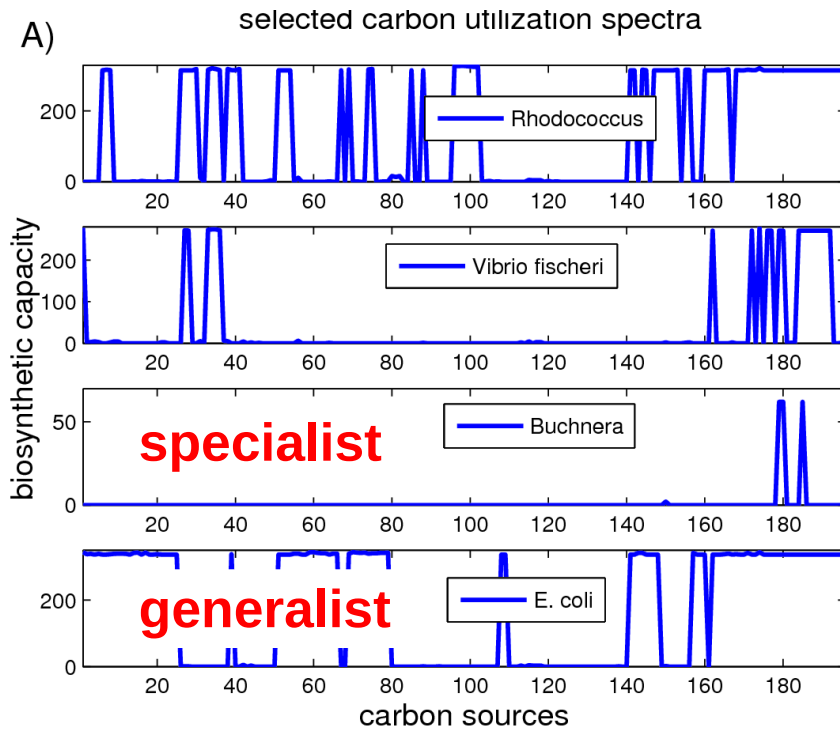
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CARBON UTILIZATION SPECTRA

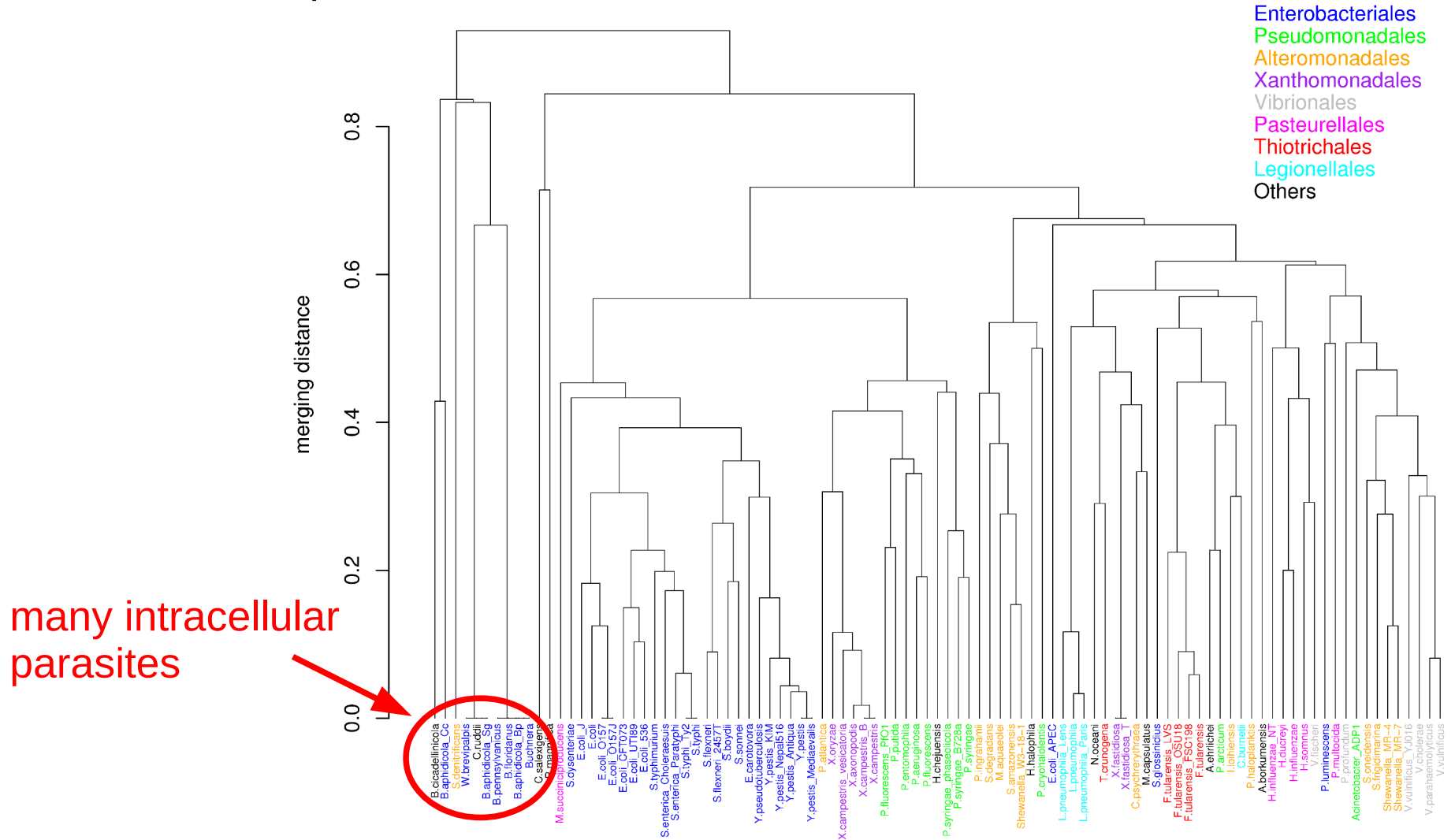


It is in principle possible to distinguish between generalists and specialists

Single organisms

A phenetic tree based on carbon utilization spectra

Organisms clustered by carbon utilization spectra



many intracellular parasites

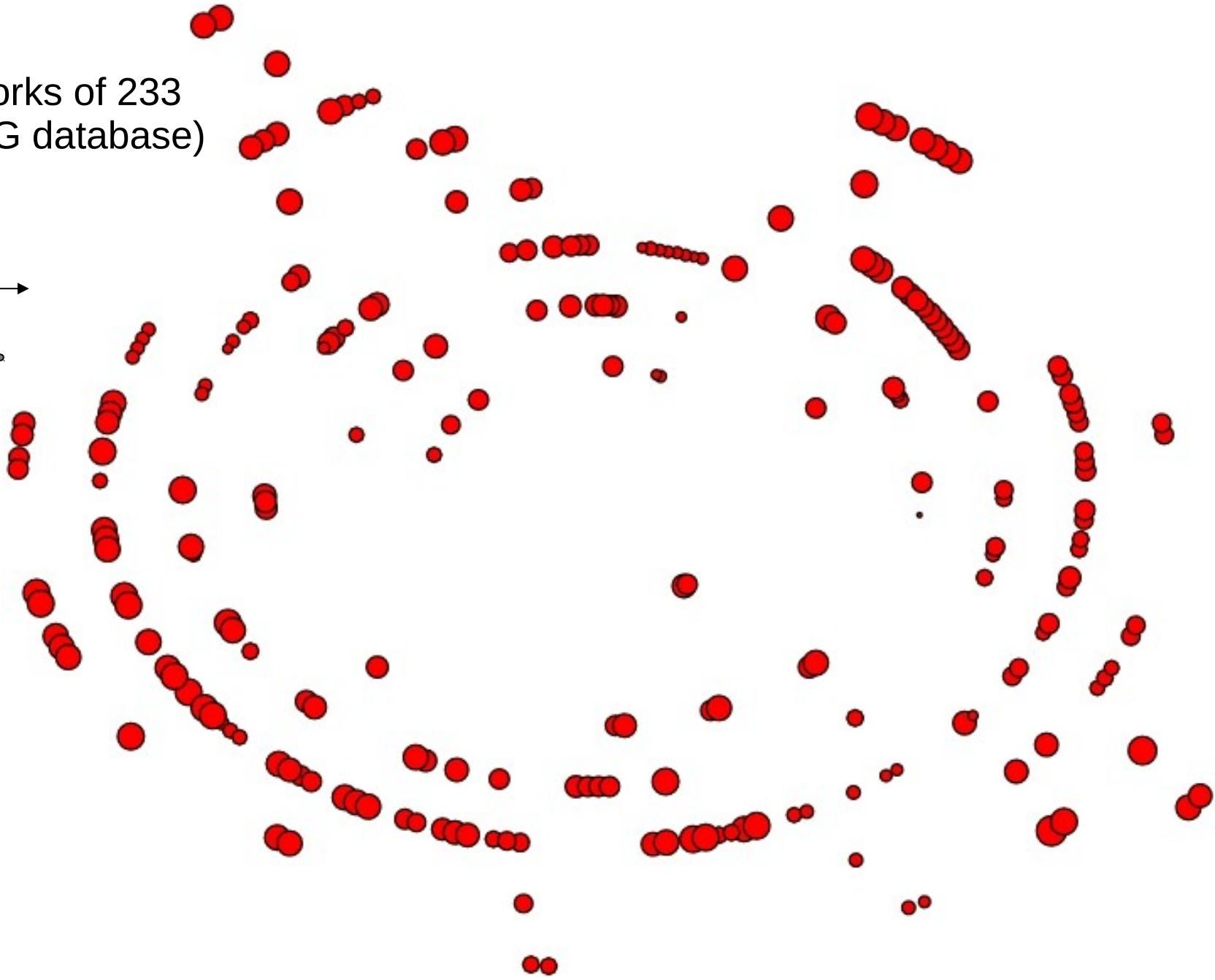
⇒ Classification of organisms by 'lifestyle'?

(Ebenhöh and Handorf, EURASIP, 2009)

Single organisms

Metabolic networks of 233 organisms (KEGG database)

	organisms			
reactions	1	0	1	0
	0	1	1	0
	1	1	1	0
	1	1	0	1
	⋮			

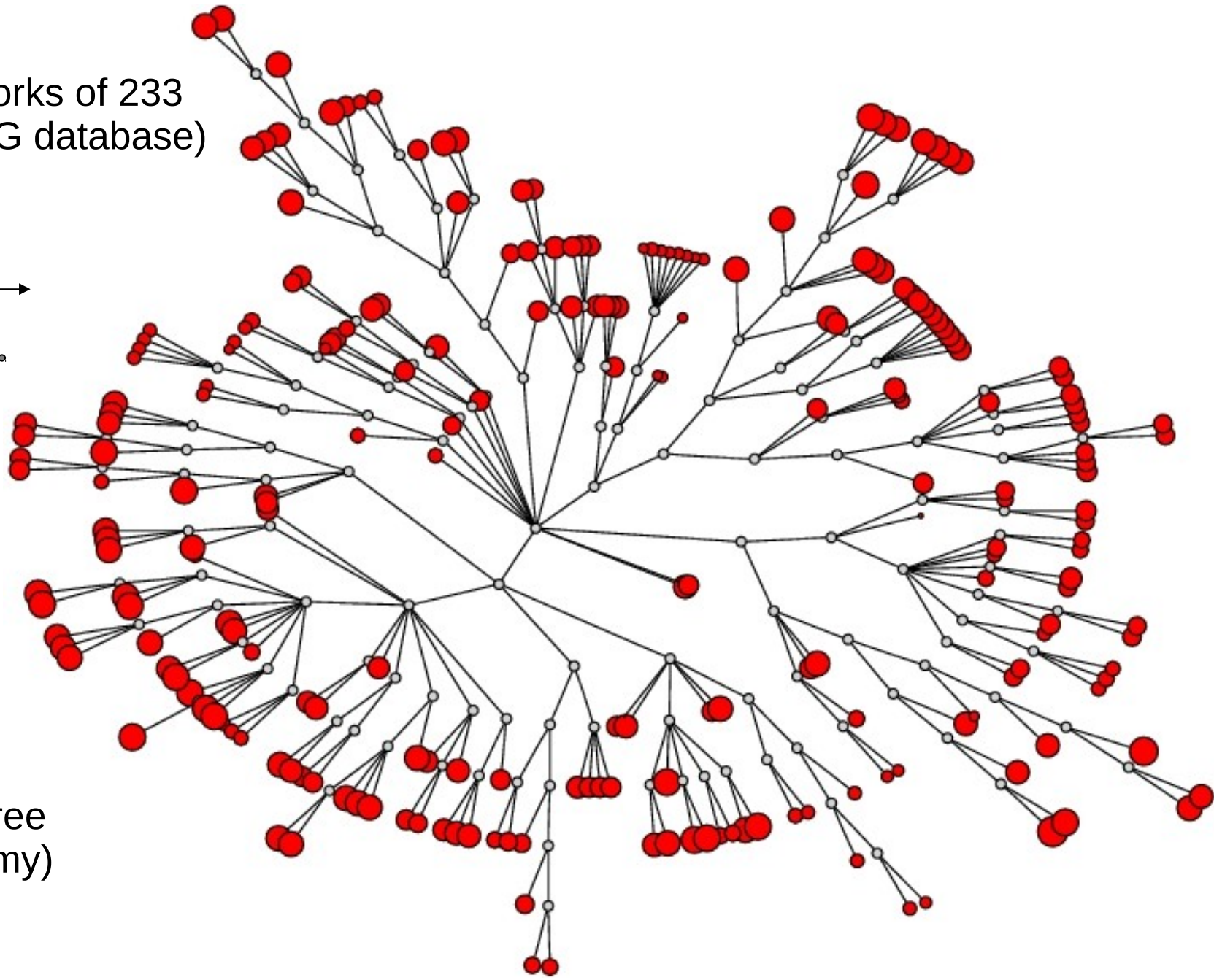


Single organisms

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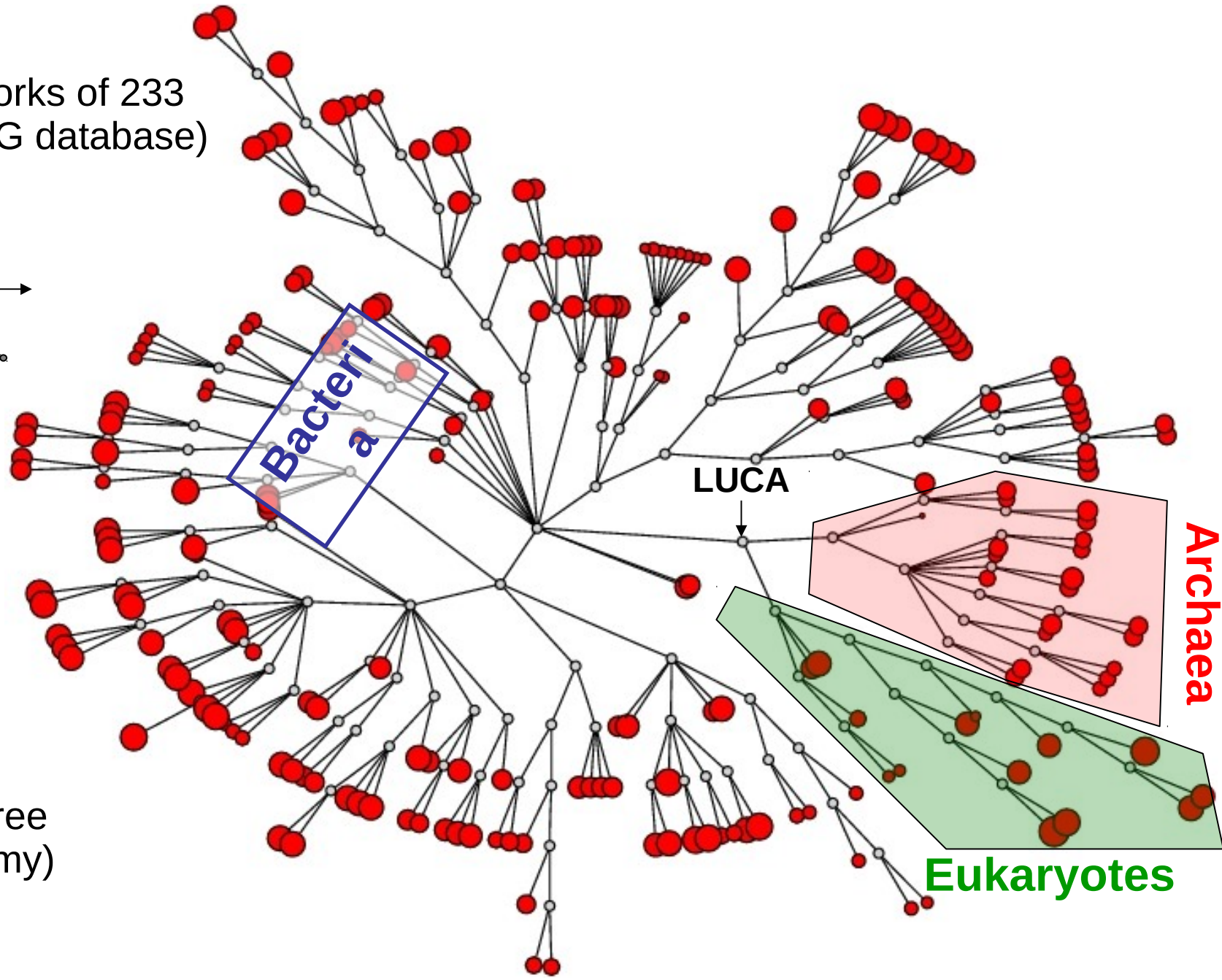
Evolutionary tree
(NCBI Taxonomy)



The tree of life

Metabolic networks of 233 organisms (KEGG database)

	organisms			
reactions	1	0	1	0
	0	1	1	0
	1	1	1	0
	1	1	0	1
	⋮	⋮	⋮	⋮

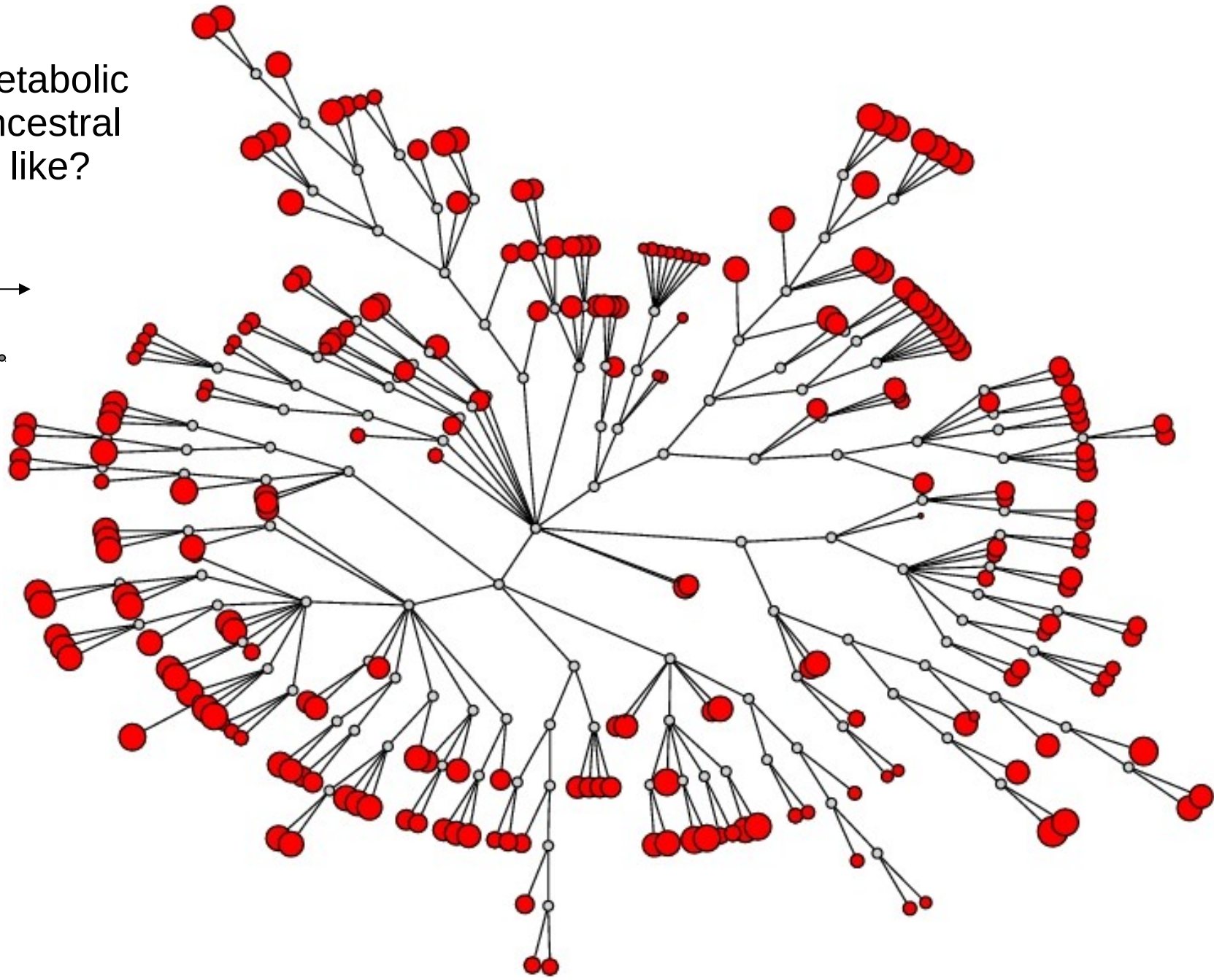


Evolutionary tree
(NCBI Taxonomy)

Ancestral networks

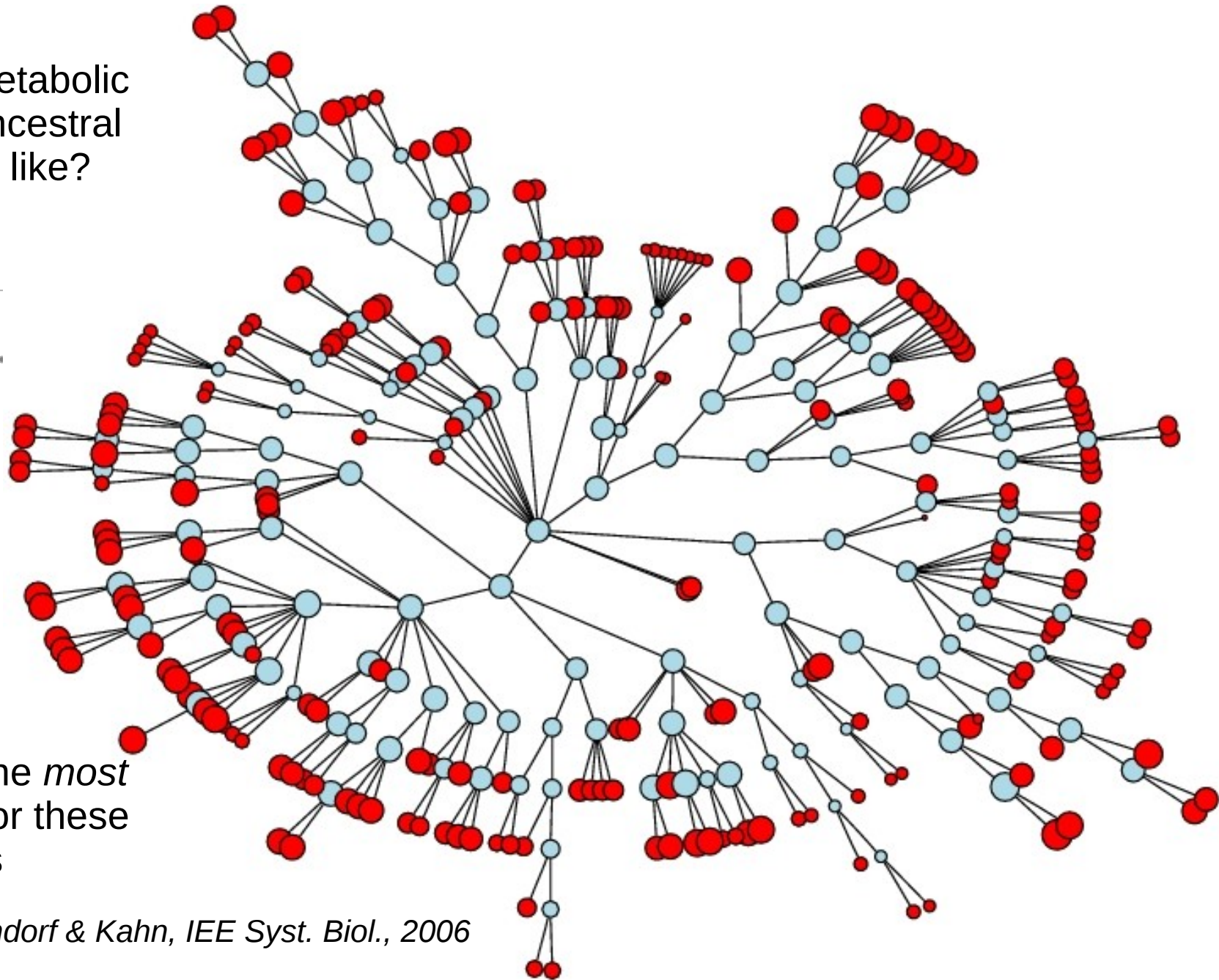
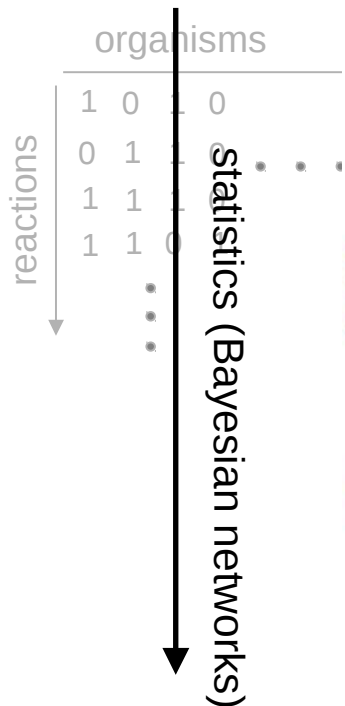
How did the metabolic networks of ancestral species look like?

	organisms			
reactions	1	0	1	0
	0	1	1	0
	1	1	1	0
	1	1	0	1
	⋮			



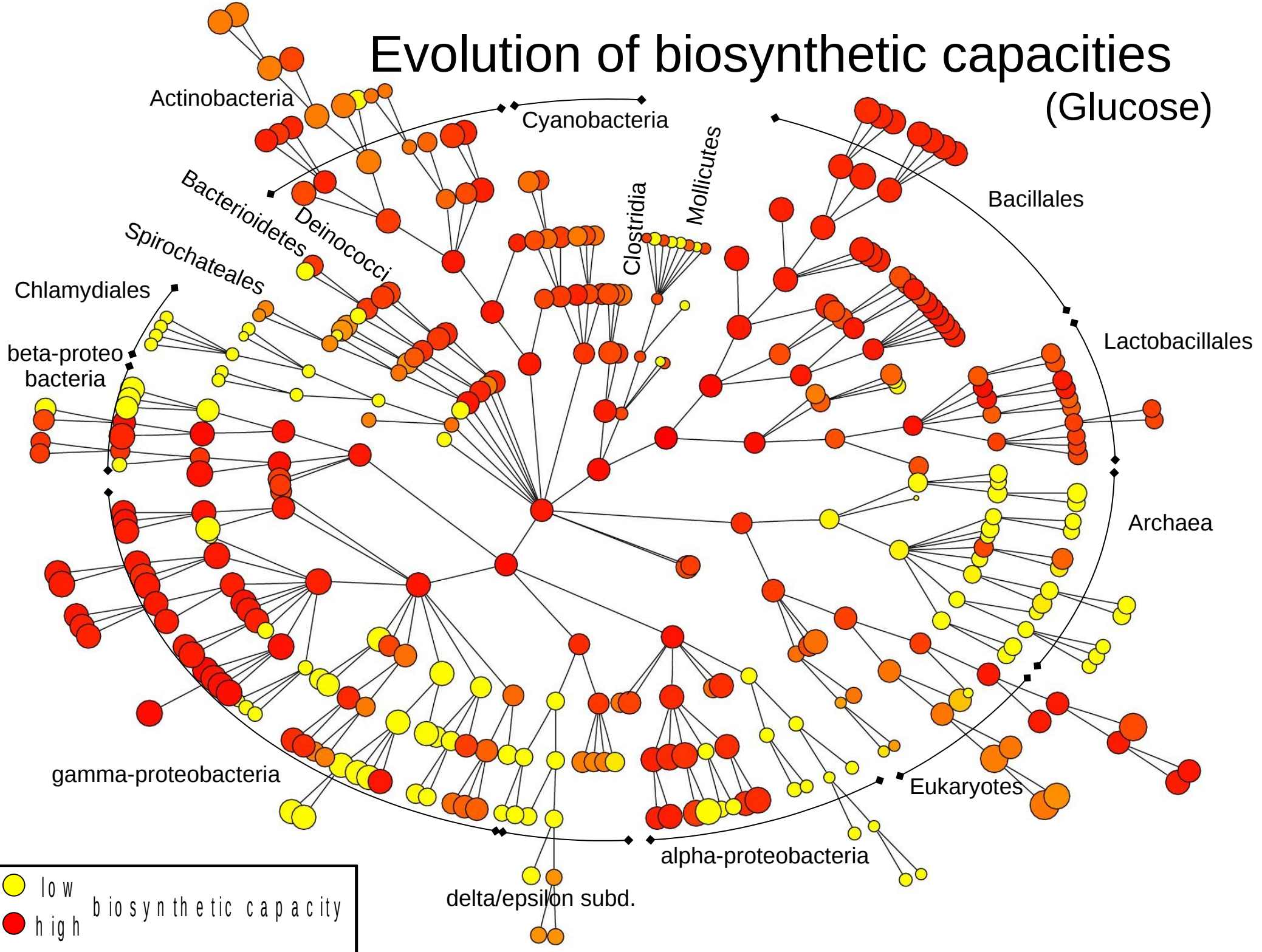
Reconstruction of ancestral networks

How did the metabolic networks of ancestral species look like?



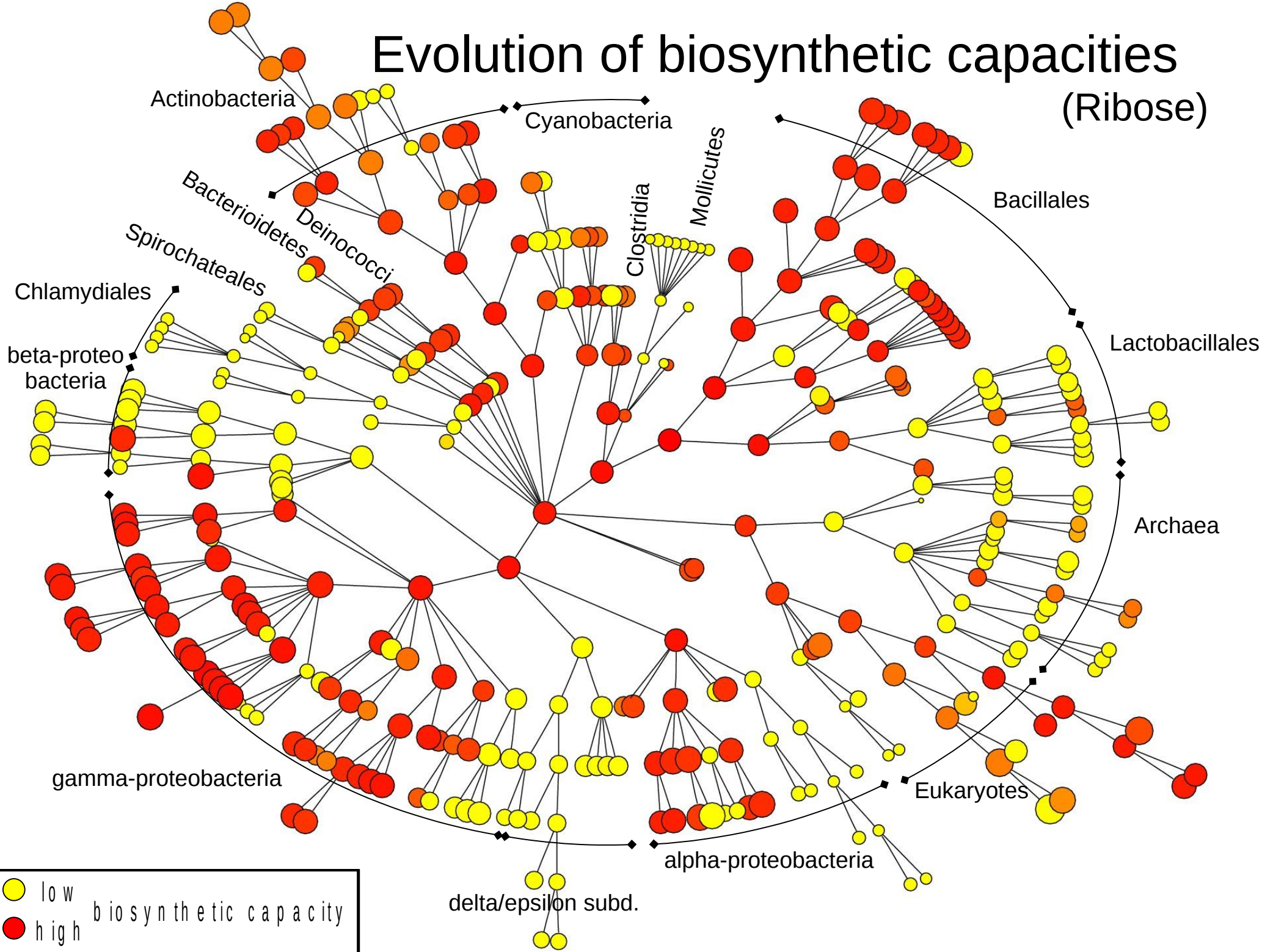
We calculated the *most likely scenario* for these networks

Evolution of biosynthetic capacities (Glucose)



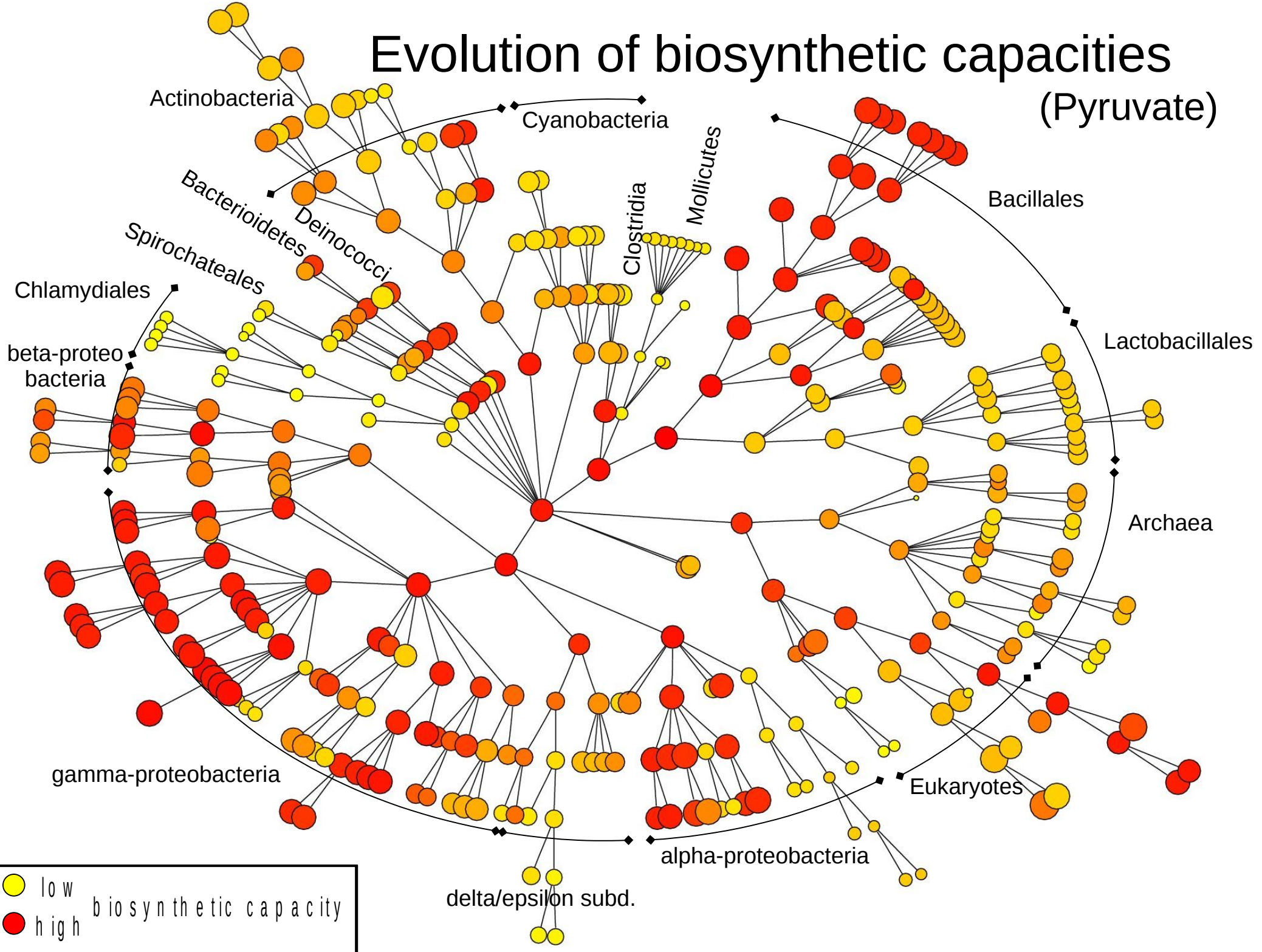
● low
● high
biosynthetic capacity

Evolution of biosynthetic capacities (Ribose)



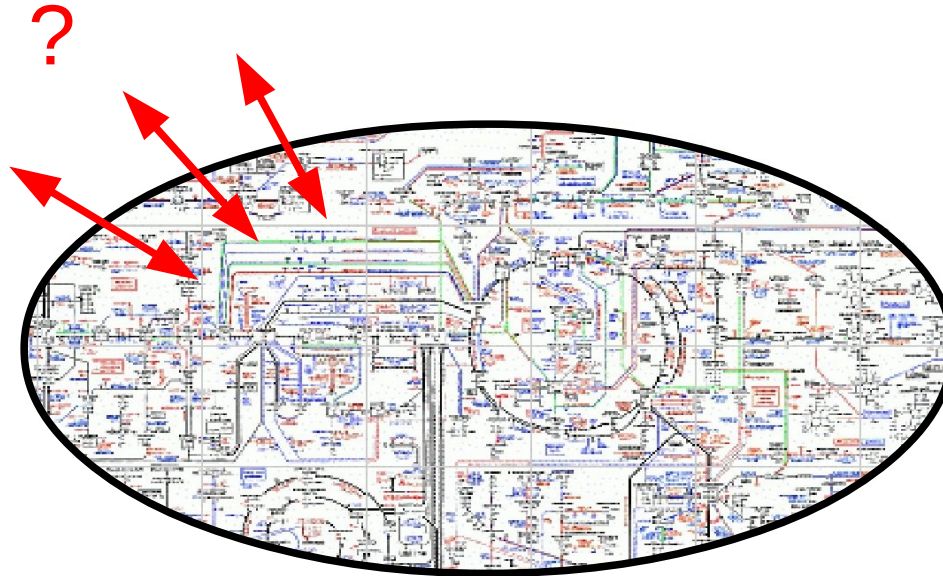
● low biosynthetic capacity
● high

Evolution of biosynthetic capacities (Pyruvate)



The inverse problem

Networks are relatively easy to obtain (e.g. from KEGG)

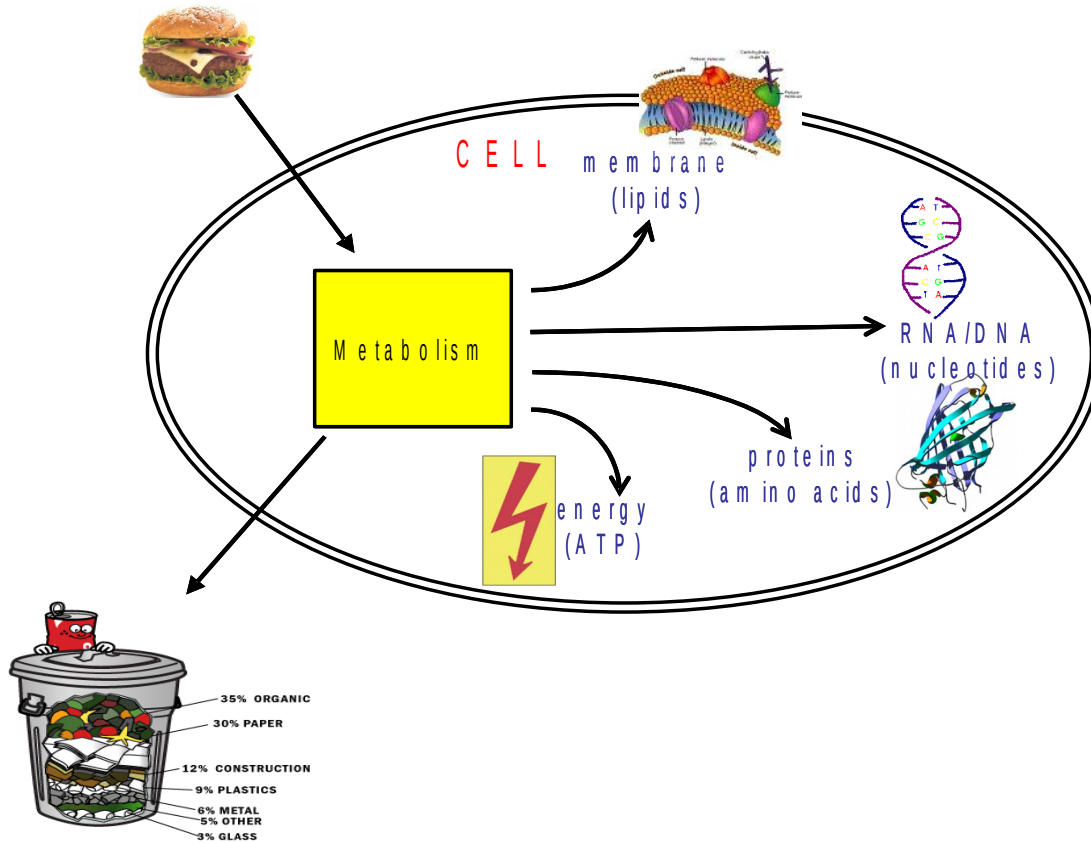


... but information of transport processes across the cellular membrane is often poorly characterized!

CAN WE PREDICT NUTRIENT MEDIA FROM THE NETWORK STRUCTURE?

Inferring nutrient requirements

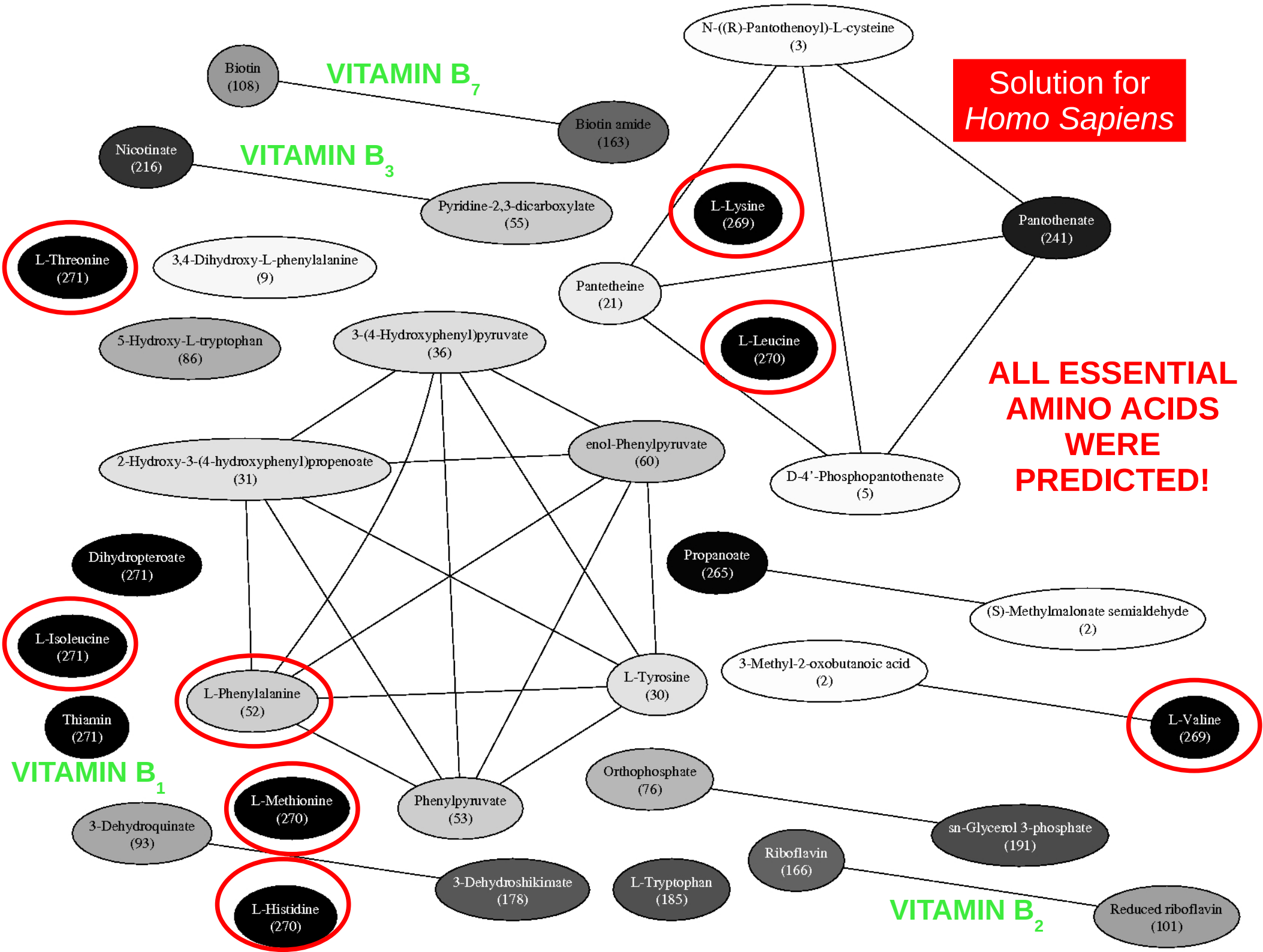
Biological knowledge

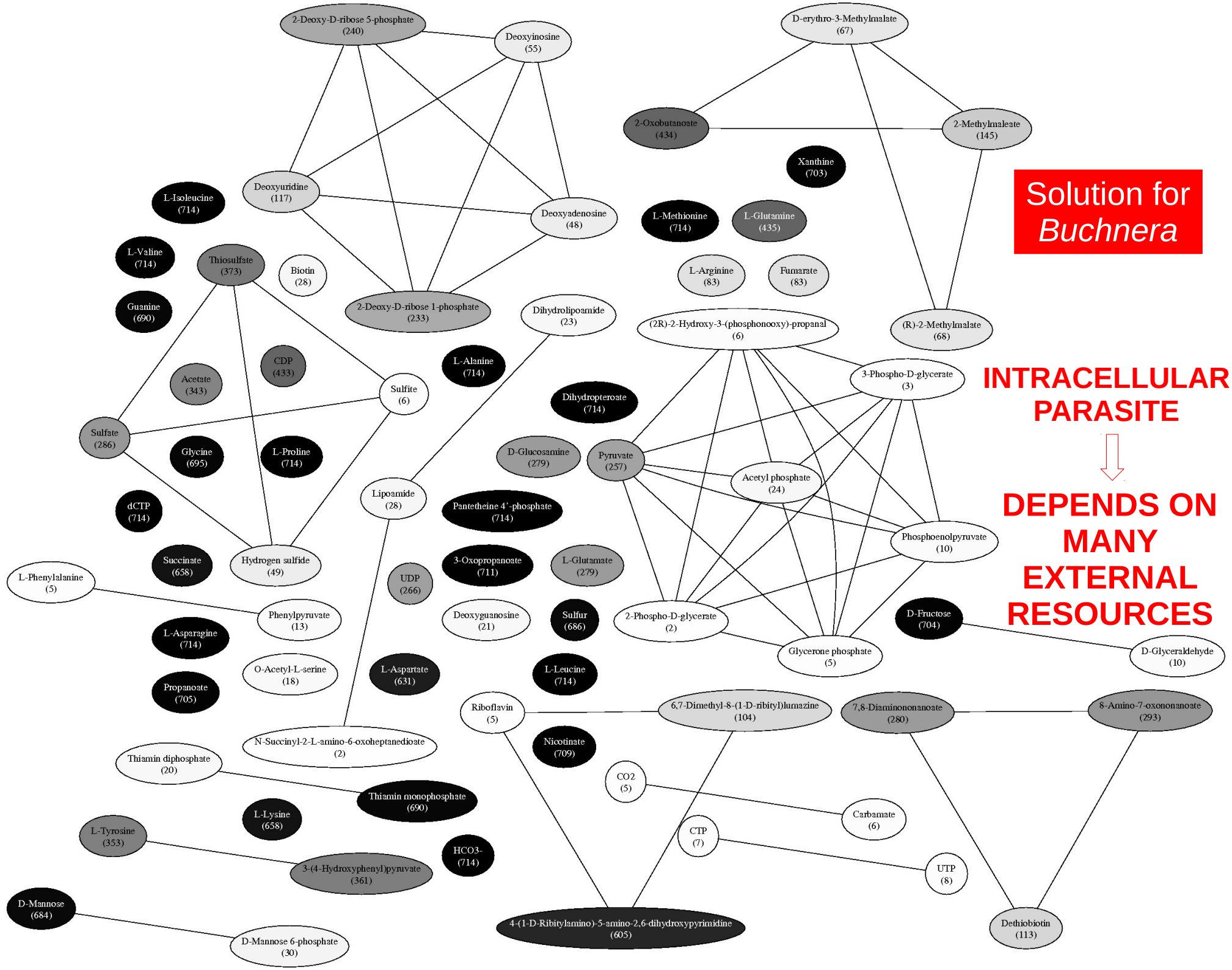


Mathematics

Every network must be able to produce precursors:

- amino acids
- nucleotides
- lipids
- energy
- etc...

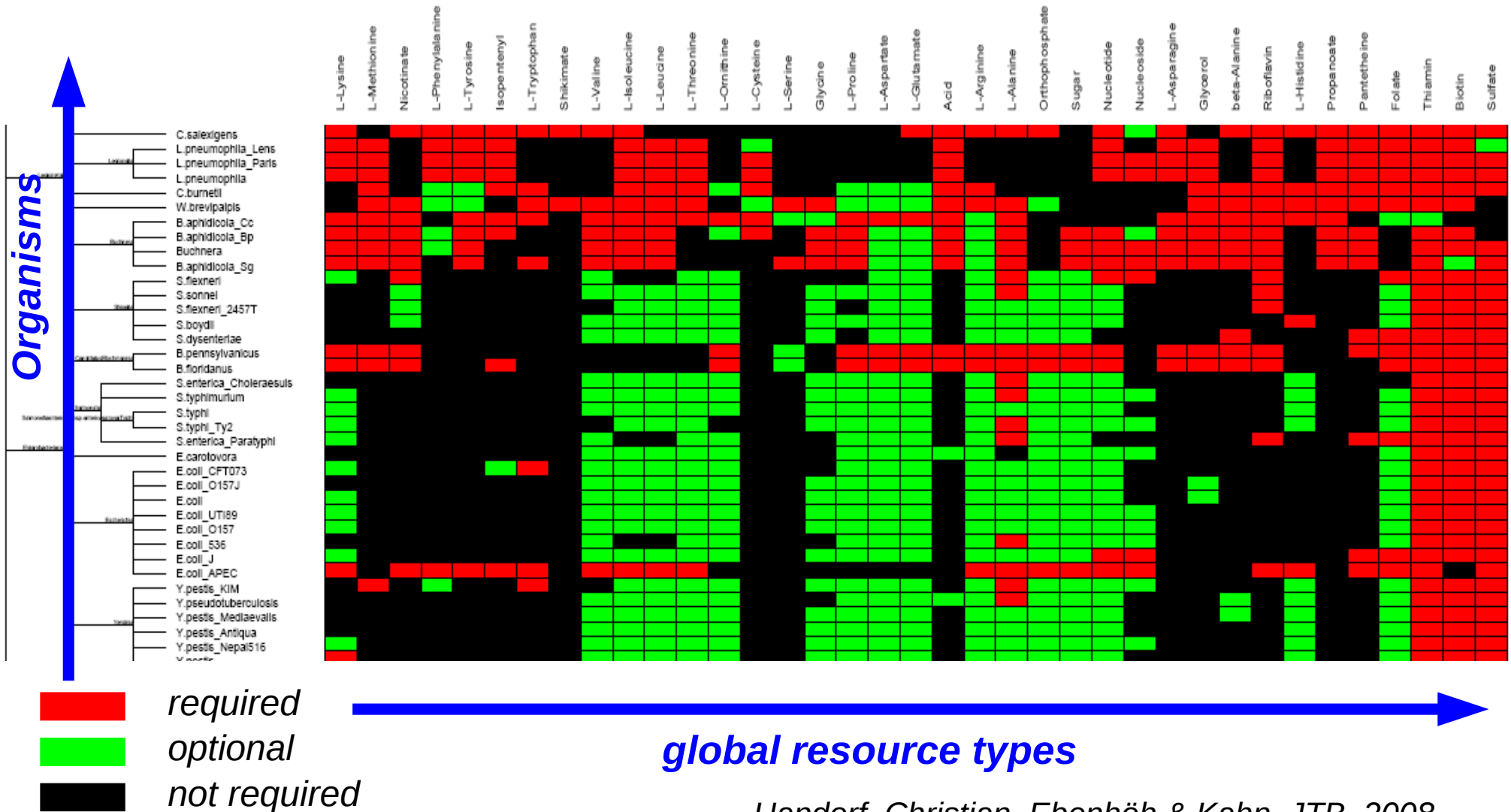




Global resource types

The comparison of the results for 400 organisms allows to define

36 global resource types



CELLULAR METABOLISM

KEGG contains over 400 organism specific networks

How are these networks constructed?

sequenced genome

BLAST genes against all metabolic genes in other organisms

sequence similarity above threshold?

no

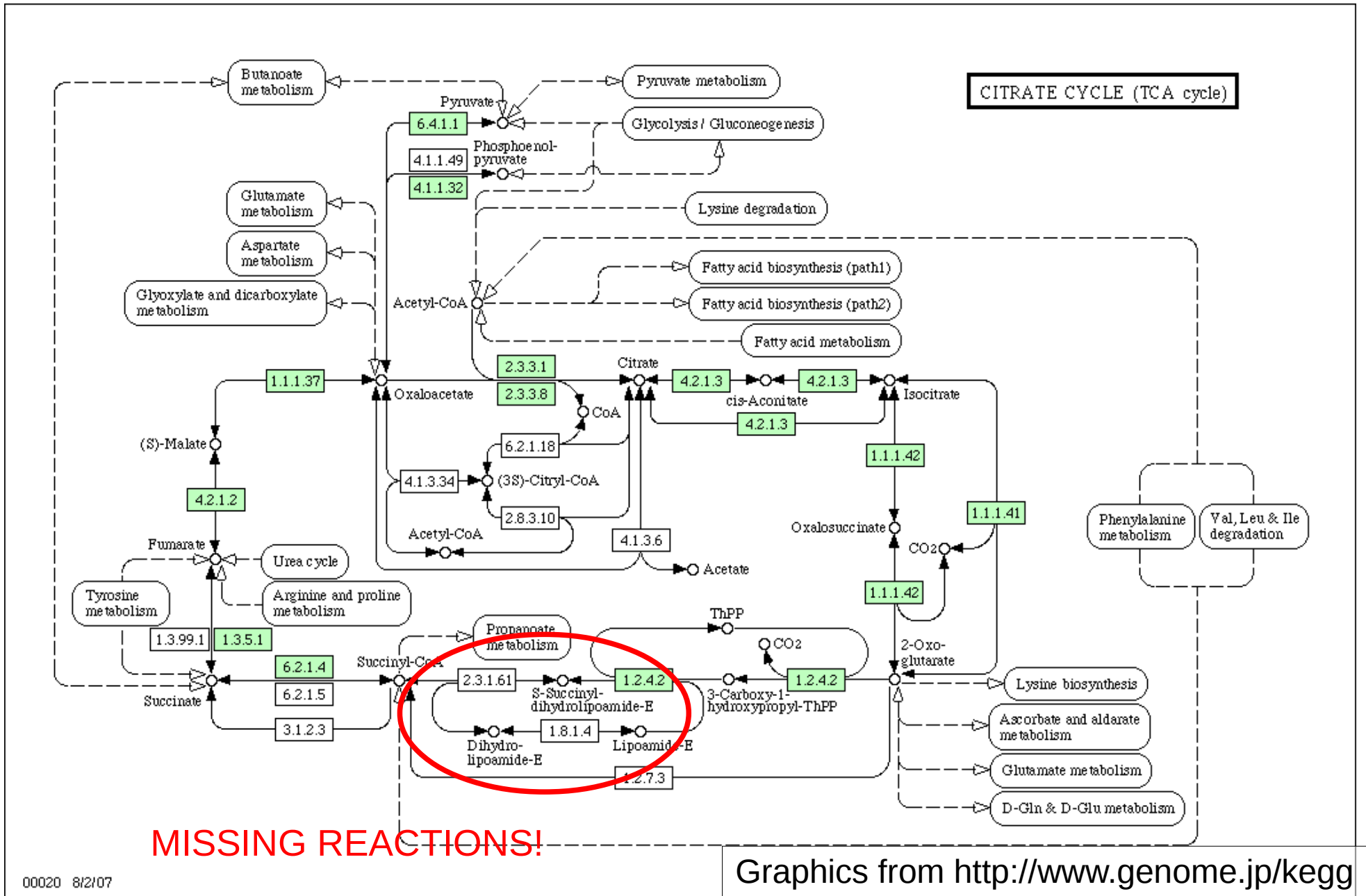
ignore

yes

assign gene the same metabolic function

AUTOMATED PROCESS: ERROR-PRONE

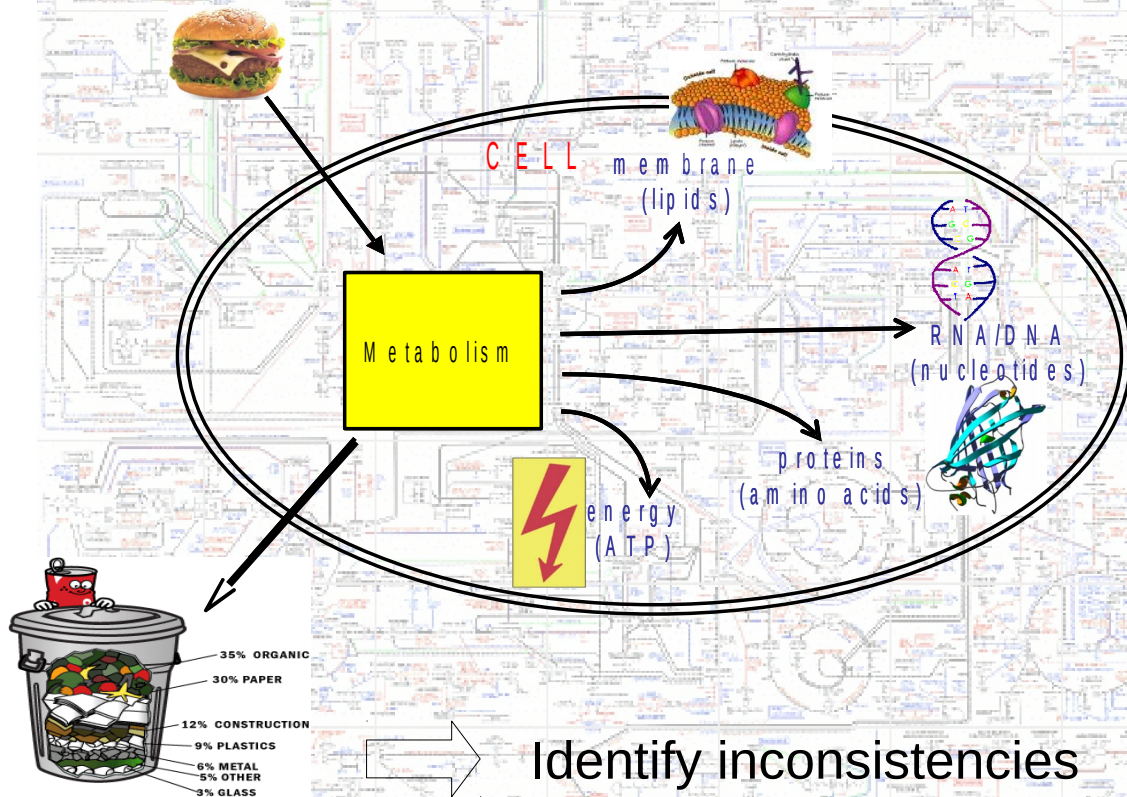
Closing gaps in metabolism



Combining expert knowledge with mathematics

Expert knowledge

Mathematics



Plausibility check:

Test whether the network can produce from experimentally verified growth media

- amino acids
- nucleotides
- lipids
- energy
- **other experimentally observed metabolites**

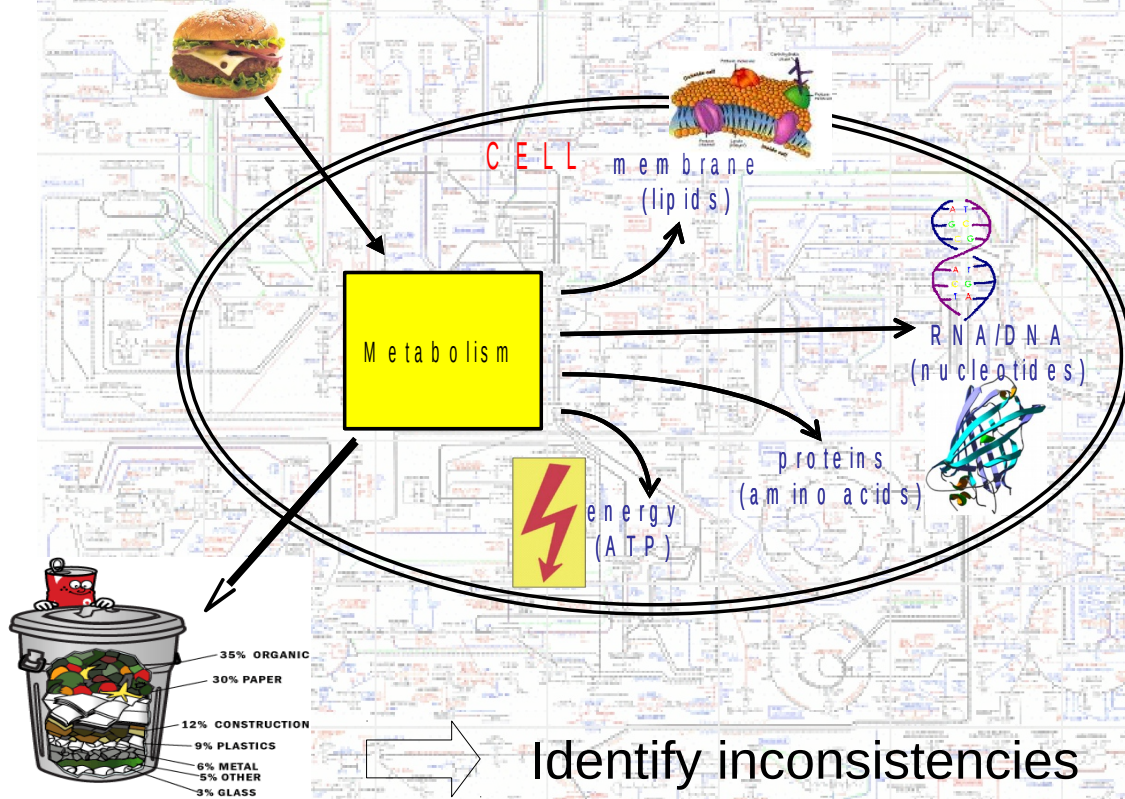
Identify inconsistencies

method: network expansion (Handorf et. al, 2005)

Combining expert knowledge with mathematics

Expert knowledge

Mathematics



Plausibility check:

Test whether the network can produce from experimentally verified growth media

- amino acids
- nucleotides
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- energy
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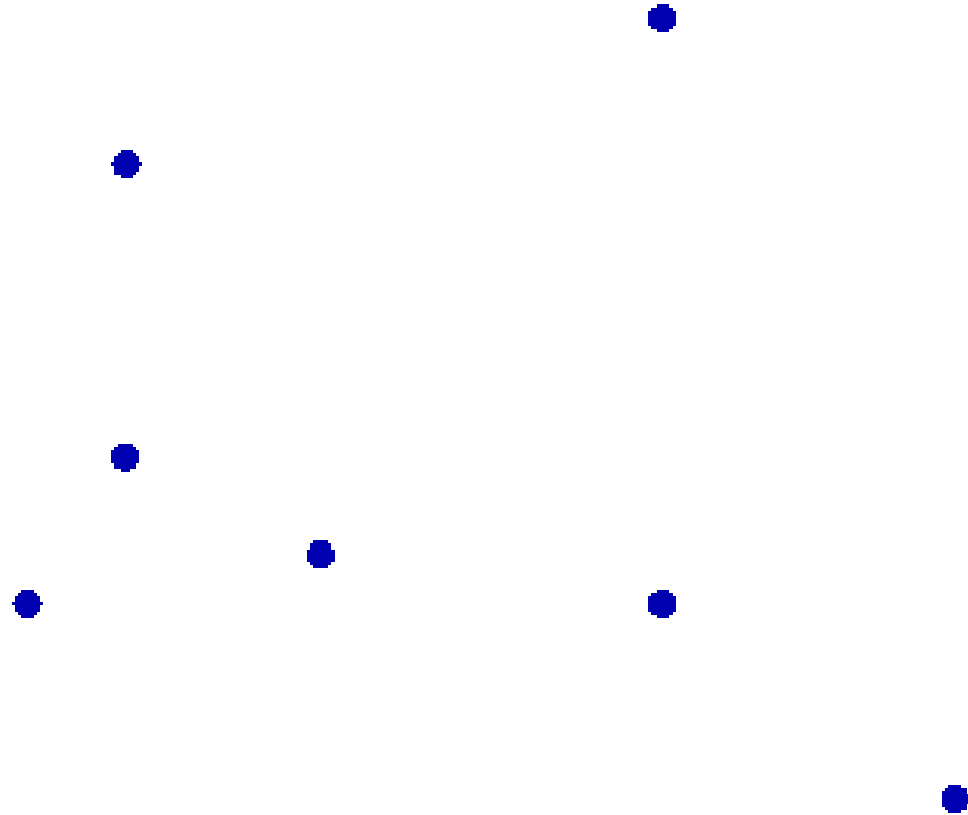
Identify inconsistencies

method: network expansion (Handorf et. al, 2005)

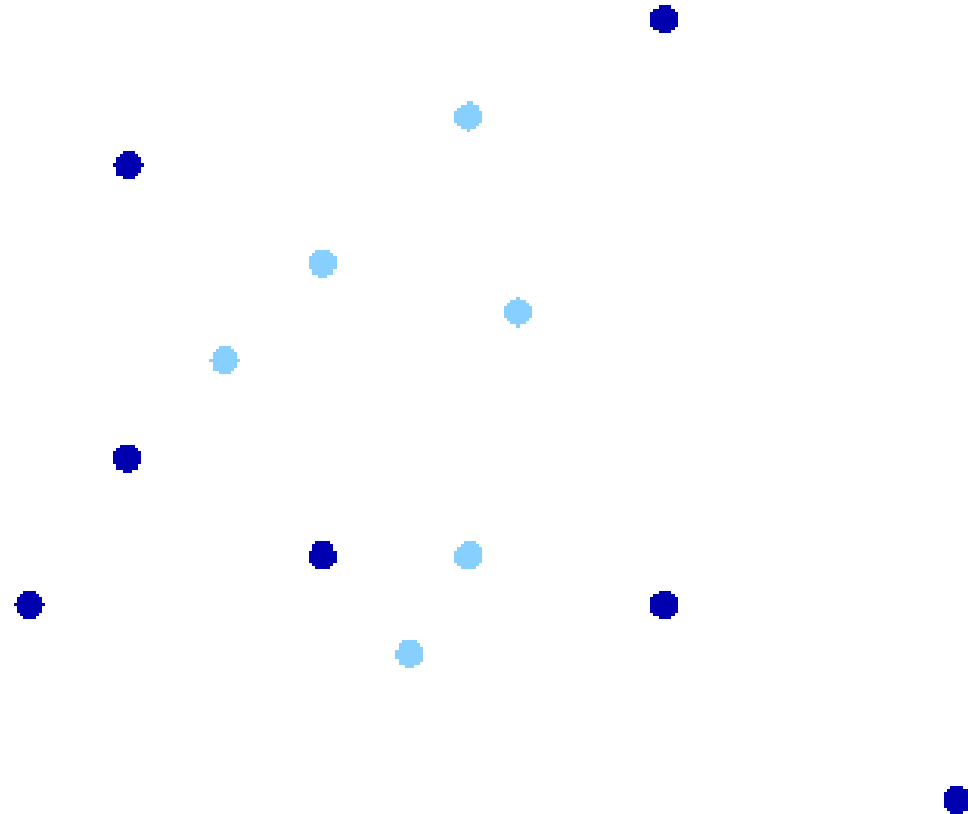
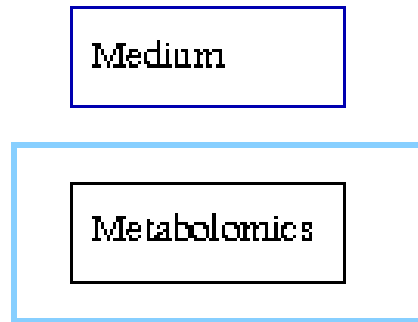
Fix networks

Filling the gaps

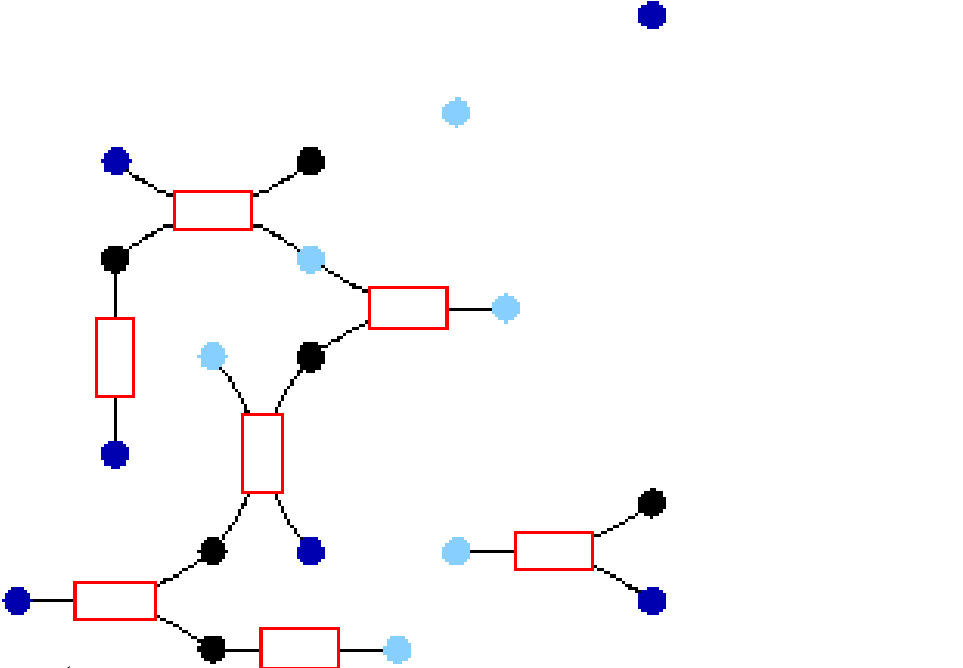
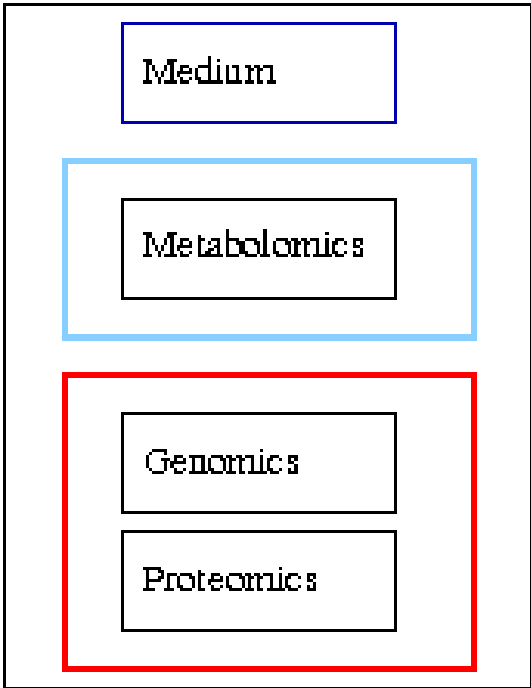
Medium



Filling the gaps

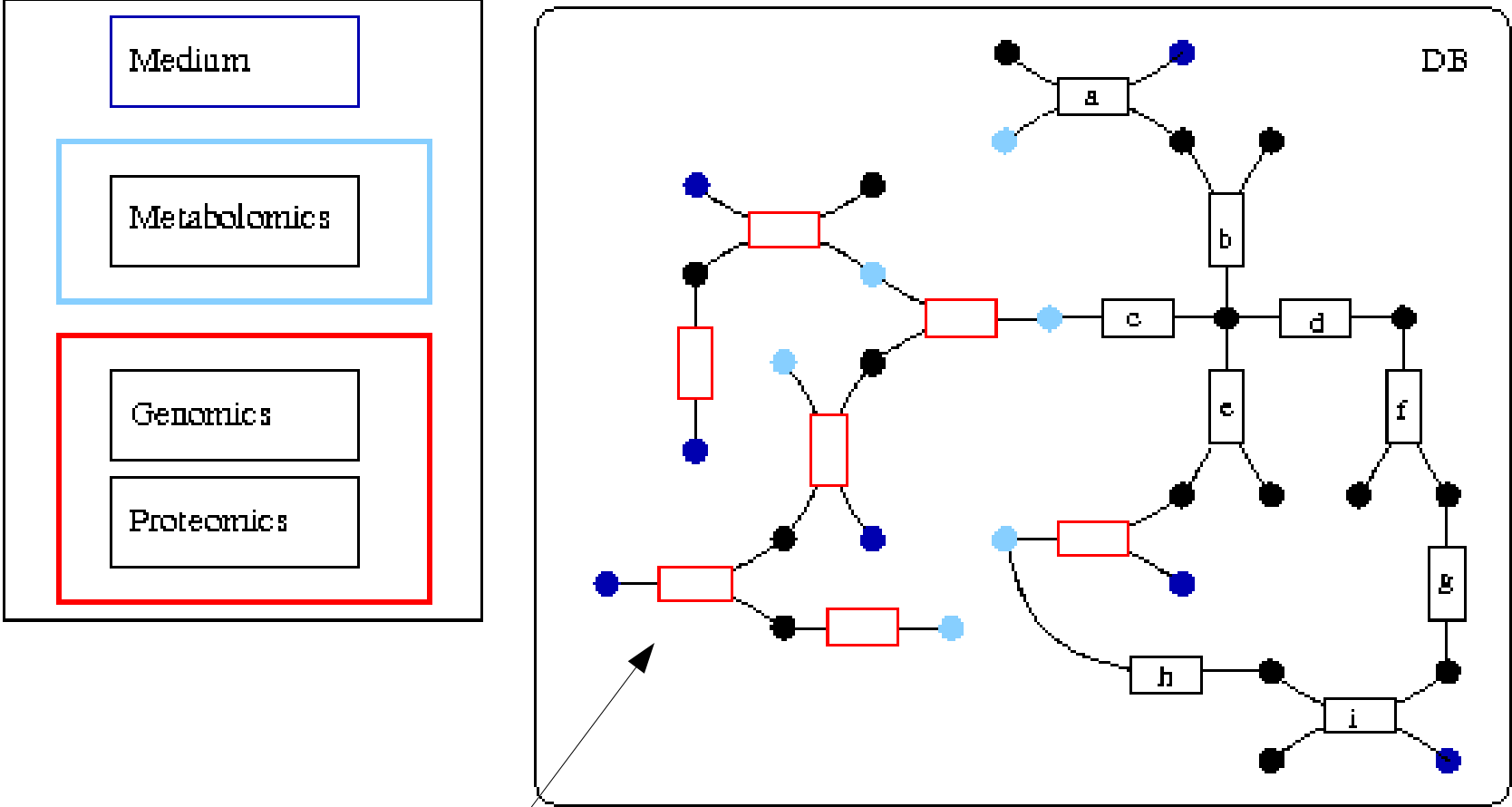


Filling the gaps



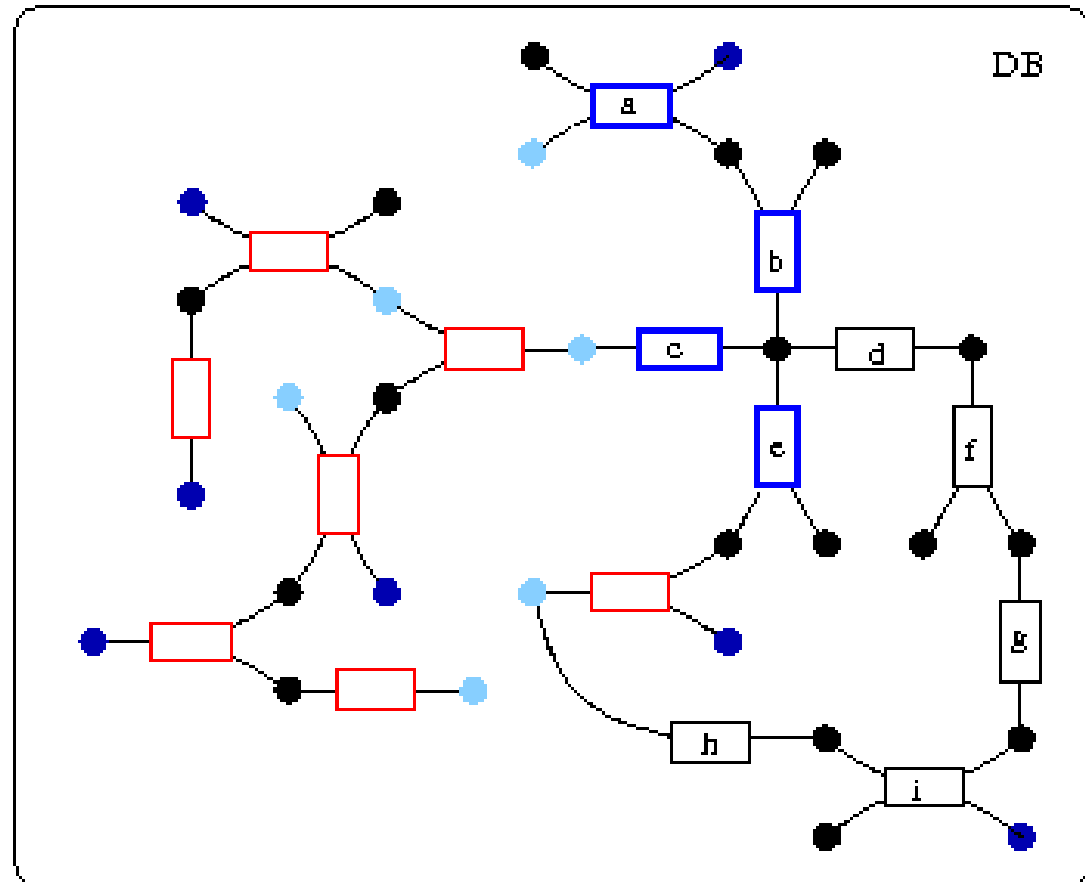
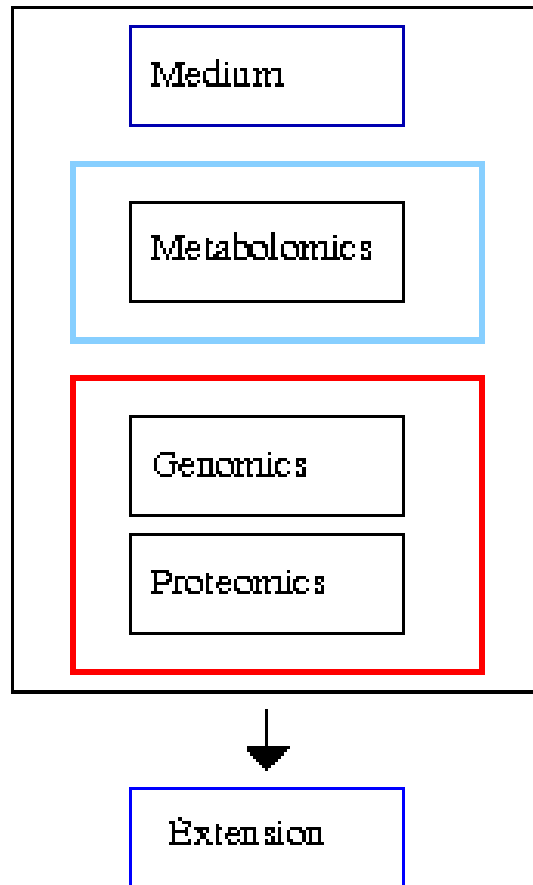
Draft network

Filling the gaps



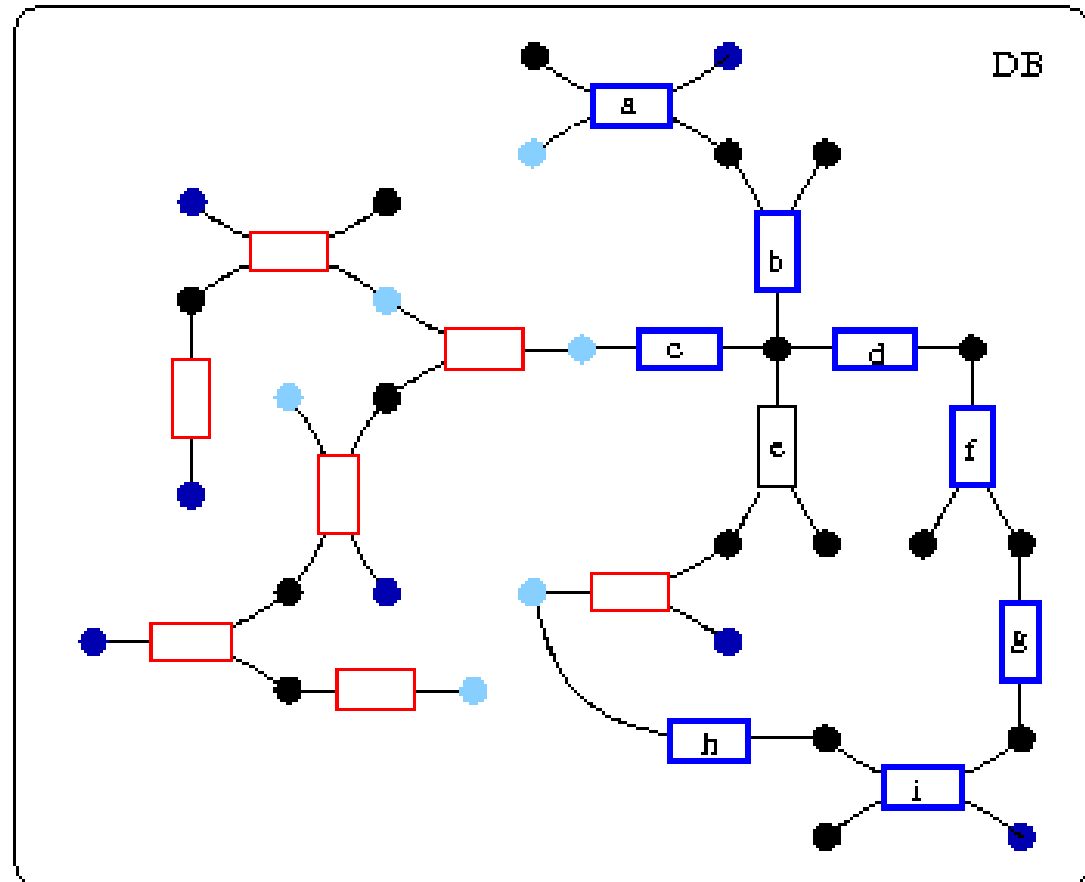
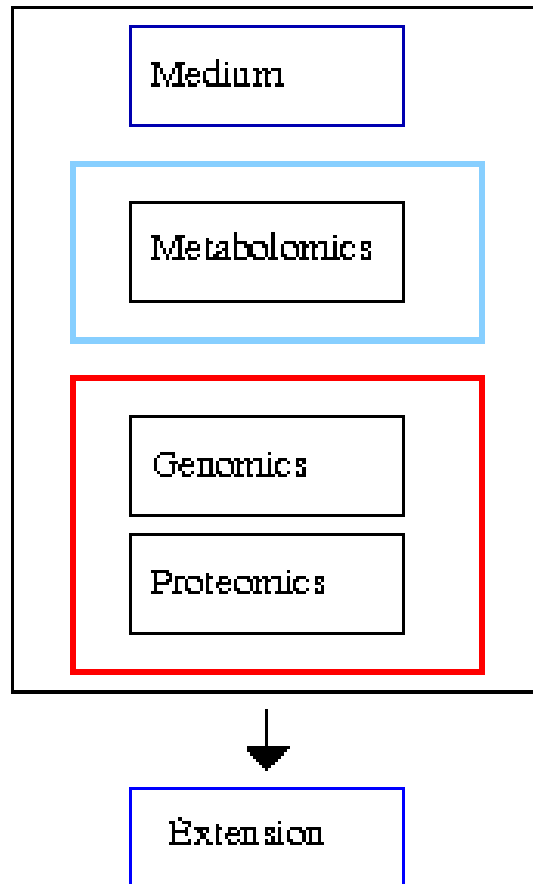
Draft network embedded in larger network (from database)

Filling the gaps



Solution 1: minimal extension with 4 reactions

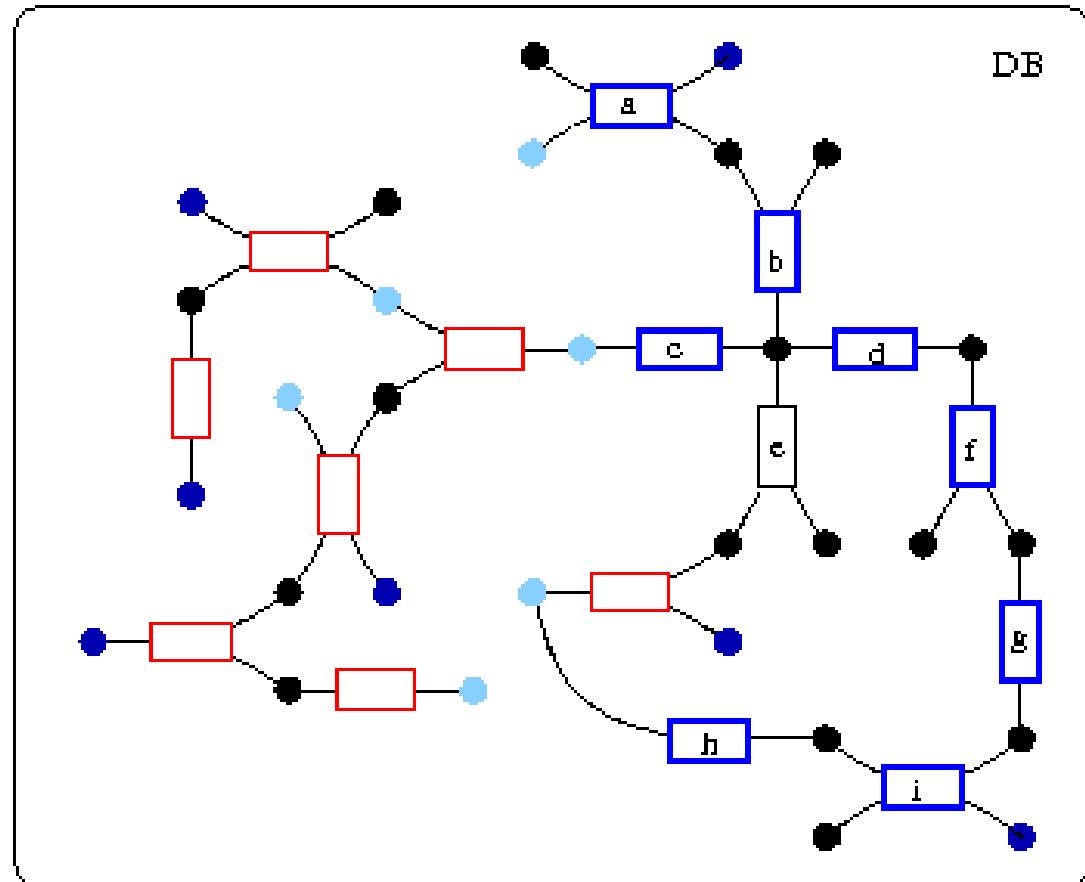
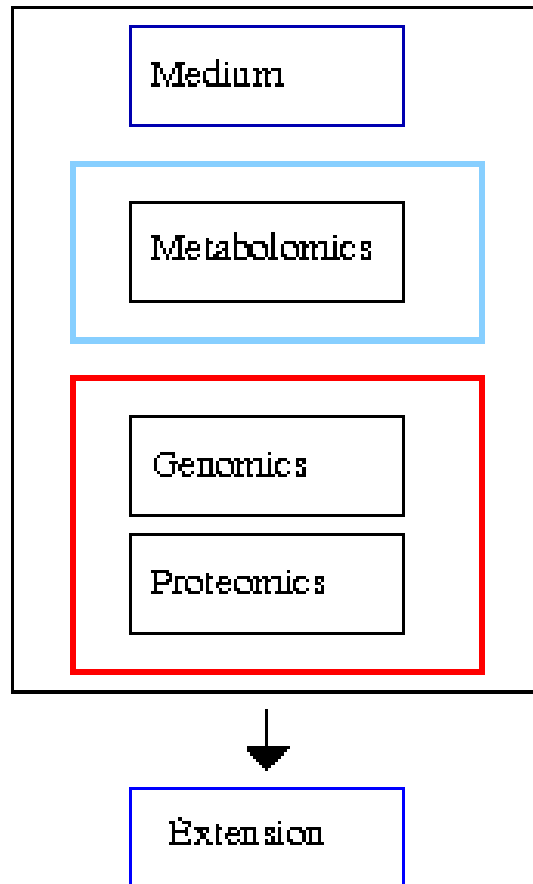
Filling the gaps



Solution 1: minimal extension with 4 reactions

Solution 2: minimal extension with 8 reactions

Filling the gaps



- greedy algorithm (traversing all reactions)
- depends on the order of the reaction lists

Solution 1: minimal extension with 4 reactions

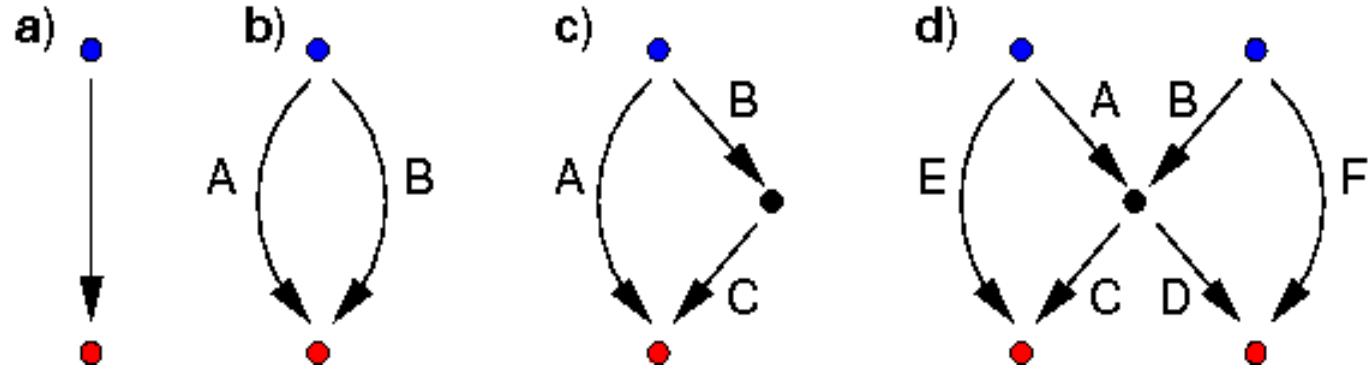
Solution 2: minimal extension with 8 reactions

Simple scenarios

nutrients \longrightarrow

possible missing reactions

observed \longrightarrow



Minimal solutions:

A

A
B

A
B+C

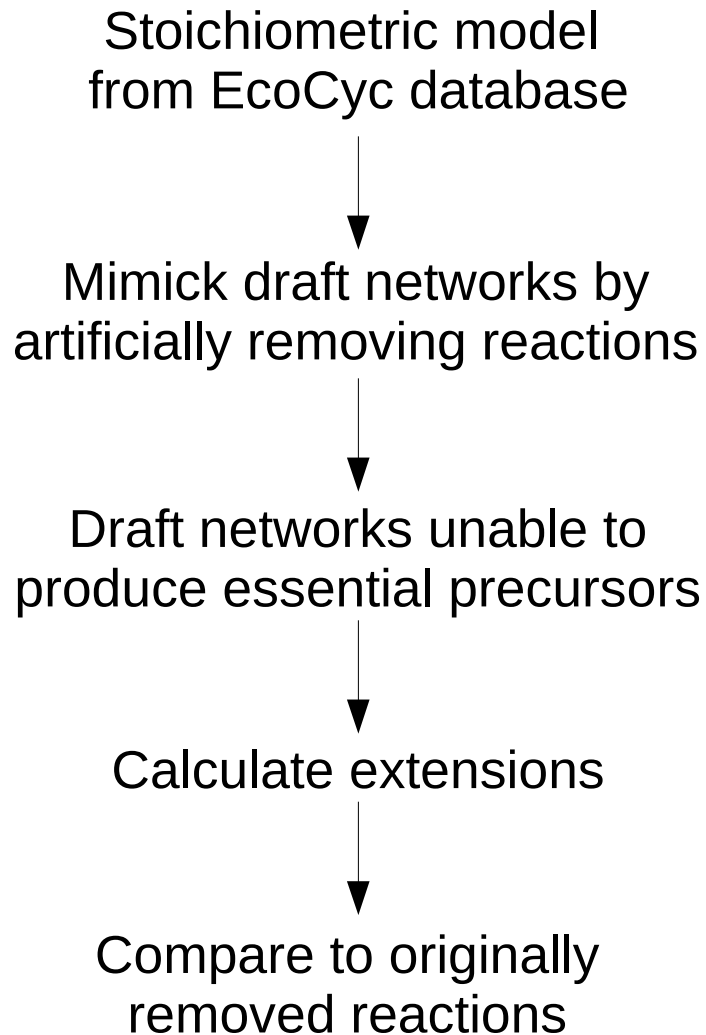
A+C+D
A+C+F
A+D+E
B+C+D
B+C+F
B+D+E
E+F

In a realistic case there will be a multitude of solutions!

HOW CAN WE IDENTIFY THE CORRECT SOLUTION?

Case study

Test method on well investigated organism: *E. coli*



Case study

Test method on well investigated organism: *E. coli*



Stoichiometric model
from EcoCyc database

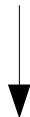


Mimick draft networks by
artificially removing reactions

400 draft networks
(100 each with 20,50,100,200 reactions removed)

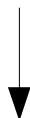


Draft networks unable to
produce essential precursors



Calculate extensions

100 extensions
for all 400 cases



Compare to originally
removed reactions

Determine prediction quality for all 40000 extensions

Case study

Test method on well investigated organism: *E. coli*



Stoichiometric model
from EcoCyc database



Mimick draft networks by
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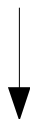


Draft networks unable to
produce essential precursors

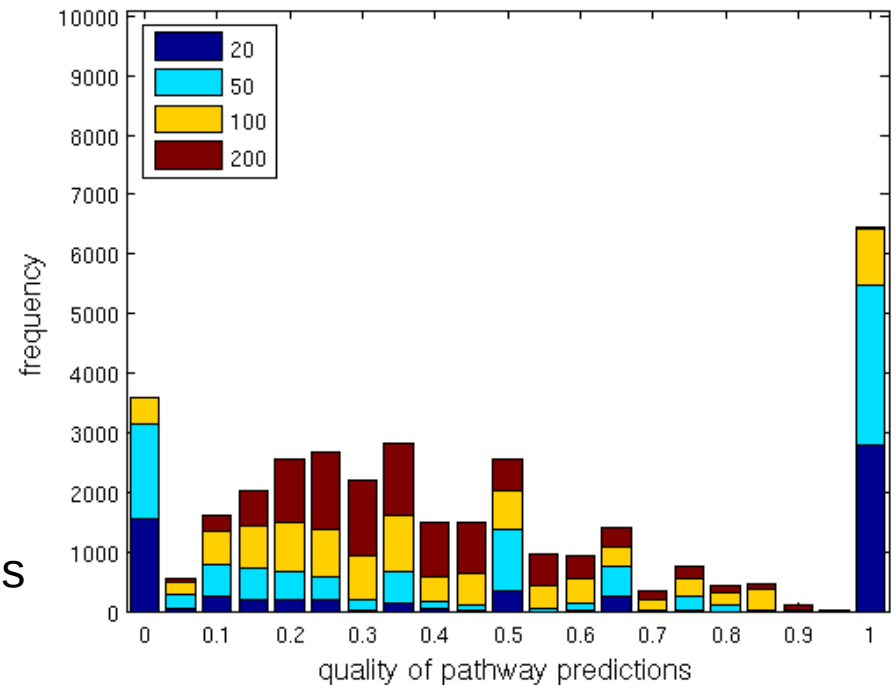


Calculate extensions

100 extensions
for all 400 cases

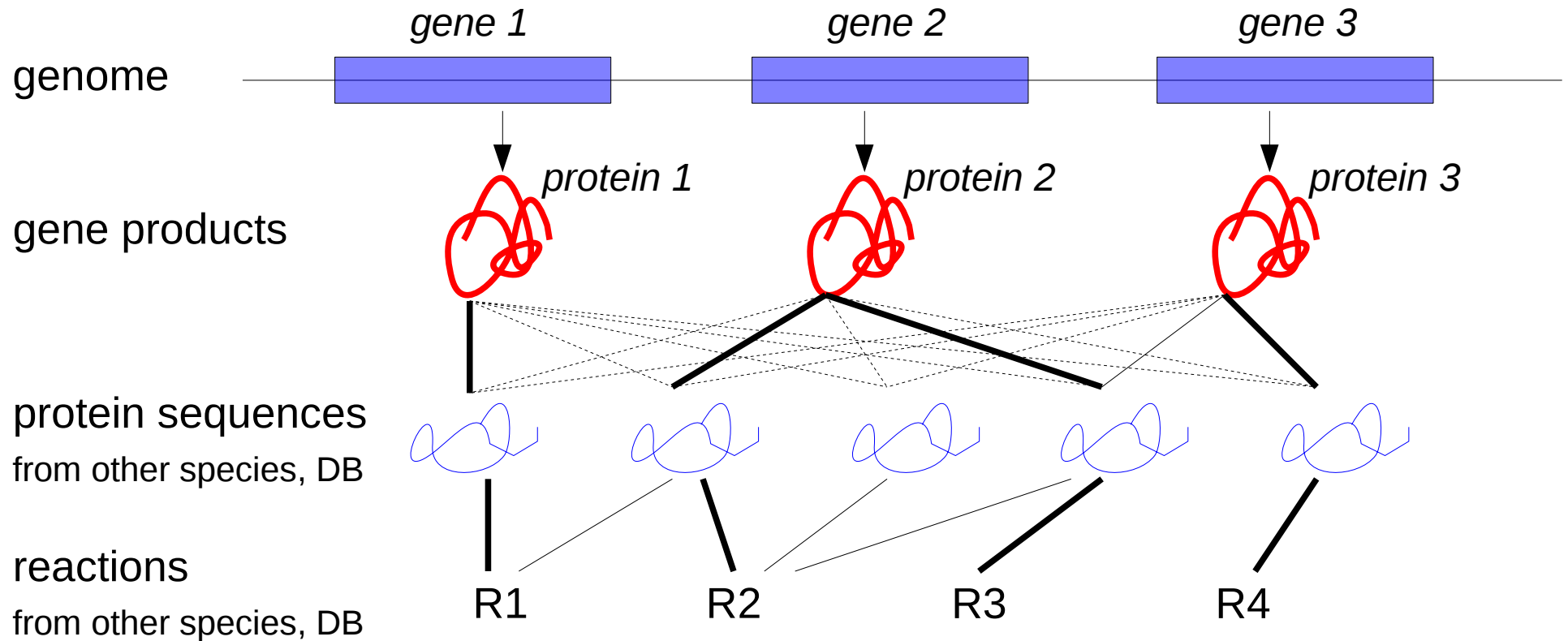


Compare to originally
removed reactions



Determine prediction quality for all 40000 extensions

Including genomic information

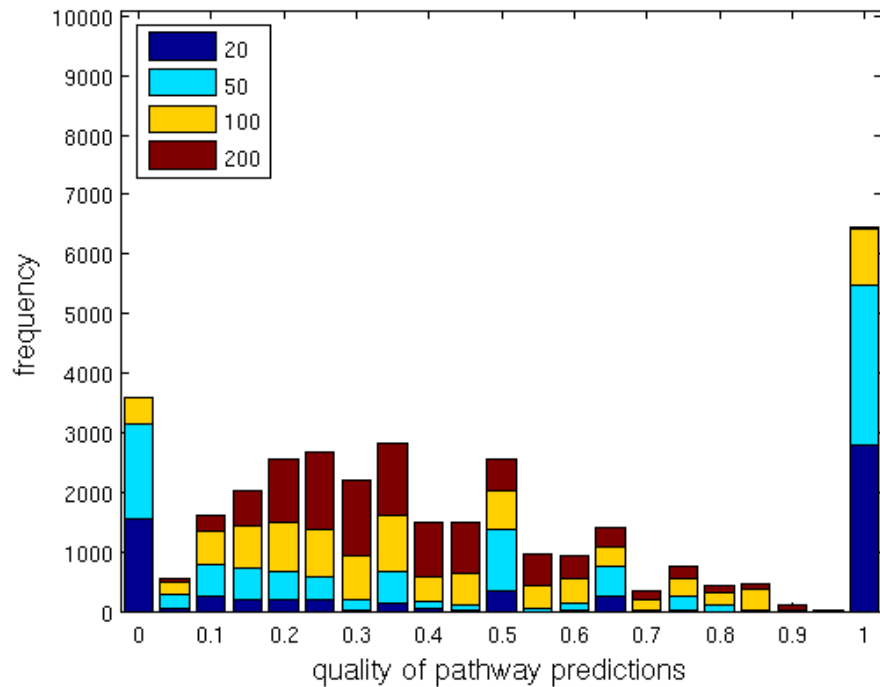


⇒ find best fits and assign scores according to sequence homology

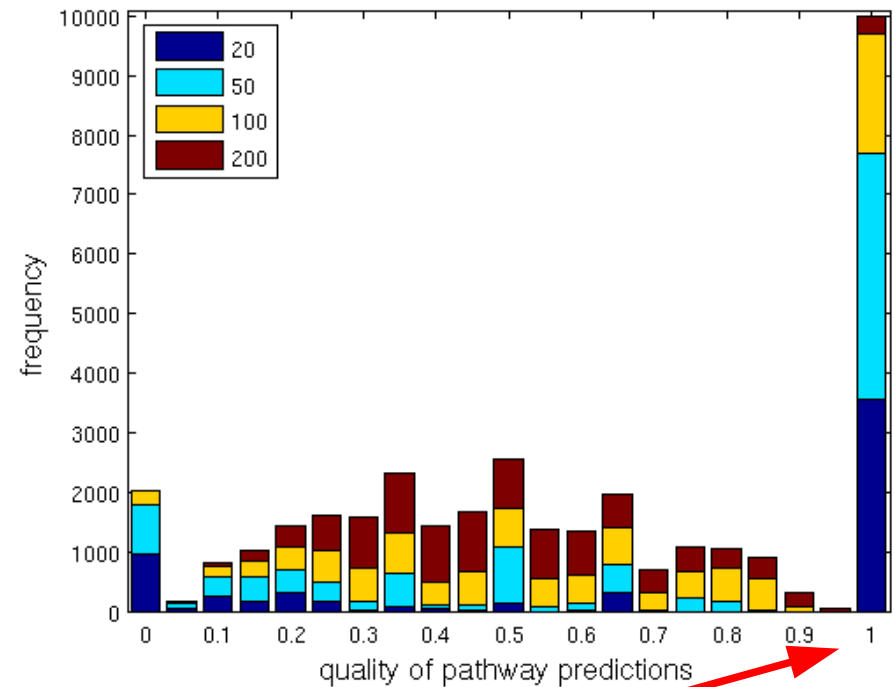
⇒ extensions: preferentially include reactions with good score

Sequence information improves predictions

Fully randomized lists

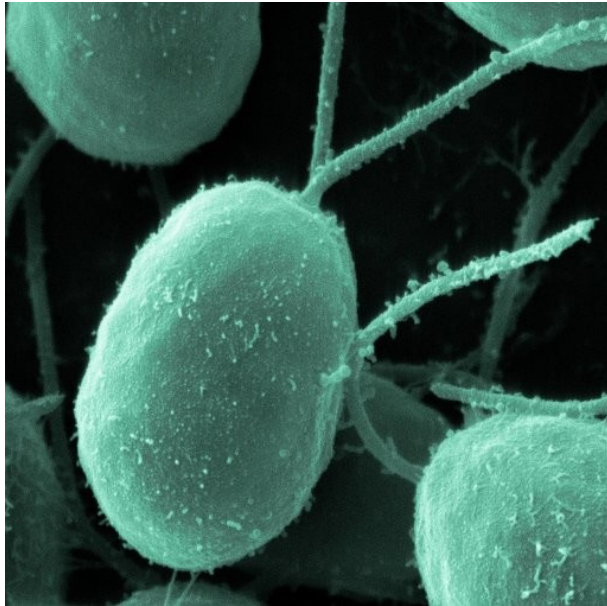


Partly randomized lists
(including sequence information)



fraction of good predictions is considerably improved!

The real world: *Chlamydomonas reinhardtii*

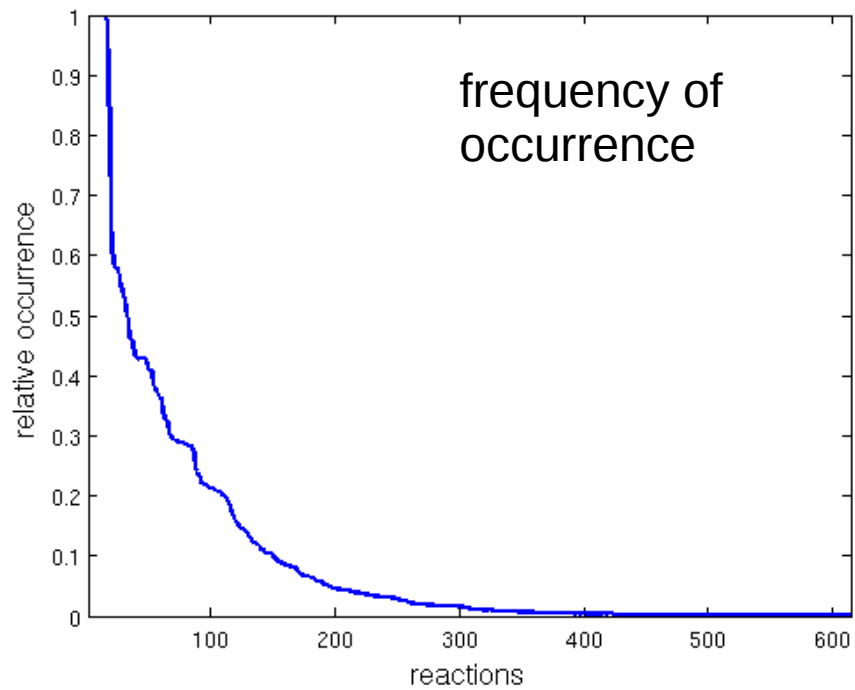
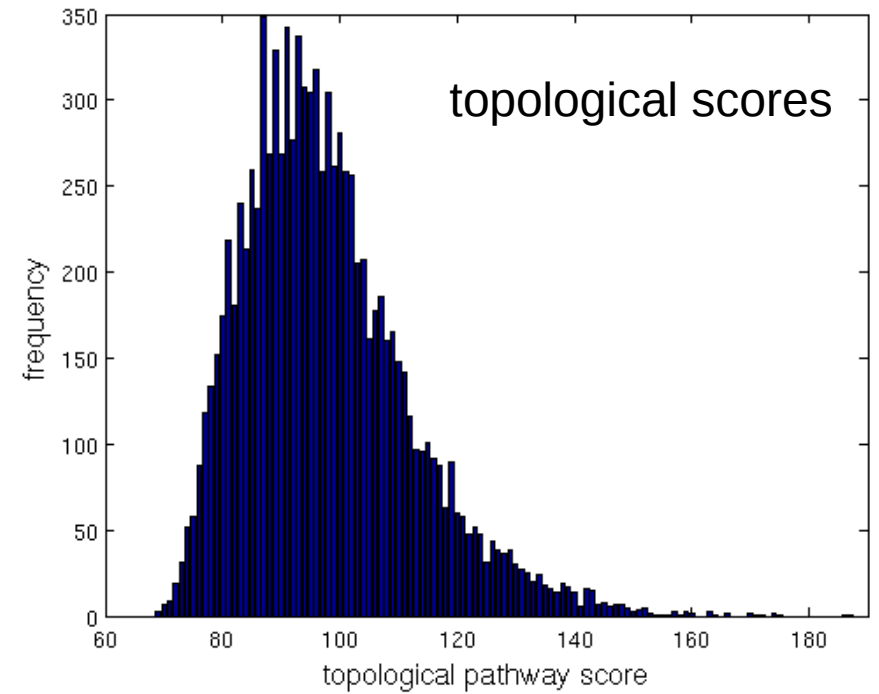
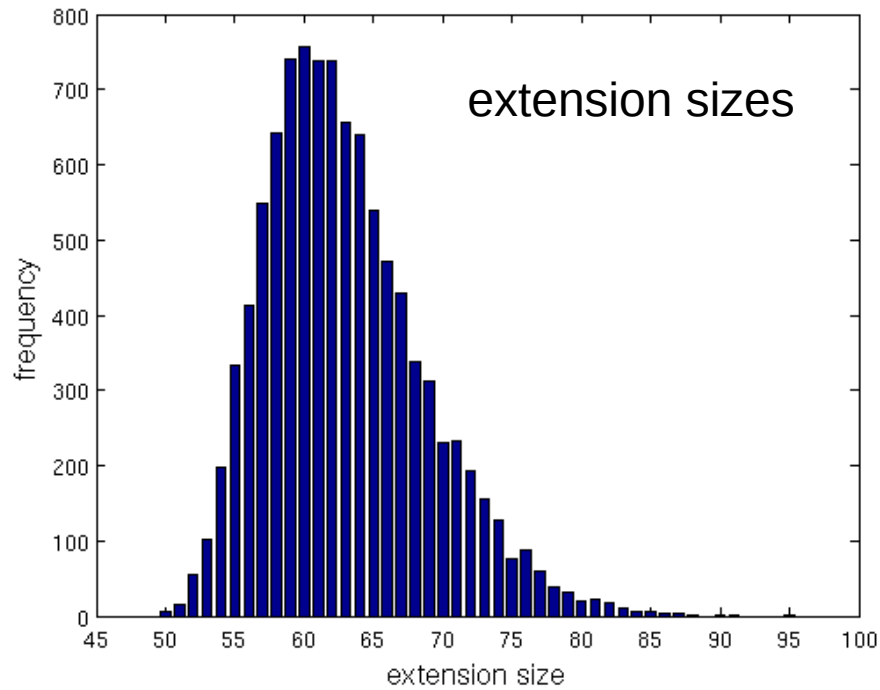


Model organism of the GoFORSYS research consortium (***photosynthesis and growth*** - <http://www.goforsys.de>)

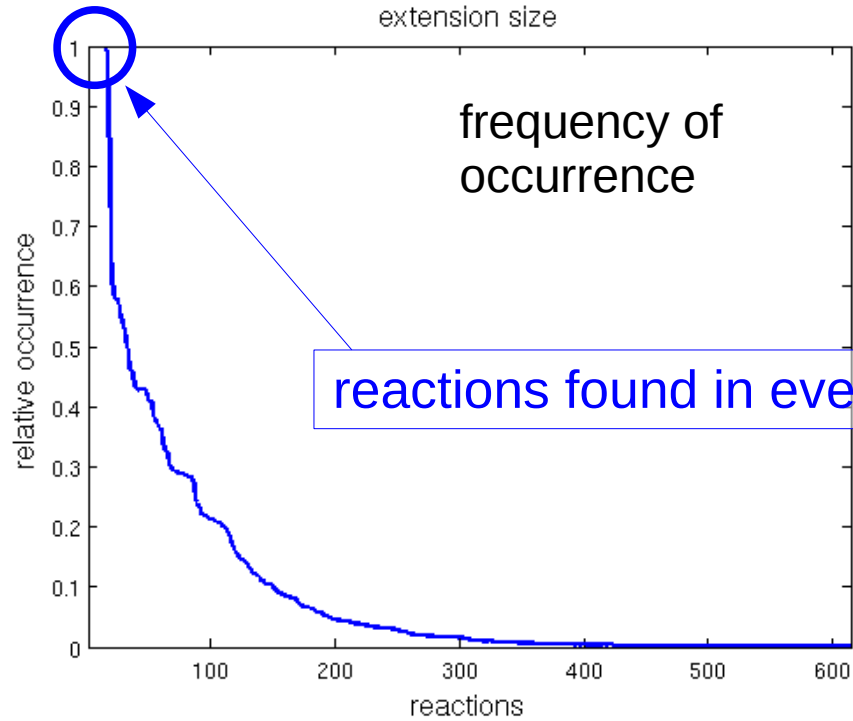
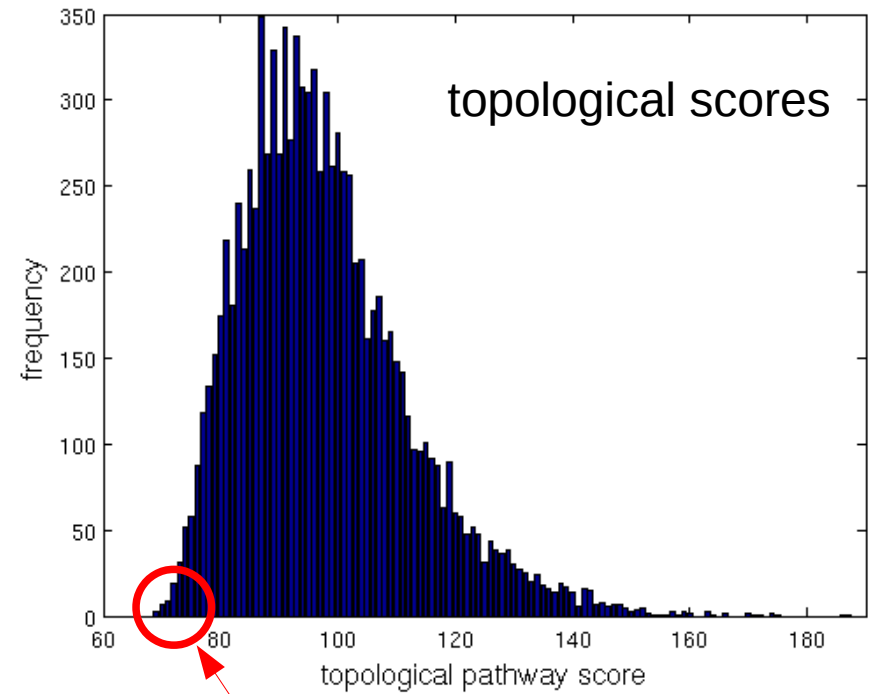
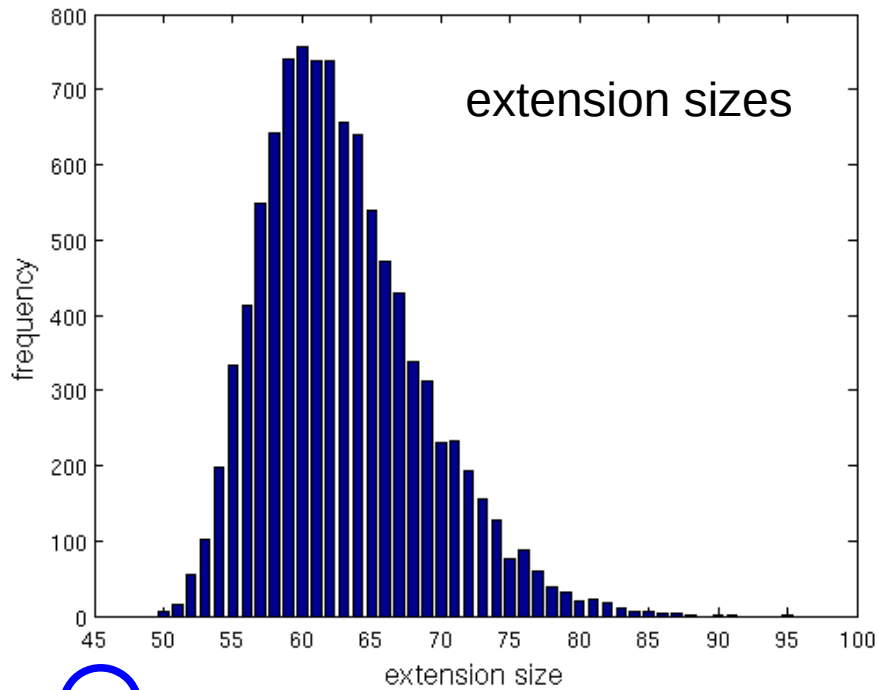
- 15143 genes (JGI)
- 2213 functional annotated genes in KEGG
- 1258 biochemical reactions (Patrick May)
- 159 measured metabolites (Stefan Kempa)
- 30 not producible by draft network

615 distinct reactions in 10000 calculated minimal extensions

Extension results for Chlamy



Extension results for Chlamy

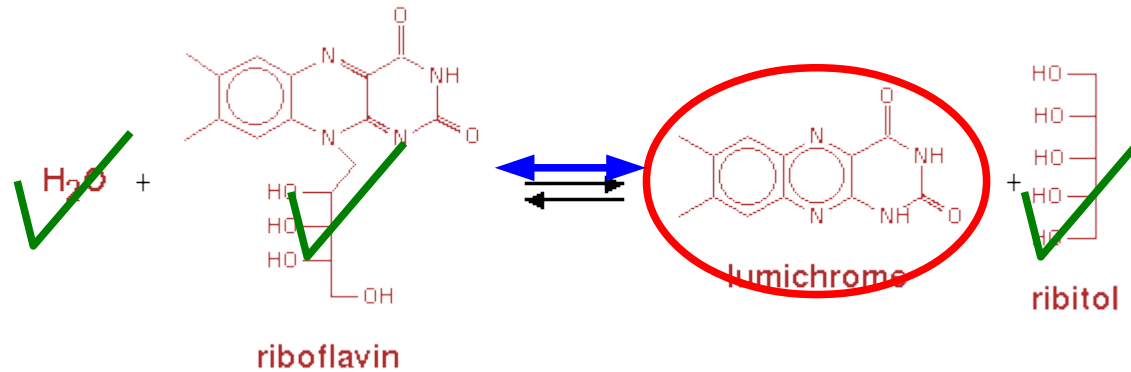


probably good pathway predictions

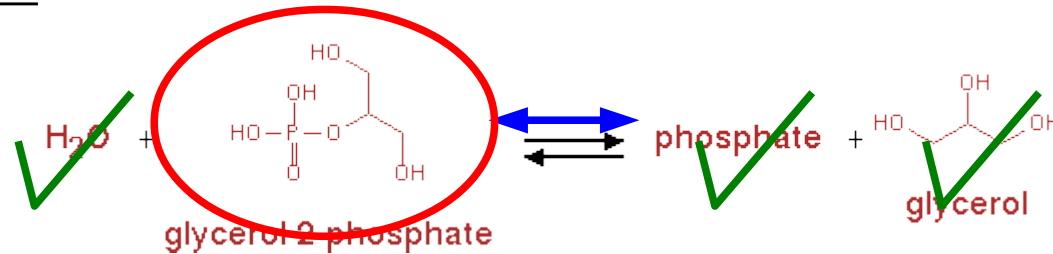
reactions found in every extension (15)

Some specific examples

lumichrome



glycerol 2-phosphate



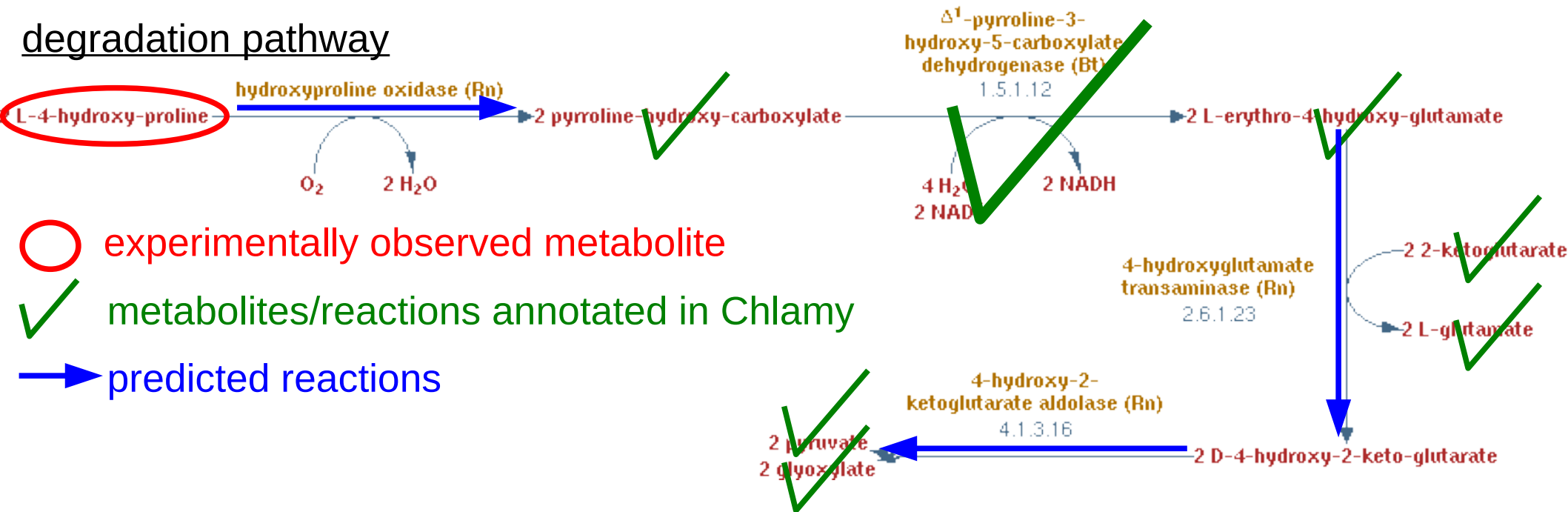
- experimentally observed metabolite
- ✓ metabolites/reactions annotated in Chlamy
- predicted reactions

Completion of a pathway

L-4-hydroxyproline

- in animals: important structural component of collagen
- in plants: found in some glycoproteins and cell wall proteins

degradation pathway

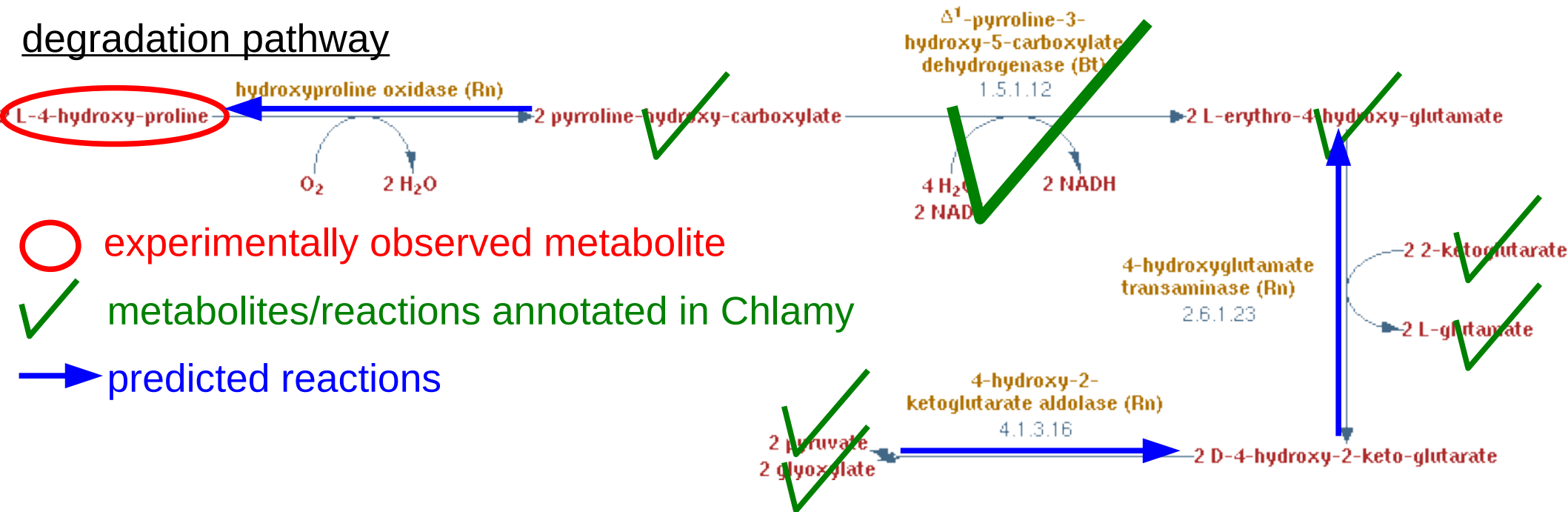


Completion of a pathway

L-4-hydroxyproline

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degradation pathway

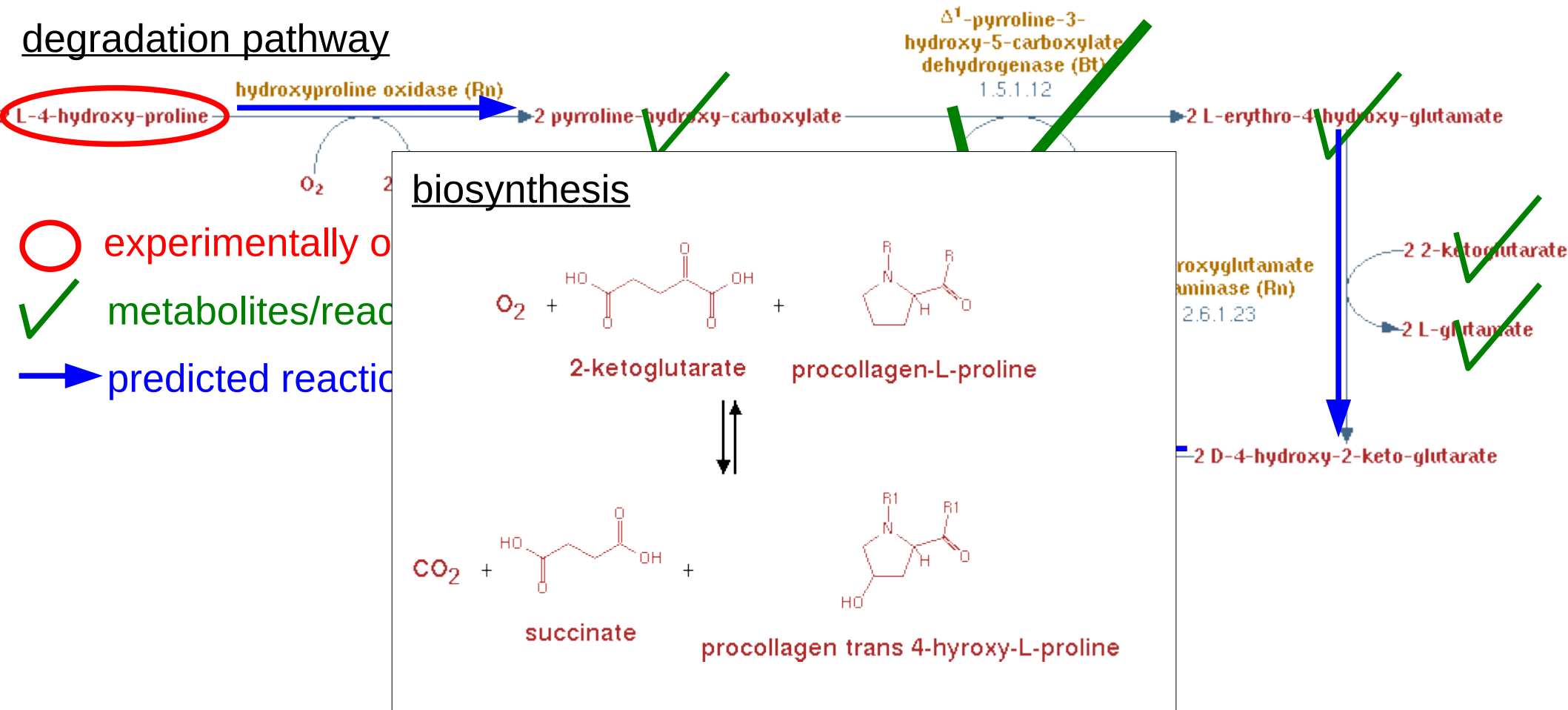


Completion of a pathway

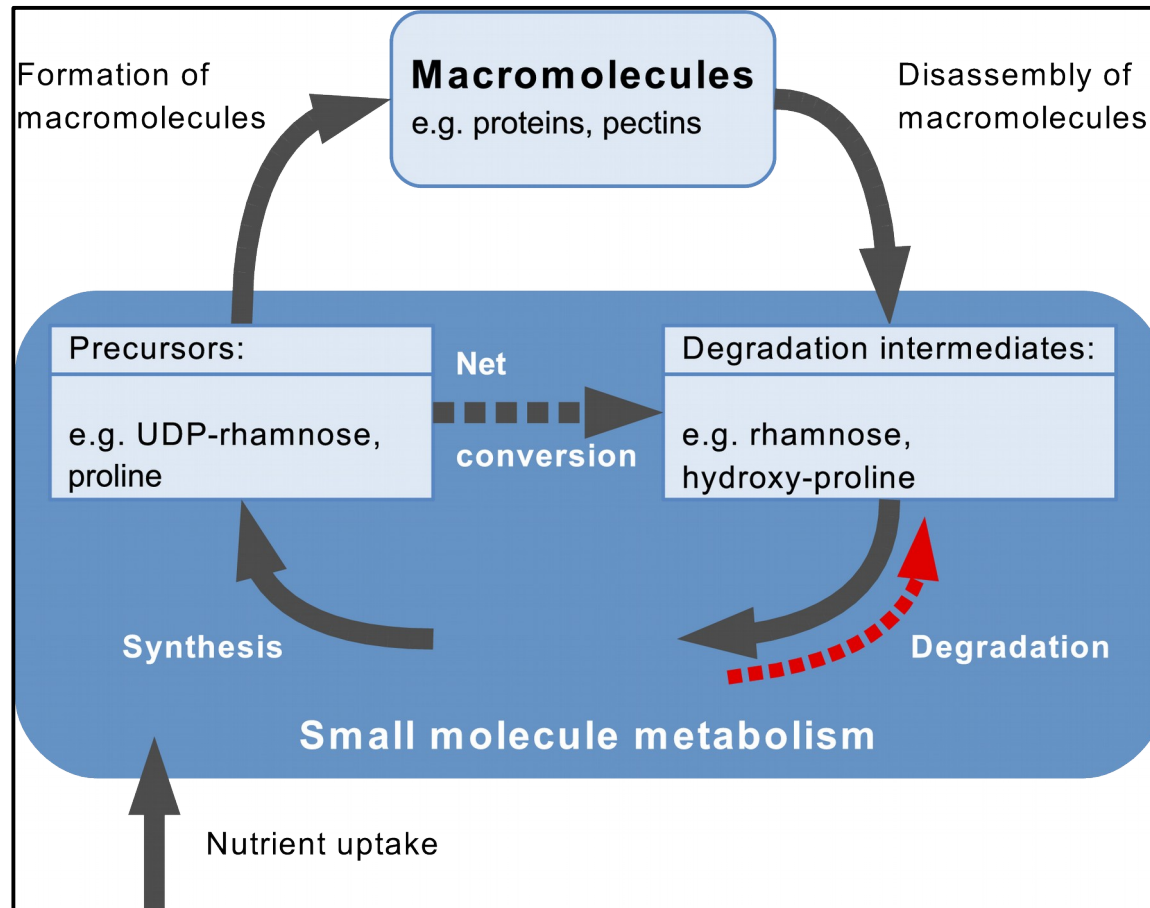
L-4-hydroxyproline

- in animals: important structural component of collagen
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degradation pathway

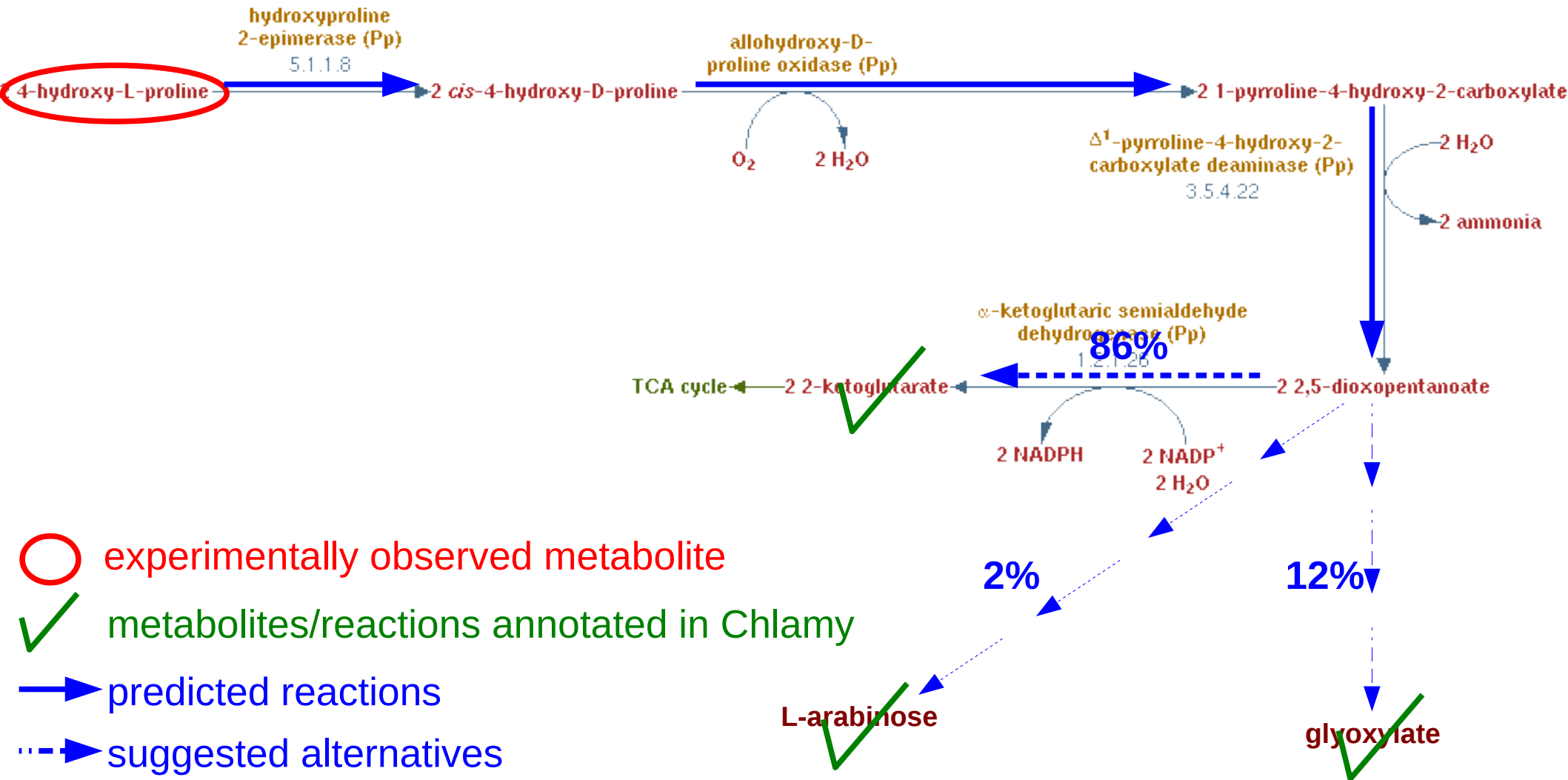


Where are the limits of metabolism?



Prediction of alternative routes

4-hydroxy-L-proline



**HETEROGENEOUS AND
INCOMPLETE DATA**

BIOINFORMATICS

**STRUCTURAL
MODELLING**

INTEGRATION

**TESTABLE
HYPOTHESES**

Table 1: Evidence for predicted reactions.

Target	Reaction/ EC number	Evidence	Comment
Ergosterol	1.14.99.7	+	Blast hit (136985) against human (ERG1)
	1.1.1.270	+	Blast hit (191061) against human (DHB7)
	1.3.1.70	+	orthologs (196516, 126431) to yeast (ERG24)
	1.3.1.71	+/-	Blast hit (196516) against yeast (ERG4)
	1.14.13.70	+	ortholog (196411) to Arabidopsis (AT1G11680)
	1.14.13.72	+	orthologs (142288,186886) to human (NP_006736.1)
	C-8 sterol isomerase	-	Blast hit (160258) against Arabidopsis (AT1G20050) but more likely C-8,7 sterol isomerase (5.3.3.5)
Lumichrome	5.3.3.5	+	ortholog (160258) to Arabidopsis (AT1G20050)
	C-22 sterol desaturase	+	ortholog (196874) to yeast (ERG5)
N-acetyl-L-phenylalanine	3.5.99.1	-	no hit
L-rhamnose	2.3.1.53	-	no sequences available
	5.3.1.14	-	no hit
	2.7.1.5	-	no hit
	4.1.2.19	-	no hit
	2.7.7.64	+	ortholog (32796) to Arabidopsis (AT5G52560)
	3.1.3.23	+/-	Blast hit (196269) to <i>E. coli</i> (SUPH)
	Hydroxyproline	hydroxyproline oxidase	+
2.6.1.23		-	maybe 2.6.1.1
4.1.3.16		-	no sequences available
Phenylacetaldehyde	4.1.1.43	+	ortholog (135197) to yeast PDC5
	4.1.1.53	+	Blast hit (40158) to <i>Solanum lycopersicum</i> AADC1A

(Christian et al., Mol BioSystems, 2009)

Organisms and their environment

No organism lives in complete isolation

Organisms shape the environment (e.g. by excreted products)

Organisms are themselves part of the environment of others (ecosystem)

Interaction on the level of metabolic networks

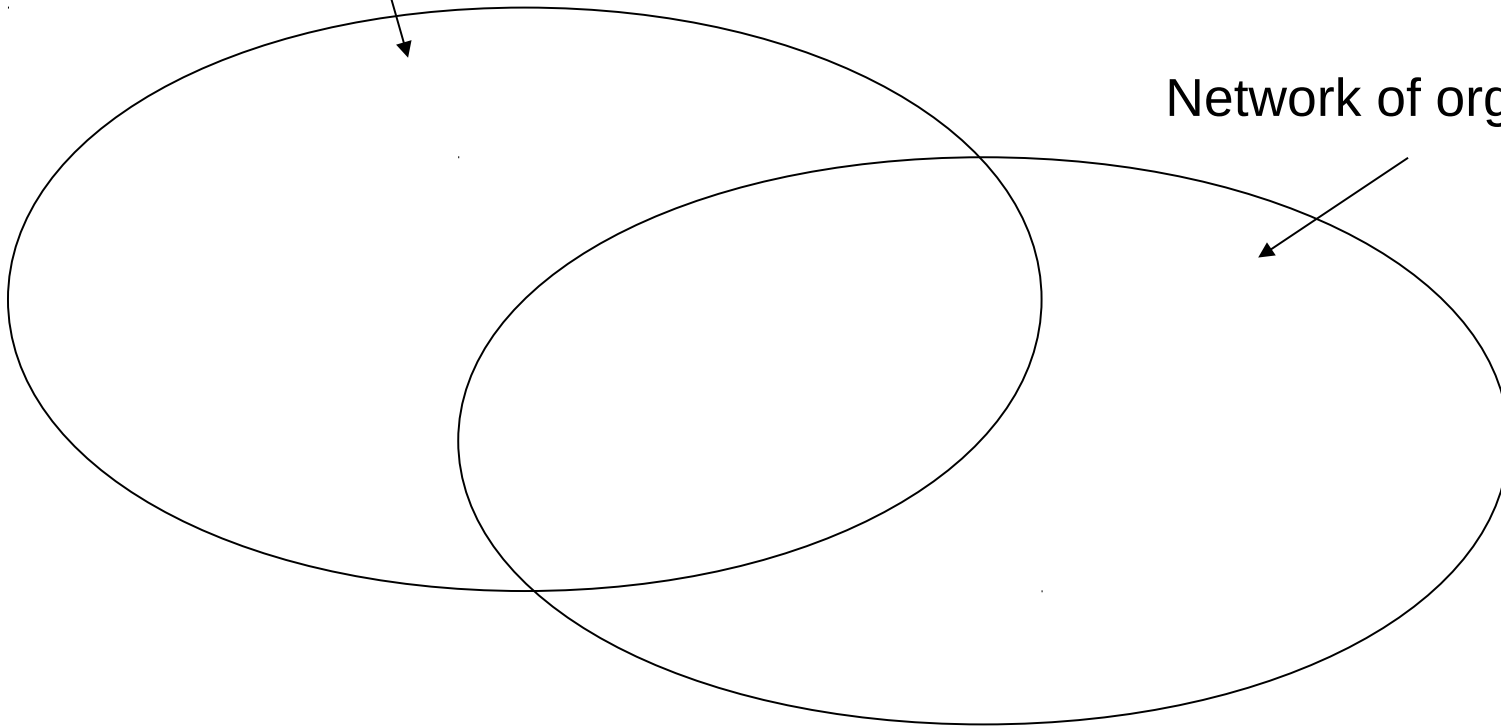
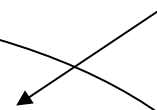
- **Biodegradation**
involves many microorganisms, requires the special metabolic capabilities
- **Symbiosis**
e.g. plants (fabaceae) and Rhizobia (nitrogen fixing bacteria)
- **Parasitism**
e.g. Wolbachia live inside insect cells

Metabolic synergy

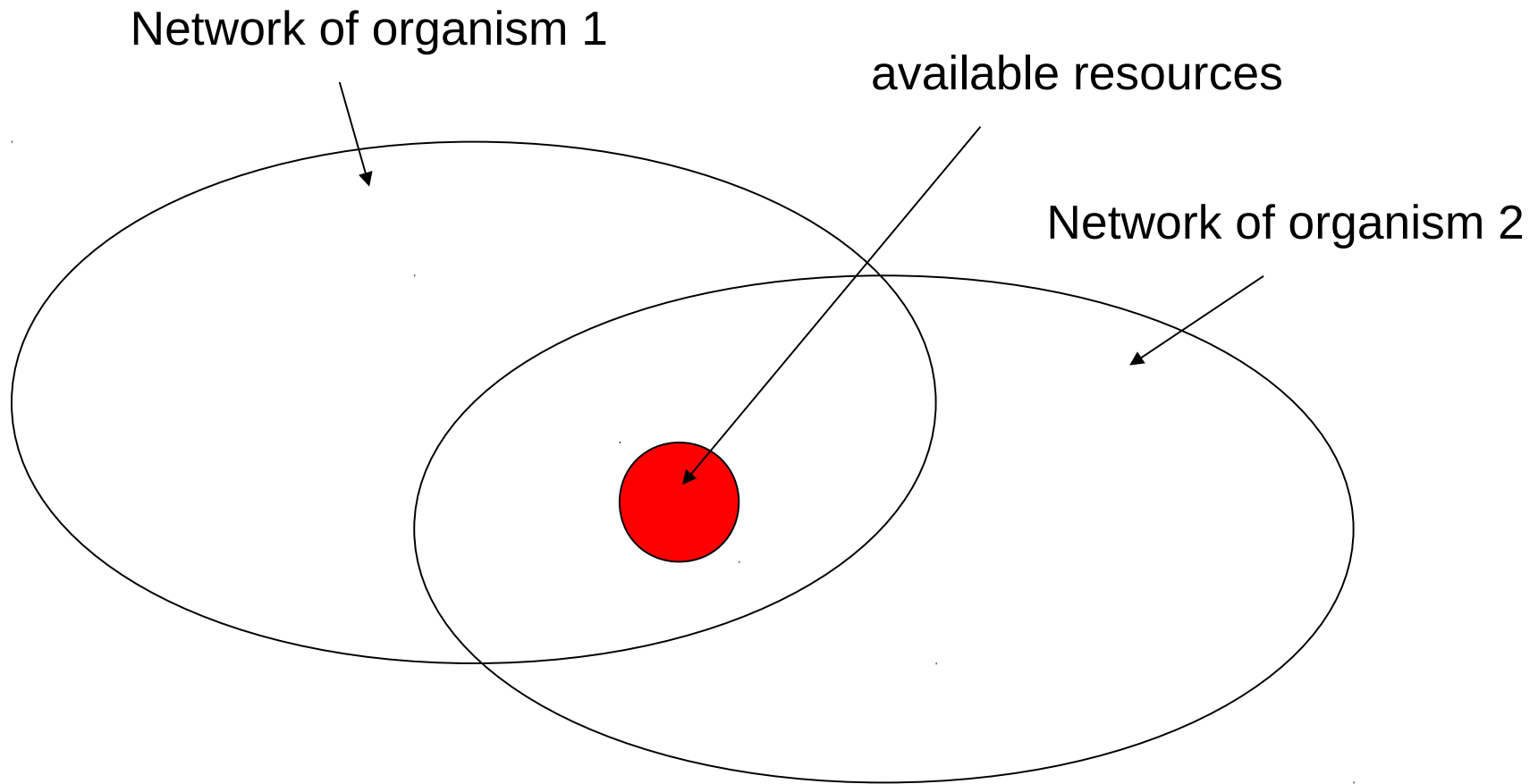
Network of organism 1



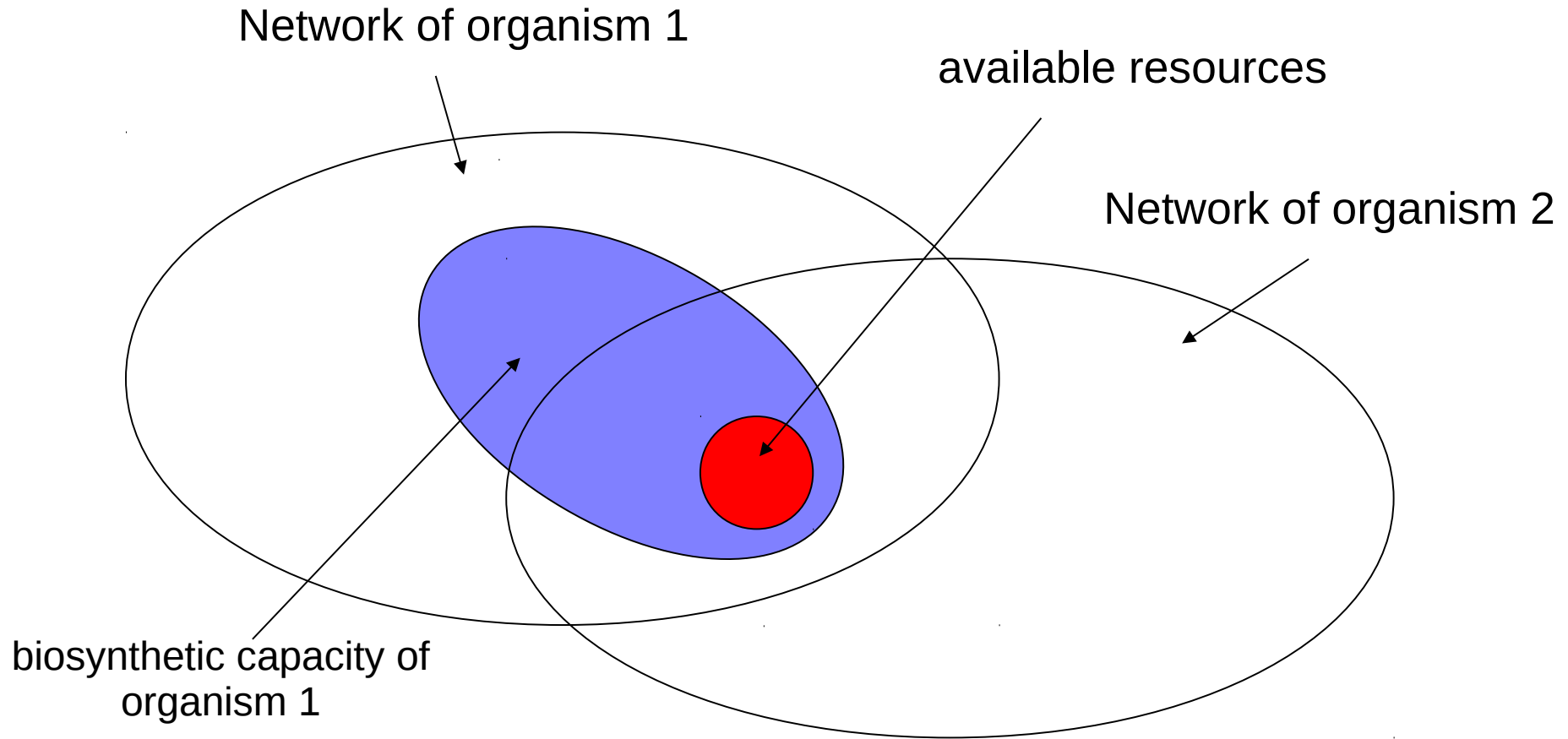
Network of organism 2



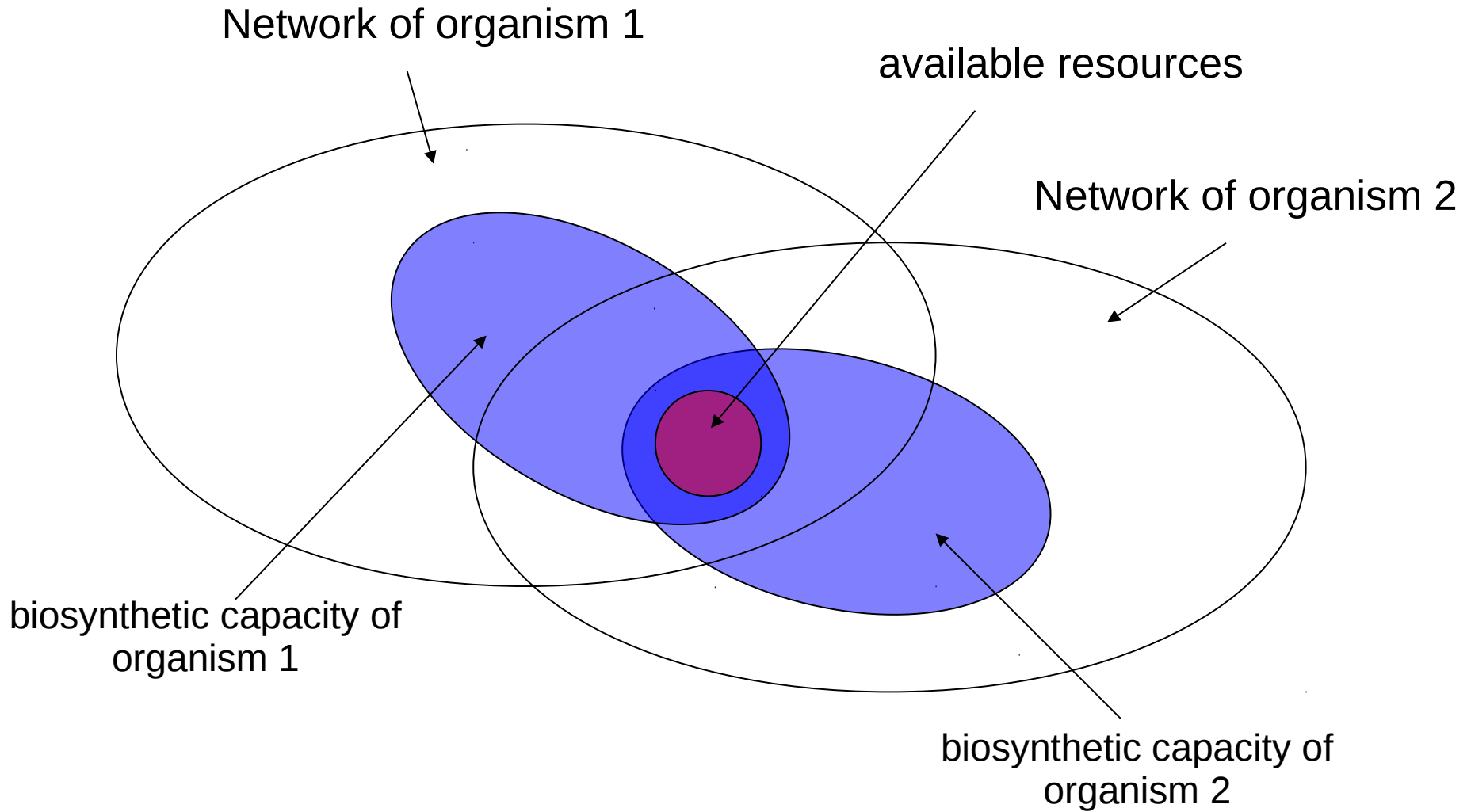
Metabolic synergy



Metabolic synergy



Metabolic synergy



Metabolic synergy

Network of organism 1

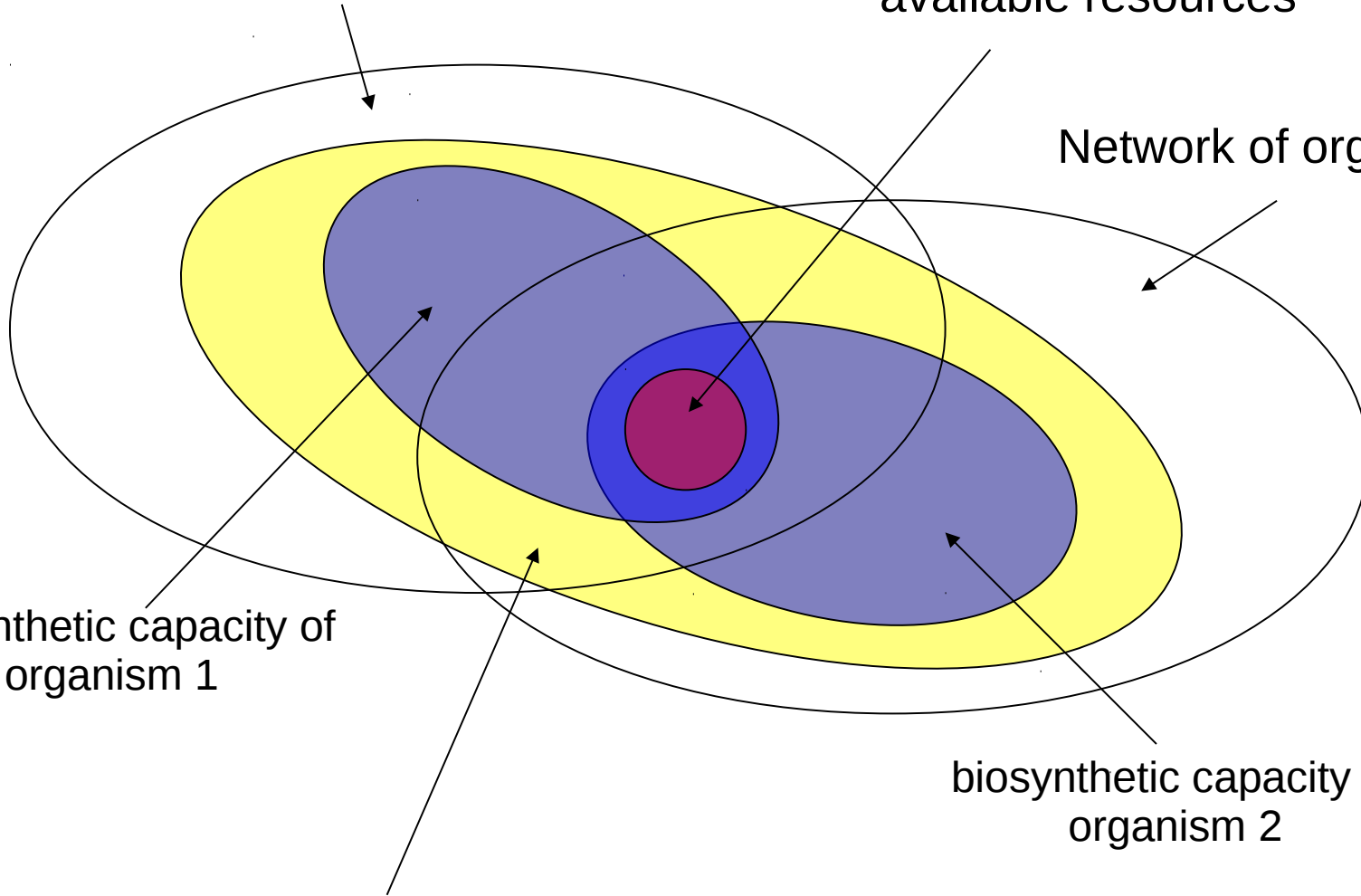
available resources

Network of organism 2

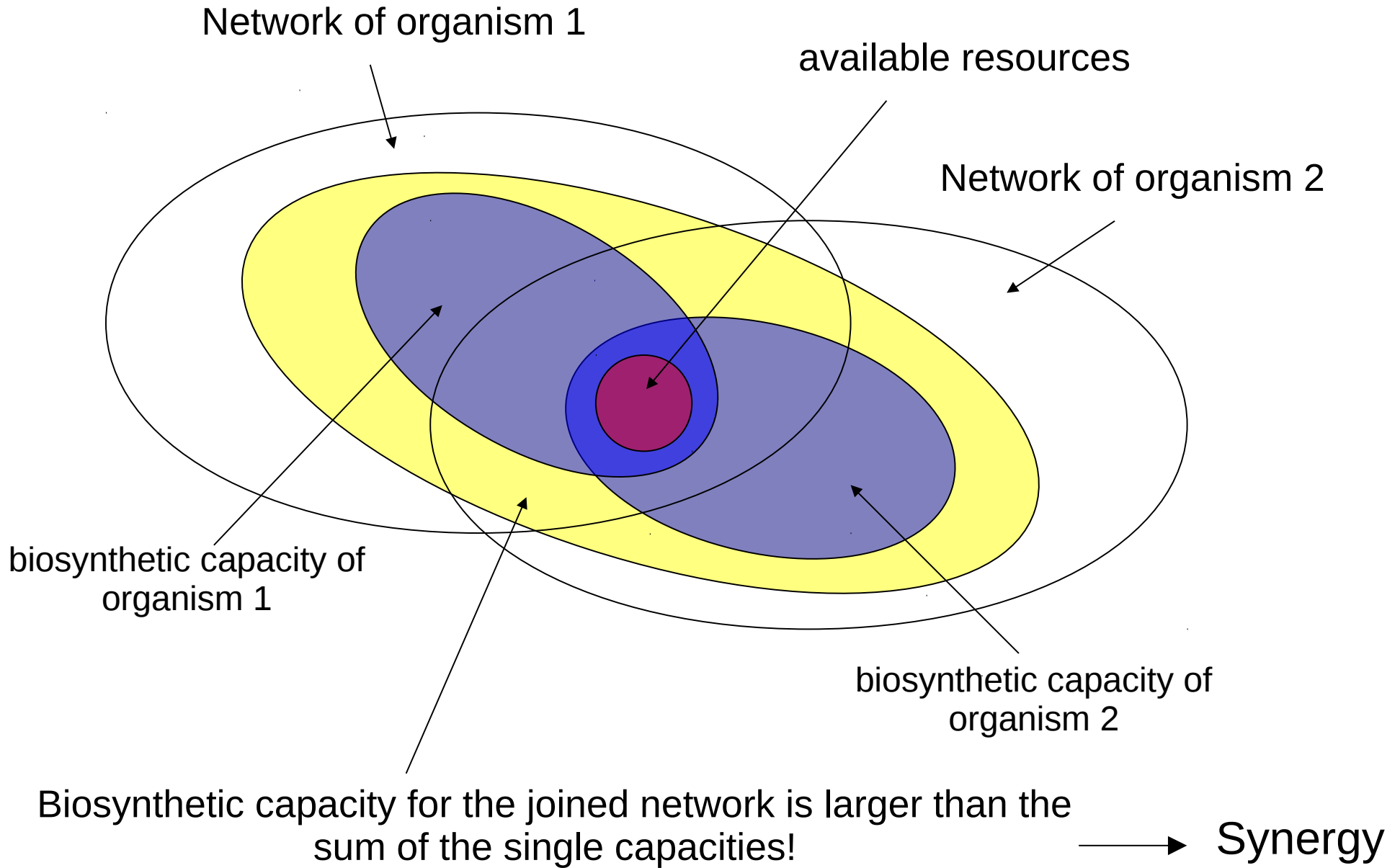
biosynthetic capacity of
organism 1

biosynthetic capacity of
organism 2

Biosynthetic capacity for the joined network is larger than the
sum of the single capacities!



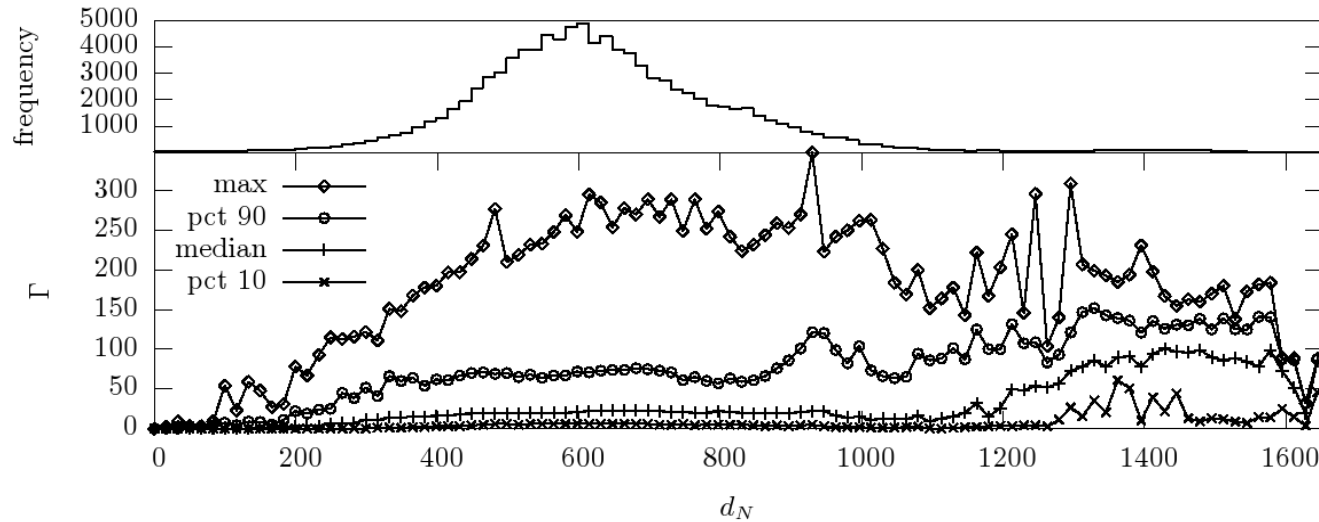
Metabolic synergy



Synergy vs. network dissimilarity

Statistics...

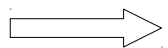
Which pairs are best suited to yield synergetic effects?



(Christian, Handorf and Ebenh oh, 2007)

A simplistic view with lots of space for improvement:

- Transport processes
- Quantification of negative effects (FBA)
- ...



Investigate specific examples

Literature

- Ebenhöh, O.; Handorf, T. & Heinrich, R.
Structural analysis of expanding metabolic networks.
Genome Inform, 2004, 15, 35-45
- Handorf, T.; Ebenhöh, O. & Heinrich, R.
Expanding metabolic networks: scopes of compounds, robustness, and evolution.
J Mol Evol, 2005, 61, 498-512
- Handorf, T.; Ebenhöh, O.; Kahn, D. & Heinrich, R.
Hierarchy of metabolic compounds based on their synthesising capacity.
Syst Biol (Stevenage), 2006, 153, 359-363
- Ebenhöh, O.; Handorf, T. & Kahn, D.
Evolutionary changes of metabolic networks and their biosynthetic capacities.
Syst Biol (Stevenage), 2006, 153, 354-358
- Christian, N.; Handorf, T. & Ebenhöh, O.
Metabolic synergy: increasing biosynthetic capabilities by network cooperation.
Genome Inform, 2007, 18, 321-330
- Kruse, K. & Ebenhöh, O.
Comparing Flux Balance Analysis to Network Expansion: Producibility, Sustainability and the Scope of Compounds
Genome Inform, 2008, 20, 91-101
- May, P.; Wienkoop, S.; Kempa, S.; Usadel, B.; Christian, N.; Rupprecht, J.; Weiss, J.; Recuenco-Munoz, L.; Ebenhöh, O.;
Weckwerth, W. & Walther, D.
Metabolomics- and Proteomics-Assisted Genome Annotation and Analysis of the Draft Metabolic Network of Chlamydomonas reinhardtii.
Genetics, 2008, 179, 157-166
- Matthäus, F.; Salazar, C. & Ebenhöh, O.
Biosynthetic potentials of metabolites and their hierarchical organization.
PLoS Comput Biol, 2008, 4, e1000049
- Handorf, T.; Christian, N.; Ebenhöh, O. & Kahn, D.
An environmental perspective on metabolism.
J Theor Biol, 2008, 252, 530-537
- Ebenhöh, O. & Handorf, T.
Functional Classification Of Genome-Scale Metabolic Networks
EURASIP Journal on Bioinformatics and Systems Biology, 2009
- Christian, N.; May, P.; Kempa, S.; Handorf, T. & Ebenhöh, O.
An integrative approach towards completing genome-scale metabolic networks.
Mol Biosyst, 2009, 5, 1889-1903